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Heat Removal Efficiency of Stratum Ventilation for Air-side Modulation

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Abstract

Stratum ventilation has significant thermal non-uniformity between the occupied and upper zones. Although the non-uniformity benefits indoor air quality and energy efficiency, it increases complexities and difficulties in the air-side modulation. In this study, a heat removal efficiency (HRE) model is first established and validated, and then used for the air-side modulation. The HRE model proposed is a function of supply air temperature, supply airflow rate and cooling load. The HRE model proposed has been proven to be applicable to stratum ventilation and displacement ventilation for different room geometries and air terminal configurations, with errors generally within $\pm 5\%$ and a mean absolute error less than 4% for thirty-three experimental cases and five simulated cases. Investigations into the air-side modulation with the proposed HRE model reveal that for both the typical stratum-ventilated classroom and office, the variable-air-volume system can serve a wider range of cooling load than the constant-air-volume system. The assumption of a constant HRE used in the conventional method could lead to errors in the room temperature prediction up to $\pm 1.3^{\circ}$ C, thus the proposed HRE model is important to the

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air-side modulation for thermal comfort. An air-side modulation method is proposed based on the HRE model to maximize the HRE for improving energy efficiency while maintaining thermal comfort. Results show that the HRE model based air-side modulation can improve the energy efficiency of stratum ventilation up to 67.3%. The HRE model based air-side modulation is also promising for displacement ventilation.

Keywords: Heat removal efficiency; Experiment and modeling; Stratum ventilation; Displacement ventilation; Non-uniformity; Air-side modulation

| Nomenclature | | | | | | | | |
|-----------------|---|-------|-------------------------|--|--|--|--|--|
| <i>a</i> , b, c | constant coefficients in HRE model | Abbre | viations | | | | | |
| c _p | specific heat capacity of air (kJ/(kg• ⁰ C)) | ACH | air changes per hour | | | | | |
| ρ | air density (kg/m ³) | CAV | constant-air-volume | | | | | |
| $Q_{\rm cl}$ | cooling load (kW) | HRE | heat removal efficiency | | | | | |
| T _e | exit air temperature (⁰ C) | PMV | Predicted Mean Vote | | | | | |
| T _r | room temperature (⁰ C) | SV | stratum ventilation | | | | | |
| T _s | supply air temperature (⁰ C) | VAV | variable-air-volume | | | | | |
| Vs | supply airflow rate (m ³ /s) | | | | | | | |

1. Introduction

Improving energy efficiency of HVAC is a critical mission for low and zero energy buildings [1, 2]. HVAC provides thermal comfort, but accounts for the largest amount of building energy consumption, e.g., around 50%, 35% and 40% in commercial buildings in the US, UK and Spain respectively [3]. Reducing energy consumption of ventilation system plays a vital role in improving the energy efficiency of HVAC systems [4-7]. The conventional air distribution, mixing ventilation, creates an acceptable thermal environment with a penalty of high energy consumption [8]. Mixing ventilation conditions the space uniformly, leading to wasteful energy use in conditioning the upper zone (without occupants) [9]. Collective air distributions (e.g., displacement ventilation and stratum ventilation) focus on the occupied zone, with a non-uniform thermal environment between the occupied zone and upper unoccupied

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zone [10]. Because of the non-uniformity, part of the energy used for the unoccupied upper zone is saved [11].

Stratum ventilation delivers conditioned air horizontally to the breathing zone, so that air in the breathing zone is young [12, 13]. Stratum ventilation generates a sandwich temperature and velocity profiles, with the lowest temperature and highest velocity at the head level [14, 15], which cools the body more effectively for thermal comfort [16, 17]. A series of experimental, numerical and human subjective studies have shown that stratum ventilation can robustly achieve satisfactory thermal comfort with symmetrically/asymmetrically distributed heat gains [18-22], and provide quality inhaled air [12, 23, 24]. Annual energy performance simulations found that stratum ventilation is applicable to small-to-medium-sized rooms and has been studied for offices, classrooms and retail shops [25].

However, the air-side modulation of the room temperature with stratum ventilation lacks investigations. The non-uniform thermal environment makes it challenging to predict the room temperature [26, 27]. Without accurate prediction of the room temperature, thermal comfort and energy efficiency might not be assured during building operation [28, 29]. Huan et al. [26] developed a multiple-node model for predicting the room temperature of stratum ventilation. This method has the application potential for the annual energy performance evaluation with building energy simulation tools when the cooling load of the non-uniform thermal environment is carefully estimated [30]. However, regarding the real building operation, it requires additional sensors for the wall temperatures/heat fluxes besides the sensors used in common practice for the supply airflow rate, supply air temperature and exit air temperature [26]. The additional sensors increase the cost and control complexities in practice [31, 32].

The air-side modulation based on the heat removal efficiency (HRE) is a promising solution to the collective air distributions with a non-uniform thermal environment [25, 33-37]. With the HRE, supply condition (i.e., supply airflow rate and supply air temperature) and exit air temperature, the room temperature can be predicted and appropriately modulated for thermal comfort [35, 37]. Since the supply condition and

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exit air temperature can be conveniently obtained with sensors installed under common practice [38], the aforementioned additional sensor cost and control complexities can be avoided by adopting the HRE based air-side modulation. Besides, the HRE, as a ventilation effectiveness index, is also widely used to reflect the efficiency of energy use [10, 39, 40]. Improving the HRE during the air-side modulation can improve the energy efficiency of the ventilation system [9, 41-43].

However, it remains as a challenge to estimate the HRE accurately for the air-side modulation in practice. The HRE highly depends on the supply condition and cooling load. Chen et al. [44] experimentally found that, for displacement ventilation, a higher supply airflow rate helped to improve the HRE. Huan et al. [21] experimentally revealed that the HRE of stratum ventilation increased with the increasing cooling load. Since the supply condition and cooling load can vary largely in practice, the HRE can also vary significantly, e.g., by 13% from around 1.28 to 1.45 reported by Huan et al. [21] for stratum ventilation. Although HRE can be estimated via experiments and CFD simulations, it is costly to produce comprehensive results of HRE with the largely varying supply condition and cooling load in practice.

Therefore, this study develops an HRE model as a function of the supply condition and cooling load. Following this section (Section 1), the HRE model is determined and validated with experimental data from two typical stratum-ventilated rooms (i.e., a medium-sized classroom with mid-level exits and a small-sized office with ceiling-level exit) (Sections 2 and 3). The applicability of the proposed HRE model is further analyzed by extrapolating the HRE model to wider ranges of the supply condition and cooling load beyond the model determination, and by extending the HRE model to two displacement ventilation systems (Section 4). Lastly, the application and effectiveness of the HRE model proposed for the air-side modulation are demonstrated to improve energy efficiency while maintaining thermal comfort (Sections 5 and 6). The HRE model based air-side modulation can be used for both the design and control of stratum ventilation and is also promising for the design and control of displacement ventilation.

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2. Methodology

2.1 Overview of methodology

HRE is defined as the ratio of the temperature difference between the exit air and supply air to the temperature difference between the room air and supply air (Equation 1). With the HRE, supply airflow rate, and supply and exit air temperatures, Equations 1 and 2 can be solved to obtain the room temperature for air-side modulation. This study mainly includes three parts (Figure 1). Firstly, The HRE model proposed (Equation 3) is determined and validated with experiments for two typical stratum-ventilated rooms. The stratum-ventilated classroom is medium-sized with mid-level exits, and the stratum-ventilated office is small-sized with ceiling-level exit. Although the room geometries and air terminal configurations can significantly affect the HRE [39, 41], the same HRE model form is shared by the two stratum-ventilated rooms (Equation 3). The HRE model proposed is an empirical model, which is in a function of the supply condition and cooling load with only three constant coefficients (Equation 3). The three constant coefficients are determined by experimental data using multiple regression. Actually, in the field of indoor built environment, there are many widely used empirical models, e.g., the PMV-PPD model [45, 46], the adaptive thermal comfort model [47], the model of the maximum velocity decay of impinging jet ventilation [48], the velocity decay model of air curtain ventilation [49], and the interface height model of underfloor air distribution [50]. Due to the complexity of indoor air distribution, these empirical models lack mathematical derivations [51-54]. Although these empirical models are obtained using the iterative improvement approach based on the observations of extensive experiments/simulations without mathematical derivations, they are powerful for the design and control of the indoor built environment. The HRE model (Equation 3) is also developed using an iterative improvement approach based on the observations of extensive experimental results. Secondly, the applicability of the HRE model is further proven by extrapolating it to the supply condition and cooling load broader than the experiments used for the HRE

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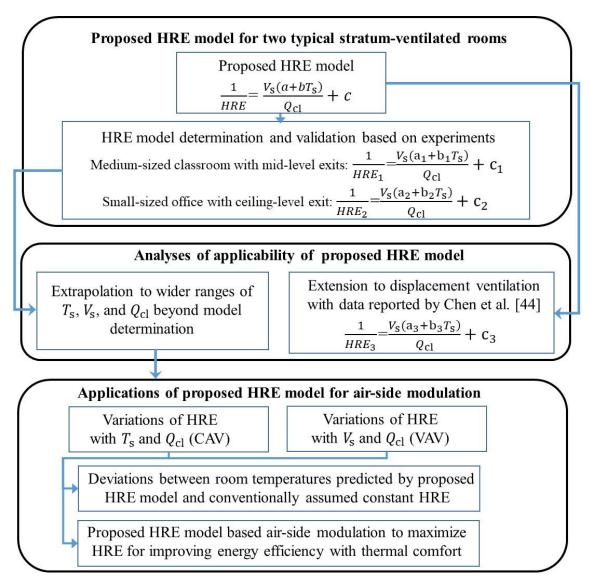
model determination. The applicability of the HRE model is also tested with displacement ventilation using the data reported by Chen et al. [44].

$$HRE = \frac{T_{\rm e} - T_{\rm s}}{T_{\rm r} - T_{\rm s}} \tag{1}$$

$$Q_{\rm cl} = \rho c_{\rm p} V_{\rm s} (T_{\rm e} - T_{\rm s}) \tag{2}$$

$$\frac{1}{HRE} = \frac{V_{\rm s}(a+bT_{\rm s})}{Q_{\rm cl}} + c \tag{3}$$

where *a*, *b* and *c* are the three constant coefficients of the HRE model; c_p is the specific heat capacity of air (kJ/(kg•⁰C)); *HRE* is the heat removal efficiency; ρ is the air density (kg/m³); Q_{cl} is the cooling load (kW); T_e , T_r and T_s are the temperatures of exit air, room air in the occupied zone and supply air respectively (⁰C); V_s is the supply airflow rate (m³/s).



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Note: T_s , V_s and Q_{cl} denote the supply air temperature, supply airflow rate and cooling load respectively; a, b, c are three constant coefficients of the heat removal efficiency (HRE) model; CAV and VAV denote the constant-air-volume system and variable-air-volume system respectively.

Fig.1. Overview of methodology.

Thirdly, the proposed HRE model is demonstrated to be used for the air-side modulation. Both the constant-air-volume and variable-air-volume systems are taken into consideration for the two typical stratum-ventilated rooms. Conventionally, since no HRE model is available, a constant HRE is simplifiedly assumed for the air-side modulation [25, 35, 37, 55]. The air-side modulation based on a constant HRE outperforms the network/multi-zone models which ignore the non-uniformity of the thermal environment [10]. The extent to which the HRE value varies with the supply condition and cooling load is investigated with the validated HRE model. A large variation of the HRE implies that the conventionally assumed constant HRE is inadequate for the air-side modulation. The room temperatures predicted by the proposed HRE model and by the conventionally assumed constant HRE are also compared. The larger deviation between the two room temperature predictions, the more deficient the conventionally assumed constant HRE for the air-side modulation for thermal comfort. Due to the deficiency of the conventionally assumed constant HRE, the proposed HRE model is essential for the air-side modulation for thermal comfort. It is noted that the room temperature predicted by the proposed HRE model is considered as credible, which will be validated by the experiments. Moreover, an air-side modulation method based on the HRE model is proposed to maximize the HRE for improving the energy efficiency while maintaining thermal comfort.

2.2 Experiments in medium-sized stratum-ventilated classroom with mid-level exits

The stratum-ventilated classroom with mid-level exits is located in City University of Hong Kong (Figure 2). The classroom is medium-sized with dimensions of 8.8 m (length) \times 6.1 m (width) \times 2.4 m (height). The air horizontally enters the breathing zone from four supply diffusers S1-S4 on the front wall at the height of 1.3 m, and then exits through four exit louvers E1-E4 on the rear wall at the same height. Perforation diffusers and double deflection grilles are used as the supply and exit air

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terminals respectively [19]. Two rows with eight seats in each are arranged for occupants (numbered 1 to 16). Sixteen thermal manikins represent students with dimensions around 400 mm (length) \times 250 mm (width) \times 1200 mm (height). Each thermal manikin is heated by a 100 W light bulb [13, 56]. Similar to Cheng et al. [18, 19], the heat generated by the radiators is adjusted to control the cooling load. The radiators are separated from the occupied zone by boards. Thus, the change in cooling load can be regarded to be caused by the outdoor weather condition [18, 19]. Eight sampling points at the height of 1.1 m (i.e., M1-M8) are evenly arranged for the room temperature measurements. Measurements at the height of 1.1 m (for seated occupants) are adequate for thermal comfort evaluation of stratum ventilation [18, 37]. SWEMA omnidirectional hot-wire anemometers with data logger are used with a measuring accuracy of $\pm 0.2^{\circ}$ C between 10° C and 40° C. Temperatures of the supply and exit air are measured at the air terminals. The supply airflow rate is measured at the supply diffusers by ALNOR balometer capture hood EBT731, with a measuring accuracy of $\pm 3\%$ of reading between 0.012 m³/s and 1.181 m³/s.

Fifteen cases (numbered 1 to 15 in Table 1) are designed for the aforementioned measurements, covering wide ranges of the supply air temperature (19.81°C to 29.44^oC), supply airflow rate (0.201 m³/s to 0.373 m³/s), cooling load (0.52 kW to 1.98 kW), exit air temperature (23.79°C to 31.95°C) and room temperature (23.23°C to 31.15°C). The supply air temperature and supply airflow rate are the mean and sum of the measurements at the four supply diffusers S1-S4 respectively. The exit air temperature is the mean of the measurements at the four exit louvers E1-E4. The room temperature is the mean of the measurements at the eight sampling points M1-M8. The cooling load is calculated by Equation 2. The 15 cases are randomly divided into two series (Series 1 and 2). Series 1 (Cases 1-7) is for the HRE model determination. Series 2 (Cases 8-15) is not involved in the model determination, but used for the model validation. The range of the supply air temperature in Series 1 is slightly broader than that in Series 2 and the range of the supply airflow rate in Series 1 is the same as that in Series 2. The supply air temperatures and supply airflow rates in Series 1 and 2 are the ones generally encountered in practice [19]. Thus, the HRE model validated is adequate for the air-side modulation in practice. The cooling load in Series 2 covers a wider range than that in Series 1, which will be used in Section

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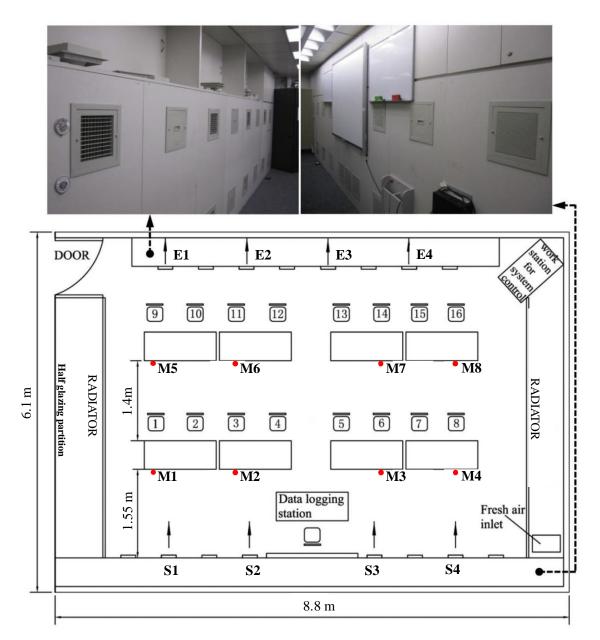
4.1 to show that the HRE model can be extrapolated to a wider range of the cooling load against the model determination.

| Cases | Cases | | $V_{\rm s}~({\rm m}^3/{\rm s})$ | $Q_{\rm cl}$ (kW) | $T_{\rm e}~(^{0}{\rm C})$ | $T_{\rm r}~(^{0}{\rm C})$ |
|-----------|-------|-------|---------------------------------|-------------------|---------------------------|---------------------------|
| | 1 | 19.81 | 0.272 | 1.30 | 23.79 | 23.23 |
| | 2 | 22.35 | 0.272 | 1.44 | 26.74 | 25.82 |
| | 3 | 23.03 | 0.201 | 1.73 | 30.2 | 28.52 |
| Series 1 | 4 | 23.25 | 0.373 | 1.09 | 25.68 | 25.16 |
| | 5 | 23.86 | 0.201 | 1.60 | 30.48 | 29.14 |
| | 6 | 26.90 | 0.201 | 0.96 | 30.89 | 29.79 |
| | 7 | 29.44 | 0.373 | 1.13 | 31.95 | 31.15 |
| | 8 | 21.87 | 0.373 | 1.44 | 25.07 | 24.58 |
| | 9 | 23.72 | 0.201 | 1.76 | 31.02 | 29.13 |
| | 10 | 22.24 | 0.272 | 1.89 | 28.01 | 26.8 |
| Garrian 2 | 11 | 23.03 | 0.201 | 1.73 | 30.2 | 28.52 |
| Series 2 | 12 | 24.99 | 0.272 | 1.79 | 30.45 | 29.17 |
| | 13 | 25.30 | 0.373 | 1.98 | 29.71 | 28.63 |
| | 14 | 26.32 | 0.373 | 1.87 | 30.48 | 29.55 |
| | 15 | 26.41 | 0.373 | 0.52 | 27.58 | 27.22 |

 Table 1. Experiment cases: Medium-sized stratum-ventilated classroom with mid-level exits.

Note: Series 1 is for the HRE model determination, and Series 2 is not involved in the

Applied Energy Volume 238, 15 March 2019, Pages 1237-1249 model determination but used for the model validation.



Note: *E* and *S* denote the exit louver and supply diffuser respectively at the height of 1.3m, and *M* denotes the sampling point at the height of 1.1 m.

Fig.2. Setup of medium-sized stratum-ventilated classroom with mid-level exits.

2.3 Experiment in small-sized stratum-ventilated office with ceiling-level exit

The small-sized stratum-ventilated office with ceiling-level exit is located in Xi'an Jiaotong University with dimensions of 3.8 m (length) \times 2.8 m (width) \times 2.6 m (height) (Figure 3). The office is designed for two occupants represented by two thermal manikins with dimensions of 400 mm (length) \times 250 mm (width) \times 1200 mm

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(height). The east wall is imbedded with the electric heating film to simulate the glass façade [21], and the other walls, ceiling and floor are insulated. The heat generated by the electric heating film is adjusted to control the cooling load. The room temperature is measured at the height of 1.1 m (for seated occupants). Detailed information on the experimental setup and measurements are reported in Huan et al. [21]. A total of 13 cases (numbered 16 to 28) are designed for the thermal comfort environment with the room temperature varying from 25.10°C to 27.29°C (Table 2). The supply air temperature runs between 17° C and 21° C, the supply airflow rate runs from 0.038 m³/s to 0.131 m³/s, the cooling load runs from 0.47 kW to 1.41 kW (Equation 2), and the exit air temperature runs from 26.20°C to 30.97°C. The 13 cases are also randomly divided into two series (Series 3 and 4). Series 3 (Cases 16-22) is for the HRE model determination. Series 4 (Cases 23-28) is not involved in the model determination, but used for the model validation.

| | | | | | 1 | |
|----------|----|-------------------------------|---------------------------------|------------------------|-------------------------------|----------------------------|
| Cases | | $T_{\rm s}~(^{\rm o}{\rm C})$ | $V_{\rm s}~({\rm m}^3/{\rm s})$ | $Q_{\rm cl}({\rm kW})$ | $T_{\rm e}~(^{\circ}{\rm C})$ | <i>T</i> _r (°C) |
| | 16 | 17 | 0.038 | 0.47 | 27.09 | 25.10 |
| | 17 | 17 | 0.078 | 1.29 | 30.64 | 26.17 |
| | 18 | 19 | 0.050 | 0.50 | 27.35 | 25.64 |
| Series 3 | 19 | 19 | 0.085 | 1.06 | 29.43 | 26.35 |
| | 20 | 21 | 0.044 | 0.27 | 26.20 | 25.22 |
| | 21 | 21 | 0.088 | 0.76 | 28.15 | 26.15 |
| | 22 | 21 | 0.131 | 1.41 | 29.97 | 27.29 |
| | 23 | 17 | 0.055 | 0.69 | 27.39 | 25.10 |
| G · 4 | 24 | 17 | 0.073 | 1.19 | 30.53 | 26.64 |
| Series 4 | 25 | 19 | 0.071 | 0.78 | 28.12 | 25.71 |
| | 26 | 19 | 0.115 | 1.66 | 30.97 | 27.27 |

 Table 2. Experiment cases: Small-sized stratum-ventilated office with ceiling-level exit.

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|--|--|----|----|-------|------|-------|-------|--|--|--|--|
| | | 27 | 21 | 0.069 | 0.54 | 27.48 | 25.89 | | | | |
| | | 28 | 17 | 0.065 | 0.96 | 29.21 | 26.27 | | | | |

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Note: Series 3 is for the HRE model determination, and Series 4 is not involved in the model determination but used for the model validation.

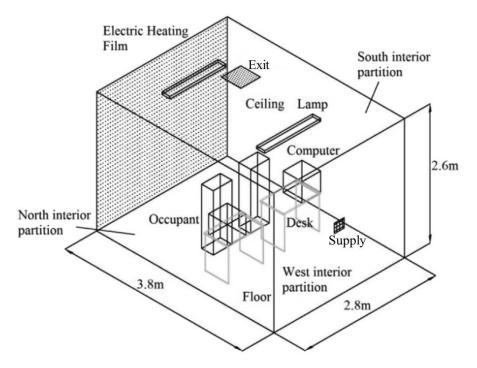


Fig.3. Setup of small-sized stratum-ventilated office with ceiling-level exit.

3. HRE model development for two typical stratum-ventilated rooms

3.1 HRE model determination and validation: Medium-sized classroom with mid-level exits

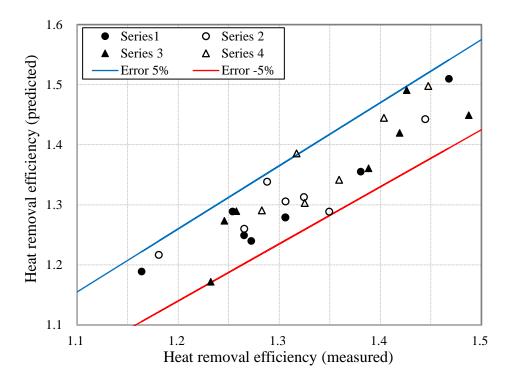
The three constant coefficients (i.e., a, b and c in Equation 3) for the HRE model of the medium-sized stratum-ventilated classroom with mid-level exits (Figure 2) are determined to be 1.737, -0.070 and 0.766 respectively (Equation 4), with the regression coefficient R^2 of 0.99. Figure 4 shows the HREs predicted by Equation 4 agree reasonably well with the measurements. The errors of the predicted HREs for both Series 1 and 2 are within $\pm 5\%$. The errors refer to the relative differences between the predicted and measured HREs. The mean absolute error of Series 1 is 2.21%, and that of Series 2 is 1.95%. The mean absolute error refers to the mean of the absolute values of errors [57]. Thus, the HRE model for this stratum-ventilated

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room is accurate.

$$\frac{1}{HRE_1} = \frac{V_{\rm s}(1.737 - 0.070T_{\rm s})}{Q_{\rm cl}} + 0.766 \tag{4}$$

where HRE_1 is the HRE model for the medium-sized stratum-ventilated classroom with mid-level exits.



Note: Series 1 and 2 (Table 1) refer to the stratum-ventilated classroom (Figure 2); Series 3 and 4 (Table 2) refer to the stratum-ventilated office (Figure 3). Error ($\pm 5\%$) indicates the relative difference between the predicted and measured values.

Fig.4. Comparisons between measured and predicted heat removal efficiencies of two typical stratum-ventilated rooms.

3.2 HRE model determination and validation: Small-sized office with ceiling-level exit

The three constant coefficients of *a*, *b* and *c* in Equation 3 for the HRE model of the small-sized stratum-ventilated office with ceiling-level exit (Figure 3) are determined to be 11.787, -0.432 and 0.419 respectively (Equation 5), with the regression coefficient R^2 of 0.93. The errors of the HREs predicted by Equation 5 for both Series 3 and 4 are within $\pm 5\%$ (Figure 4). The mean absolute error of Series 3 is 2.7%, and that of Series 4 is 2.5%. Thus, the HRE model for this stratum-ventilated room is also accurate.

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$$\frac{1}{HRE_2} = \frac{V_{\rm s}(11.787 - 0.432T_{\rm s})}{Q_{\rm cl}} + 0.419\tag{5}$$

where HRE_2 is the HRE model for the small-sized stratum-ventilated office with ceiling-level exit.

4. Analyses of applicability of proposed HRE model

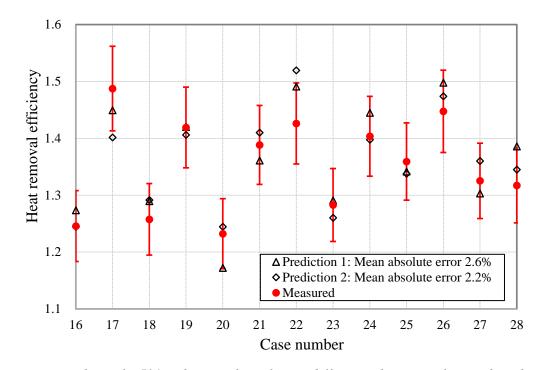
4.1 Extrapolation to wider ranges of supply condition and cooling load

The HRE model is extrapolated to wider ranges of the supply condition and cooling load to further test its applicability. For the cooling load, it is shown in Table 1 that the cases for the model validation which are not involved in the model determination (Series 2) cover a much wider range of the cooling load (i.e., 0.52kW to 1.98kW) than that of the cases for the model determination (Series 1) (i.e., 0.96kW to 1.73kW). The HREs of the cases for the model validation (Series 2) could be accurately predicted by the proposed HRE model (Equation 4) with errors within $\pm 5\%$ and a mean absolute error of 1.95% (Section 3.1). Thus, the HRE model determined within a specific range of the cooling load can be extrapolated to a wider range of the cooling load.

For the supply condition, Cases 16-19, 23-25 and 28 (Table 2) are used to re-determine the HRE model. Cases 16-19, 23-25 and 28 cover a narrower range of the supply air temperature (i.e., 17° C to 19° C) and supply airflow rate (i.e., $0.038 \text{ m}^3/\text{s}$ to $0.085 \text{ m}^3/\text{s}$). When using the re-determined model for predicting the HREs of Cases 16-28 covering a wider range of the supply air temperature from 17° C to 21° C and supply airflow rate from $0.038 \text{m}^3/\text{s}$ to $0.131 \text{m}^3/\text{s}$, the errors are within $\pm 5\%$ except for Cases 17 and 22 (Figure 5). The errors of Case 17 and 22 are within $\pm 5.8\%$ and $\pm 6.5\%$ respectively which are also acceptable in practice. The mean absolute error for Cases 16-28 of the re-determined HRE model is 2.2%, which is similar to that of the original HRE model (i.e., 2.6%). The original HRE model is determined by cases (Series 3 in Table 2) covering a wider range of the supply air temperature (i.e., 17° C to 21° C) and supply airflow rate (i.e., $0.038 \text{ m}^3/\text{s}$ to $0.131 \text{ m}^3/\text{s}$). Thus, the proposed HRE model determined by a narrower range of the supply condition have

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similar accuracy. This implies that the proposed HRE model determined by a certain range of the supply condition could be extrapolated to a wider range of the supply condition.



Note: Error bar of $\pm 5\%$ indicates the relative difference between the predicted and measured values is within $\pm 5\%$; cases for the model determination of Prediction 1 cover a wider range of the supply condition (Series 3 in Table 2); cases for the model determination of Prediction 2 cover a narrower range of the supply condition (Cases 16-19, 23-25 and 28 in Table 2).

Fig.5. Comparisons between measured and predicted heat removal efficiencies of small-sized stratum-ventilated office with ceiling-level exit.

4.2 Extension to displacement ventilation

Two displacement ventilation systems in Delft University of Technology are considered with the room dimensions of 5.6 m (length) \times 3.0 m (width) \times 3.2 m (height) (Figure 6) [44]. The supply and exit air terminals are on the same side for System 1, and on the opposite sides for System 2. On the other hand, the heat source is placed on the opposite side to the supply air terminal for System 1, and on the same side for System 2. The heat source is located on the window to simulate the solar radiation. Ten cases (numbered 29 to 38 in Table 3) are extracted from the

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experiments and CFD simulations of Chen et al. [44]. The supply air temperature runs from 16.0° C to 20.8° C, the supply airflow rate runs from $0.04 \text{ m}^3/\text{s}$ to $0.10 \text{ m}^3/\text{s}$, the cooling load runs from 0.50 kW to 0.94 kW (Equation 2), the exit air temperature runs from 24.8° C to 27.1° C, and the room temperature is maintained around 23.5° C (between 22.9° C and 23.8° C). The room temperature is measured at the height of 1.6m (for standing occupants). Cases 29-36 are for System 1 and the remaining two cases are for System 2. More information about the experiments and CFD simulations could be found in Chen et al. [44]. The 10 cases are divided into two series (Series 5 and 6). Series 5 (Cases 29-34) is used for the HRE model determination. Series 6 (Cases 35-38) is not involved in the model determination, but used for the model validation.

| Cases | 8 | System | Data source | T_{s} (⁰ C) | $\frac{V_{\rm s}}{({\rm m}^3/{\rm s})}$ | Q _{cl} (kW) | T_{e} (⁰ C) | <i>T</i> _r (⁰ C) |
|----------|----|--------|----------------|---------------------------|---|-------------------------|---------------------------|--|
| | 29 | 1 | Exp | 16.0 | 0.04 | 0.52 | 25.6 | 23.8 |
| | 30 | 1 | Exp | 19.7 | 0.07 | 0.48 | 25.0 | 23.2 |
| Series 5 | 31 | 1 | Exp | 20.8 | 0.10 | 0.50 | 24.8 | 22.9 |
| Series 5 | 32 | 1 | Exp | 19.6 | 0.10 | 0.94 | 27.1 | 23.8 |
| | 33 | 1 | CFD | 16.0 | 0.04 | 0.53 | 25.8 | 23.5 |
| | 34 | 1 | CFD | 19.1 | 0.07 | 0.53 | 25.0 | 23.4 |
| | 35 | 1 | CFD | 20.7 | 0.10 | 0.53 | 24.9 | 23.4 |
| Series (| 36 | 1 | CFD | 19.4 | 0.10 | 0.94 | 26.9 | 23.7 |
| Series 6 | 37 | 2 | Exp | 19.3 | 0.07 | 0.51 | 25.0 | 23.2 |
| | 38 | 2 | CFD | 18.7 | 0.07 | 0.55 | 24.8 | 23.2 |

Table 3. Experiment and simulation cases: Displacement ventilation [44].

Note: Exp denotes experiment; Series 5 is for the HRE model determination, and Series 6 is not involved in the model determination but used for the model validation.

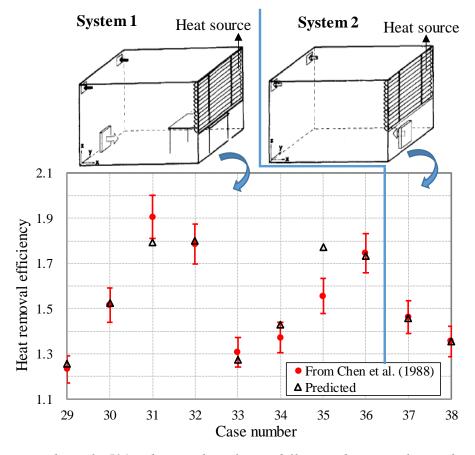
The three constant coefficients of *a*, *b* and *c* (Equation 3) for the HRE model of System 1 are determined as 21.533, -0.970 and 0.276 respectively, with the regression coefficient R^2 of 0.82 (Equation 6). Figure 6 shows the predicted HREs by Equation

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6 agree reasonably well with the results reported by Chen et al. [44]. The errors of the predicted HREs for cases of System 1 (Cases 29-36) are within \pm 5%, except Cases 31 and 35. The errors of Cases 31 and 35 are 6.2% and 13.7% respectively. The large error of Case 35 is caused by the small difference between the supply air temperature and room temperature (2.7°C in Table 3). With such a small difference between the supply air temperature and room temperature, a variation of 0.33°C in the room temperature can result in a variation of 13.7% in the HRE (Equation 1). Thus, the error is also common and acceptable for engineering applications. The mean absolute error of the predicted HREs for System 1 is 3.8%. Thus, the proposed HRE model is accurate for System 1.

$$\frac{1}{HRE_3} = \frac{V_{\rm s}(21.533 - 0.970T_{\rm s})}{Q_{\rm cl}} + 0.276 \tag{6}$$

where HRE_3 is the HRE model for System 1 of displacement ventilation.



Note: Error bar of $\pm 5\%$ indicates the relative difference between the predicted value and data reported by Chen et al. [44] is within $\pm 5\%$.

Fig.6. Comparisons between heat removal efficiencies of two displacement

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ventilation systems predicted by HRE model and reported by Chen et al. [44].

The proposed HRE model of System 1 (Equation 6) is also tested for System 2 (Cases 37 and 38). The predicted HREs are in fairly good agreement with the data given by Chen at al. [44] with errors within $\pm 1\%$ (Figure 6). Although the configurations of the air terminals and heat sources are important in airflow computations, the same HRE model with the same constant coefficients is shared by the two different displacement ventilation systems. This might be attributed to the similar airflow pattern of Systems 1 and 2, which is consistent with the results of Chen at al. [44] and Lin et al. [58]. Summarily, the above analyses imply that the proposed HRE model is applicable to displacement ventilation. More experimental data can be found in the literature to support the proposed HRE model (Equation 3), e.g., the experiments on displacement ventilation with floor heating in Technical University of Denmark [27]. However, considering the lengthy, no more repeated validations on the HRE model (Equation 3) are presented in this paper.

As a summary, for a given room with specific room geometries and air terminal configurations, the proposed HRE model can be determined as the function of the supply air temperature, supply airflow rate and cooling load by quantifying the three constant coefficients in Equation 3. The determined HRE is promising for a wider range of the supply air temperature, supply airflow rate and cooling load against the model determination. For substantially different rooms, the three constant coefficients are recommended to be re-determined (e.g., Figures 2 and 3). The HRE models of two typical stratum-ventilated rooms and two displacement-ventilated rooms have been determined (Equations 4-6). The HRE models for more stratum-ventilated and displacement-ventilated rooms generally encountered in practice, e.g., stratum ventilation with the supply and exit air terminals on the same wall [60, 61], should be prepared to form the database of HRE models in future studies. For different stratum-ventilated/displacement-ventilated rooms in practice, the corresponding HRE models can be selected from the database and used for the air-side modulation. The air-side modulation using the HRE model is illustrated in the following two sections.

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5. Applications of HRE to air-side modulation for thermal comfort

The modified PMV (Equation 7) can be used for the thermal comfort evaluation of stratum ventilation [37], which is explained as follows. For occupants with typical summer clothing and sedentary activity, the PMV given by ASHRAE 55-2017 [45] is expressed to be the function of the room temperature and air velocity using multiple regression analysis. The mean radiant temperature is assumed to be the same as the room temperature [18, 45] and the relative humidity is assumed to be 58.5%. Chow et al. [62] experimentally confirmed that when the relative humidity was between 50% and 80%, the variation of the relative humidity imposed insignificant effects on thermal comfort. The air velocity is further correlated to the room temperature and supply airflow rate by multiple regression analysis. By replacing the air velocity in the PMV with the room temperature and supply airflow rate, the PMV model is modified to be the function of the room temperature and supply airflow rate. Equation 7 has been experimentally validated to be applicable to the two stratum-ventilated rooms (Figures 2 and 3) [37]. More details about the modified PMV can be found in Zhang et al. [37]. The supply airflow rate could be readily read from the building management system, while the room temperature for collective air distributions with a non-uniform thermal environment is difficult to predict (Section 1). In other words, to modulate the air-side for thermal comfort, the room temperature prediction is the core issue. Thus, the room temperature prediction for thermal comfort is the focus of this section.

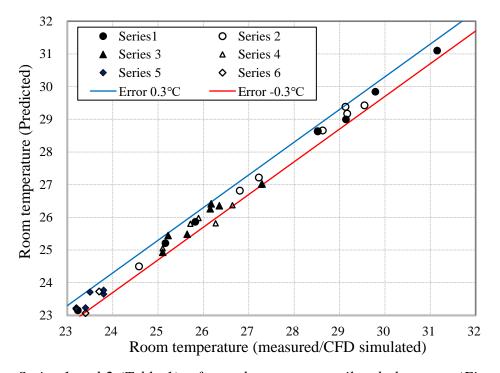
$$PMV = -\frac{7}{91300}NT_{\rm r}^2 + \frac{19}{50}T_{\rm r} - \frac{689}{74}$$
(7)

where PMV is the Predicted Mean Vote; N is the supply airflow rate in term of air changes per hour (ACH).

Figure 7 compares the room temperatures predicted by the HRE model proposed with the experiments and CFD simulations for the two typical stratum-ventilated rooms and two displacement ventilation systems (Tables 1-3). The HRE model predicts the room temperature by solving equations 1, 2 and 4/5/6 with the inputs of the supply condition and exit air temperature (Tables 1, 2 and 3). A wide range of the room temperature is covered, running from around 23^oC to 31^oC. The errors of the room temperature prediction are generally within $\pm 0.3^{\circ}$ C except Cases 28 and 35. The

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errors for Cases 28 and 35 is -0.45°C and -0.33°C respectively. The mean absolute error of all the predicted room temperatures is 0.12°C, which meets the requirements for thermal comfort evaluation [63]. The good agreement of the predicted room temperatures with the experiments and CFD simulations can be explained by the accuracy of the HRE model proposed (Sections 3 and 4). Therefore, in the following investigations on the air-side modulation, the HREs and room temperatures predicted by the HRE model are regarded as accurate.



Note: Series 1 and 2 (Table 1) refer to the stratum-ventilated classroom (Figure 2); Series 3 and 4 (Table 2) refer to the stratum-ventilated office (Figure 3); Series 5 and 6 (Table 3) refer to the two displacement ventilation systems (Figure 6); error $(\pm 0.3^{\circ}C)$ indicates the difference between the HRE-model-predicted and measured/CFD simulated values.

Fig.7. Comparisons of HRE-model-predicted and measured/CFD simulated room temperatures.

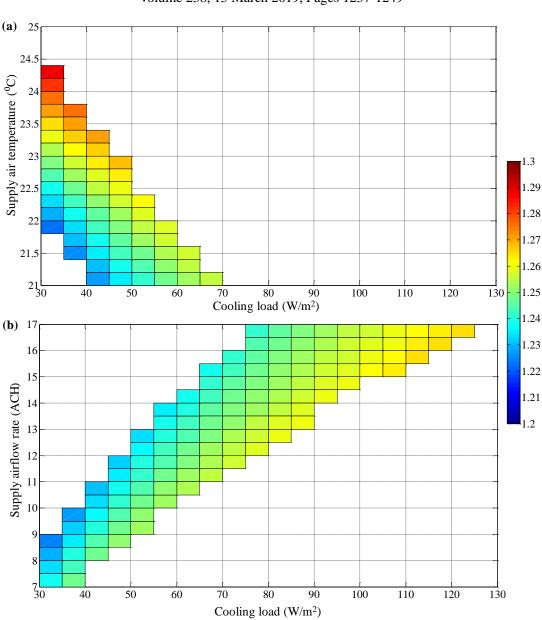
The following investigations on the air-side modulation for the two typical stratum-ventilated rooms cover a wide range of the supply condition and cooling load. The cooling load runs from 30 W/m² to 130 W/m² [21]. To minimize draft risk, the supply air temperature is between 21° C and 25° C for the constant-air-volume system, and the supply airflow rate is from 7 ACH to 15 ACH for the variable-air-volume

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system [19]. PMV (Equation 7) is restricted within ± 0.5 for thermal comfort [18, 37, 45].

5.1 Room temperature modulation: Medium-sized classroom with mid-level exits

Figure 8 shows variations of the HRE with supply conditions and cooling loads of the medium-sized stratum-ventilated classroom with mid-level exits. The HRE outside the thermally workable zone is excluded. With a low supply air temperature and small cooling load, PMV would be lower than -0.5; and on the contrary, PMV would be higher than 0.5, which is outside the thermally workable zone of the constant-air-volume system. Similarly, with a high supply airflow rate and small cooling load, PMV would be lower than -0.5; and on the contrary, PMV would be higher than 0.5, which is outside the thermally workable zone of the variable-air-volume system. With a supply airflow rate setting of 11 ACH [19], the constant-air-volume system can serve a cooling load running from 30 W/m^2 to 70 W/m^2 . With a supply air temperature setting of 21^oC [19], the variable-air-volume system can serve a cooling load ranging from 30 W/m^2 to 125 W/m^2 . It is noted that the specific range of the cooling load which the constant-air-volume system and variable-air-volume system can serve is affected by the supply airflow rate setting and supply air temperature setting respectively (Equation 7). The constant-air-volume system serves a narrower range of the cooling load than the variable-air-volume system because PMV is more sensitive to the supply air temperature than to the supply airflow rate (Equation 7) [64]. For the constant-air-volume system, the HRE increases from around 1.22 to 1.31 with the increasing cooling load and supply air temperature. For the variable-air-volume system, the HRE increases from around 1.22 to 1.27 with the increasing cooling load and decreasing supply airflow rate. Thus, the variations of the HRE for both the two systems are small, which indicates that a properly assumed constant HRE is adequate for the air-side modulation of the room temperature for thermal comfort.



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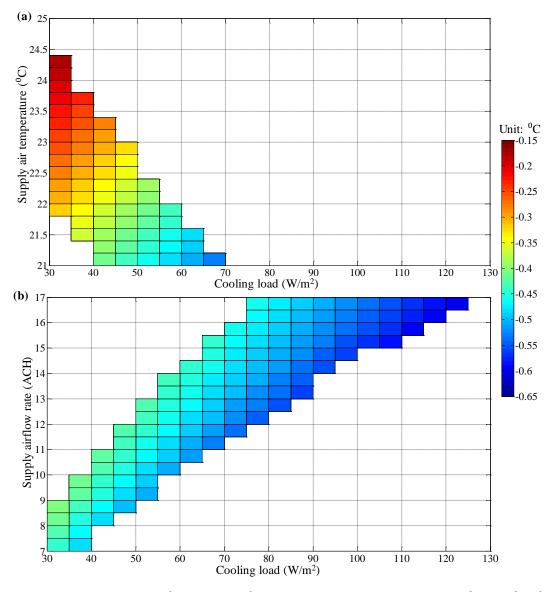
Note: HRE is calculated by the validated HRE model (Equation 4).

Fig.8. Variations of heat removal efficiencies with supply conditions and cooling loads of medium-sized stratum-ventilated classroom with mid-level exits: (a) Constant-air-volume system; and (b) variable-air-volume system.

With the conventionally used constant HRE, i.e., 1.38 [25, 35-37], the error of the room temperature prediction runs from around -0.55° C to -0.14° C and from around -0.62° C to -0.39° C for the constant-air-volume and variable-air-volume systems respectively (Figure 9). The error of the room temperature prediction is calculated as the room temperature deviation between the predictions by the conventionally used constant HRE and the proposed HRE model (Equation 4). The larger error range of

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the room temperature for the constant-air-volume system is caused by the larger variation of the HRE when compared with that for the variable-air-volume system. On the other hand, it is seen that by properly assuming the value of the constant HRE, the error of the room temperature prediction could be maintained within $\pm 0.25^{\circ}$ C and $\pm 0.15^{\circ}$ C for the constant-air-volume and variable-air-volume systems respectively which are acceptable in practice for thermal comfort. However, with different designs of these two systems (i.e., the supply airflow rate setting for the constant-air-volume system), the proper constant HRE can be substantially different (Figure 4). The proper constant HRE can be proposed HRE model.



Note: Room temperature deviation is the error in room temperature prediction by the

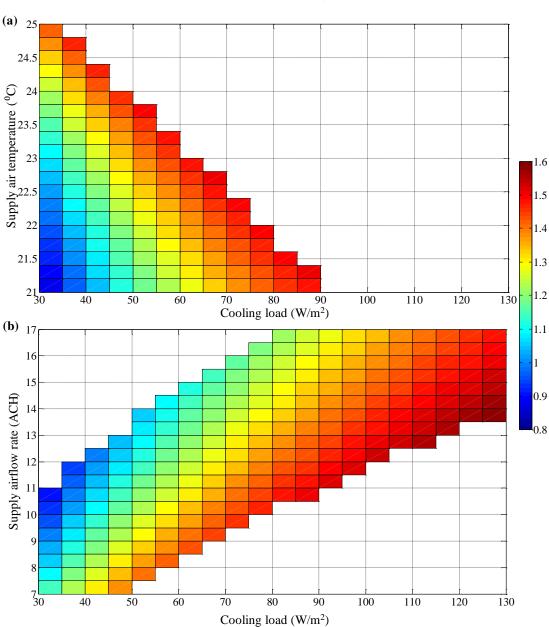
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conventionally assumed constant HRE of 1.38.

Fig.9. Variations of room temperature deviations with supply conditions and cooling loads of medium-sized stratum-ventilated classroom with mid-level exits: (a) Constant-air-volume system; and (b) variable-air-volume system.

5.2 Room temperature modulation: Small-sized office with ceiling-level exit

Figure 10 shows variations of the HRE with supply conditions and cooling loads of the small-sized stratum-ventilated office with ceiling-level exit. With a supply airflow rate setting of 11 ACH [19], the constant-air-volume system can serve a cooling load running from 30 W/m² to 90 W/m². With a supply air temperature setting of 21^{0} C [19], the variable-air-volume system can serve all considered cooling loads (30 W/m² to 130 W/m²). For the constant-air-volume system, the HRE increases from around 0.88 to 1.58 with the increasing cooling load and supply air temperature. For the variable-air-volume system, the HRE increases from around 0.88 to 1.60 with the increasing cooling load and decreasing supply airflow rate. Thus, the variations of the HRE for both the two systems are large, which indicates that an assumed constant HRE would lead to a poor air-side modulation of room temperature for thermal comfort.



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Note: HRE is calculated by the validated HRE model (Equation 5).

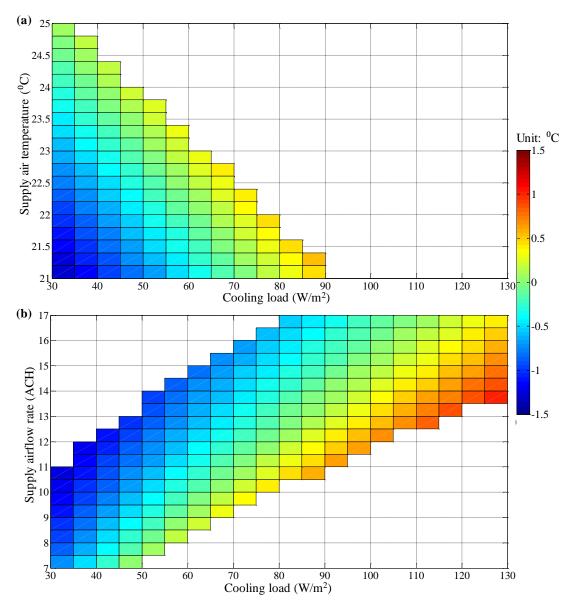
Fig.10. Variations of heat removal efficiencies with supply conditions and cooling loads of small-sized stratum-ventilated office with ceiling-level exit: (a) Constant-air-volume system; and (b) variable-air-volume system.

With the conventionally used constant HRE of 1.38 [25, 35-37], the error of the room temperature prediction runs from -1.30° C to 0.78° C and from -1.30° C to 1.13° C for the constant-air-volume system and variable-air-volume system respectively (Figure 11). The error of the room temperature prediction is calculated as the room temperature deviation between the predictions by the conventionally used constant

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HRE and the proposed HRE model (Equation 5). The larger error range of the room temperature prediction by the conventionally used constant HRE for the variable-air-volume system can be explained by the larger variation of the HRE when compared with the constant-air-volume system. It is seen that by properly assuming the value of the constant HRE, the error of the room temperature prediction could be maintained within $\pm 1.1^{\circ}$ C and $\pm 1.3^{\circ}$ C for the constant-air-volume system and variable-air-volume system respectively. An error in the room temperature prediction of $\pm 1.1^{\circ}$ C can result in an unacceptable error in the prediction of PMV (Equation 7), which reveals the deficiency of a constant HRE for the air-side modulation of room temperature for thermal comfort. Thus, in practice, the HRE model proposed is needed for the air-side modulation of room temperature for thermal comfort.

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Note: Room temperature deviation is the error in room temperature prediction by the conventionally used constant HRE of 1.38.

Fig.11. Variations of room temperature deviations with supply conditions and cooling loads of small-sized stratum-ventilated office with ceiling-level exit: (a) Constant-air-volume system; and (b) variable-air-volume system.

Compared with the medium-sized stratum-ventilated classroom with mid-level exits, the HRE variation range of the small-sized stratum-ventilated office with ceiling-level exit is much wider, which may be caused by the differences in airflow pattern stability due to the different exit air terminal layouts and/or room geometries. It is mainly caused by the different exit air terminal layouts. For the stratum-ventilated classroom, the exit louvers are located on the wall at the height of 1.3 m, while the exit of the

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stratum-ventilated office is located on the ceiling. Due to the thermal buoyancy effect, the exit air temperature of the stratum-ventilated office is significantly different from the room temperature (at the height of 1.1 m), which leads to the large variation of the HRE. While for the stratum-ventilated classroom, because the exit louvers are close to the height of 1.1 m in the occupied zone, the thermal buoyancy effect on the exit air temperature is small and the exit air temperature is close to the room temperature. Thus, the variation of the HRE of the stratum-ventilated classroom is small. Summarily, the above results demonstrate the importance and effectiveness of the proposed HRE model in the air-side modulation for thermal comfort.

6. Applications of HRE to air-side modulation for improving energy efficiency while maintaining thermal comfort

The proposed HRE model based air-side modulation can be used to improve the energy efficiency of the air conditioning system by maximizing the HRE while maintaining thermal comfort [10, 39, 40]. A larger HRE indicates a higher energy efficiency [10, 39, 40]. Thus, maximizing the HRE is a convenient and straightforward method for improving the energy efficiency of the air conditioning system [18, 41-43], which is particularly useful when the detailed information of the energy consumption of the air conditioning system is not available.

The potential for energy efficiency improvement of the proposed HRE model based air-side modulation can be demonstrated by the maximal HRE difference for the same cooling load. The maximal HRE difference is defined as the difference between the maximal and minimal HREs for the same cooling load (Equation 8). The maximal value of HRE for a particular cooling load is the HRE value that can be achieved by the proposed HRE model based air-side modulation. The minimal value of the HRE for that particular cooling load is the worst HRE value that can be encountered in practice. Thus, a larger maximal HRE difference of the same cooling load indicates a larger energy efficiency improvement potential by the proposed HRE model based air-side modulation. For example, as shown in Figure 10(a), when the cooling load is 60 W/m^2 , the proposed HRE model based air-side modulation determines the supply air temperature to be 23.4°C to achieve the maximal HRE of 1.56. Without the modulation, the supply air temperature might be determined as 21°C with the minimal

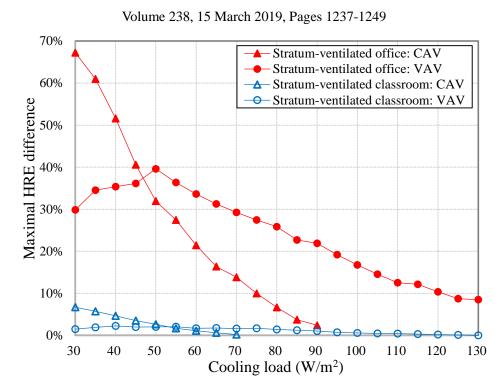
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HRE of 1.28. Thus the corresponding maximal HRE difference is 21.9%. It is noted that the maximal HRE difference for the same cooling load is calculated while thermal comfort is maintained. For thermal comfort, PMV is limited to ± 0.5 in the following analyses and the supply air temperature is constrained to be not less than 21° C to minimize draft risk [19].

$$Maximal \ HRE \ difference = \frac{HRE_{max} - HRE_{min}}{HRE_{min}}$$
(8)

where HRE_{max} and HRE_{min} are the maximal and minimal HREs for the same cooling load respectively.

For the stratum-ventilated office (Figure 3), the maximal HRE difference for the same cooling load with the constant-air-volume system (calculated from Figure 10a) varies between 2.4% and 67.3% (Figure 12) when the cooling load varies from 30 W/m^2 to 90 W/m^2 . The maximal HRE difference for the same cooling load of the variable-air-volume system (calculated from Figure 10b) varies from 8.5% to 39.6% when the cooling load varies between 30 W/m^2 and 130 W/m^2 . The maximal HRE difference for the cooling load larger than 90 W/m^2 of the constant-air-volume system does not exist, because the constant-air-volume system cannot provide thermal comfort (Figure 10a). For the constant-air-volume system, the maximal HRE difference for the same cooling load decreases with the increasing cooling load. This is because that the options of the supply air temperature meeting the requirement of thermal comfort decrease with the increasing cooling load (Figure 10a). For the variable-air-volume system, the maximal HRE difference for the same cooling load increases first and then decreases with the increasing cooling load. This is because when the cooling load is extremely low or high, fewer options of the supply airflow rate can satisfy the requirement of thermal comfort (Figure 10b). With the maximal HRE difference of the same cooling load for the constant-air-volume system and variable-air-volume system up to 67.3% and 39.6% respectively, the proposed HRE model based air-side modulation is effective in energy saving while maintaining thermal comfort for this stratum-ventilated office.



Note: A larger maximal HRE difference (Equation 8) indicates a larger energy saving potential by the proposed HRE model based air-side modulation.

Fig.12. Variations of maximal HRE difference with cooling loads of two typical stratum-ventilated rooms.

With regards to the stratum-ventilated classroom (Figure 2), the maximal HRE difference of the same cooling load for the constant-air-volume system runs from 0.2% to 6.7% (calculated from Figure 8a) when the cooling load varies from 30 W/m² to 70 W/m² (Figure 12). The maximal HRE difference of the same cooling load for the variable-air-volume system runs from 0.1% to 2.2% (calculated from Figure 8b) when the cooling load varies from 30 W/m² to 125 W/m² (Figure 12). The maximal HRE difference of the same cooling load for this stratum-ventilated classroom is smaller than that of the stratum-ventilated office. This is because the variation of the HRE for the stratum-ventilated classroom is smaller (Figures 8 and 10). The smaller maximal HRE difference of the same cooling load indicates the smaller energy efficiency improvement. Thus, the larger the variation of the HRE with the supply air temperature, supply airflow rate and cooling load, the more necessary the HRE model for the air-side modulation for energy saving and thermal comfort. Since the proposed HRE model based air-side modulation is convenient to employ in practice (Section 1), it is also recommended for the stratum-ventilated classroom for energy saving while

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maintaining thermal comfort.

The HRE model based air-side modulation can be used for both design and operation phases. When designing the supply air temperature of the variable-air-volume system or the supply airflow rate of the constant-air-volume system, with the given cooling load (i.e., the designed cooling load) [65, 66], HREs with all possible combinations of the supply air temperatures (e.g., from 21° C to 25° C) and supply airflow rates (e.g., from 7 ACH to 15 ACH) are calculated using the HRE model (Equation 3) and compared when confining the room temperature within the desired range for thermal comfort (Equation 7). The room temperature can be obtained by solving Equations 1-3. By identifying the maximal HRE from all the calculated HREs, the supply air temperature or the supply airflow rate associated with the maximal HRE are determined as the designed supply air temperature of the variable-air-volume system or the designed supply airflow rate of the constant-air-volume system respectively. During the operation phase, the supply airflow rate, and supply and exit air temperatures are monitored by the building management system. With the monitored data, the room temperature is predicted by solving Equations 1-3. Then, PMV is calculated using the monitored supply airflow rate and predicted room temperature (Equation 7). If the calculated PMV indicates thermal comfort, the supply condition (i.e., the supply air temperature of the constant-air-volume system or the supply airflow rate of the variable-air-volume system) is kept invariable. Otherwise, the supply condition needs to be updated. When updating the supply condition, the cooling load is assumed to be the same as that before the updating (Equation 2) [67], and the HREs with all possible supply air temperatures or supply airflow rates are calculated. The supply air temperature or the supply airflow rate leading to the maximal HRE while maintaining thermal comfort is determined to be the updated supply condition for the constant-air-volume system or the variable-air-volume system respectively.

It is noted that since the HRE model is derived from the experiments under steady states. The air-side modulation of the design phase and the supervisory control in the operation is generally based on hourly data, where the steady-state assumption is acceptable [38, 68]. The supervisory control has been widely implemented for the

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operation optimization of the air conditioning system [68]. Thus, the HRE model based air-side modulation is applicable to both the design phase and the supervisory control of operation phase. The applicability of the HRE model based air-side modulation for dynamic processes needs to be further investigated. Section 4.2 confirms that the HRE model is also applicable to displacement ventilation, thus the proposed HRE model based air-side modulation is also promising for displacement ventilation. Since stratum ventilation and displacement ventilation can be used in offices, classrooms and retail shops and have the potential to be applied in telecommunication sites and data centers etc. [25, 69-73], this study contributes to the proper air-side modulation of these buildings for the maximal energy efficiency with the desired room temperature.

7. Conclusions

An HRE model is proposed as a function of the supply condition (i.e., supply air temperature and supply airflow rate) and cooling load. The HRE model determines its three constant coefficients by means of experiments/CFD simulations through multiple regression. The model can be extrapolated to wider ranges of the supply condition and cooling load than those used for the model determination. Six series of experiments (thirty-three cases) and CFD simulations (five cases) demonstrate that the proposed HRE model is accurate for stratum ventilation and displacement ventilation with different room geometries and air terminal configurations, with errors generally within $\pm 5\%$ and mean absolute errors less than 4%.

The applications of the HRE model to the air-side modulation for the two stratum-ventilated rooms have been investigated. The results show that the variable-air-volume system can serve a wider range of the cooling load than the constant-air-volume system. The conventionally used constant HRE is deficient in the room temperature prediction with an error up to $\pm 1.3^{\circ}$ C. The HRE model proposed for the air-side modulation of room temperature could improve thermal comfort. Moreover, the proposed HRE model based air-side modulation can improve the energy efficiency up to 67.3% while maintaining thermal comfort.

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