

One-Dimensional vs. Two-Dimensional based Features: Plant Identification Approach

Alaa Tharwat^{a,b}, Tarek Gaber^{b,c,1,*}, Aboul Ella Hassanien^{b,d}

^a*Faculty of Engineering, Suez Canal University, Egypt*

^b*Scientific Research Group in Egypt (SRGE), <http://www.egyptscience.net>*

^c*Faculty of Computers and Informatics, Suez Canal University, Ismailia, Egypt*

^d*Faculty of Computers and Information, Cairo University, Egypt*

Abstract

1 The number of endangered species has been increased due to shifts in the agri-
2 cultural production, climate change, and poor urban planning. This lead to
3 investigating new methods to address the problem of plant species identifi-
4 cation/classification. In this paper, a plant identification approach using 2D
5 digital leaves images was proposed. The approach used two features extrac-
6 tion methods based on one-dimensional (1D) and two-dimensional (2D) and the
7 Bagging classifier. For the 1D-based methods, Principal Component Analysis
8 (PCA), Direct Linear Discriminant Analysis (DLDA), and PCA+LDA tech-
9 niques were applied, while 2DPCA and 2DLDA algorithms were used for the
10 2D-based method. To classify the extracted features in both methods, the Bag-
11 ging classifier, with the decision tree as a weak learner was used. The five
12 variants, i.e. PCA, PCA+LDA, DLDA, 2DPCA, and 2DLDA, of the approach
13 were tested using the Flavia public dataset which consists of 1907 colored leaves
14 images. The accuracy of these variants was evaluated and the results showed
15 that the 2DPCA and 2DLDA methods were much better than using the PCA,
16 PCA+LDA, and DLDA. Furthermore, it was found that the 2DLDA method
17 was the best one and the increase of the weak learners of the Bagging classifier
18 yielded a better classification accuracy. Also, a comparison with the most re-
19 lated work showed that our approach achieved better accuracy under the same
20 dataset and same experimental setup.

Keywords: Plant Identification, Principal Component Analysis, Linear

Discriminant Analysis (LDA), Bagging classifier, weak learners, 2DLDA,
2DPCA, Direct-LDA, Leaf Image, Leaves Images, Small Sample Size (SSS),
PCA+LDA

21 **1. Introduction**

22 Plants are a vital element of the Earth's ecology system. They maintain a
23 healthy breathable atmosphere. Almost the entire oxygen, needed for humans
24 and other animals breathe, are produced by plants, thus without plants, there
25 is no life on the earth (Gaber et al., 2015; Chaki et al., 2016). In addition,
26 plants can be used as an alternative energy source, e.g., bio-fuel (Chaki and
27 Parekh, 2012). There are various species of plants which are subject to the
28 danger of extinction. Saving endangered species of these plants from becoming
29 extinct and protecting their wild places is important for our health and the
30 future of our children. The impact of biodiversity loss may lead to fewer new
31 medicines, greater vulnerability to natural disasters and greater effects from
32 global warming. Therefore, there is a need for protecting plants and classifying
33 them into different species. For this purpose, plant identification techniques
34 have become a hot area of research.

35 Traditional plant identification can be achieved by a manual matching of
36 the plant's characteristics including leaves, fruits, flowers, and stem, against
37 an atlas. Such identification requires extensive knowledge and it makes use of
38 complex terminology in a way that even a professional botanist needs to spend
39 much time in a field to achieve plant identification. The plant identification
40 could be automatically achieved through using the plants' features that are ex-
41 tracted from their images and then these features can be classified using various
42 classifier techniques such as, Neuro-Fuzzy Classifier (Chaki et al., 2016), Sup-
43 port Vector Machine (SVM) (Arun Priya et al., 2012a), etc. Since some plants'
44 flowers and fruits are seasonal and their colors are changed according to the
45 season, the leaves are more suitable to identify plants than flowers and fruits.
46 Hence, the majority of the existing computer-based plant identification has used

47 the leaves of plants (Chaki and Parekh, 2012; Chaki et al., 2015, 2016). The
48 automatic plant identification based on information technology is a very vital
49 task for different parties: agriculture, pharmacological, forestry science. Auto-
50 matic plant identification process will achieve fast, cheap, and accurate systems,
51 which provide a great help to medicine, industry, and foodstuff production, as
52 well as to biologists, chemists, and environmentalists.

53 This paper describes an approach addressing the plant identification prob-
54 lem by using features that are extracted from digital images of plant leaves as it
55 is a low-cost and convenient way to get leaf images dataset. The approach used
56 two features extraction techniques (one-dimensional (1D) and two-dimensional
57 (2D) based) with the Bagging classifier. For the 1D-based techniques, PCA,
58 PCA+LDA, and Direct-LDA techniques were applied, while 2DPCA and 2DLDA
59 algorithms were used for the 2D-based method. To classify the extracted fea-
60 tures in both methods, the Bagging classifier, with the decision tree as a weak
61 learner was used.

62 The rest of the paper is organized as follows; Section (2) summarizes the
63 related work of the plant identification based on machine learning. Section (3)
64 highlights the feature extraction methods and the classifier used in the design
65 of the proposed approach which is presented in Section (4). The experimental
66 results are reported in Section (5) while the results' discussion and the conclusion
67 are presented in Section (6) and Section (7), respectively.

68 2. Related Works

69 There are a number of plant identification approaches that used digital im-
70 ages (Valliammal and Geethalakshmi, 2011; Arora et al., 2012; Arun Priya et al.,
71 2012b; Satti et al., 2013). Satti *et al.* classified plant leaves based on 2D im-
72 ages. They used Flavia image dataset and applied many preprocessing steps on
73 the leaf images (Satti et al., 2013). Their approach achieved accuracy 85.9%
74 and 93.3% using k -Nearest Neighbour (k -NN) and Artificial Neural Networks
75 (ANN) classifiers, respectively. Arora *et al.* applied the Speed Up Robust Fea-

76 tures (SURF) to extract the features from leaf images and then used the Random
77 Forest (RF) classifier and tested their approach using Plant Leaves II dataset
78 (Arora et al., 2012). In another research, Caglayan *et al.* utilized color and
79 shape features to classify 32 different kinds of plants. They used SVM, k -NN,
80 RF, and Naive Bayes (NB) classifiers and the RF classifier achieved the best
81 accuracy (96%) (Caglayan et al., 2013). Arun *et al.* transformed the leaf images
82 into grayscale and applied boundary enhancement operations (Arun Priya et al.,
83 2012b). They then used the PCA to extract features and then used SVM and
84 k -NN for classification. They used Flavia dataset and achieved the accuracy of
85 78% to 81.3% using k -NN classifier.

86 Valliamma *et al.* proposed identification approach for flower images dataset
87 (Valliammal and Geethalakshmi, 2011). They applied Preferential Image Seg-
88 mentation (PIS) and other enhancement operations to the images. They then
89 used the image thresholding to obtain some features and then used the prob-
90 abilistic curve for classification. They used a dataset of 500 flowers images.
91 In another research, Uluturk and Uger converted the plant leaf images into
92 grayscale, the region of interest was segmented and the features were extracted
93 (Uluturk and Ugur, 2012). Probabilistic Neural Networks (PNN) classifier was
94 then used of Flavia dataset and the classification rate was 92.5%.

95 Recently, Chaki *et al.*, proposed a plant recognition approach using both of
96 texture and shape features (Chaki et al., 2015). The texture features were ex-
97 tracted by Gray Level Co-occurrence Matrix (GLCM) and Gabor filter while the
98 shape features were extracted using the curvelet transform coefficients and the
99 invariant moments. This approach was tested using two neural-based classifiers:
100 a feed-forward back-propagation Multi-Layered Perceptron (MLP) and a Neuro-
101 Fuzzy Classifier (NFC) to classify 31 plant species of leaves images. In another
102 study, (Chaki et al., 2016) proposed another approach based on ridge filter and
103 curvelet transform with a Neuro-Fuzzy classifier. The classification accuracy of
104 almost all classes (plant species) was 100%. However, it needs preprocessing
105 step which imposes more CPU time.

106 **3. Preliminaries**

107 In this section, the background of the PCA and LDA methods are introduced.
108 Moreover, the details of how to use both methods in vector or matrix form are
109 explained below.

110 *3.1. Feature Extraction Method*

111 The aim of the feature extraction step is to transform the objects' proper-
112 ties into numeric values. There are many types of features for an image such as
113 shape, texture, and color features. The shape features are used to describe the
114 shape of the image or the Region of Interest (ROI) while the texture features
115 describe the texture analysis of the image. The texture features methods are
116 generally classified into two methods: sparse method and dense method. In
117 the sparse method, the interest points are first detected and then a local patch
118 around these points is constructed, and finally, invariant features are extracted.
119 *Scale Invariant Feature Transformation* (SIFT) is one of the most common al-
120 gorithms in the sparse descriptor method (Lowe, 1999; Tharwat et al., 2015). In
121 the dense method, the local features are extracted from each pixel over the input
122 image. *Local Binary Patterns* (LBP) is one of the most common algorithms in
123 dense method (Ojala et al., 2002; Tharwat et al., 2014b). The color features are
124 widely used in image retrieval due to its robustness against image size variation
125 and orientation (Salvador et al., 2004). The feature extraction techniques used
126 in the proposed approach are highlighted below.

127 *3.1.1. An Overview of PCA*

128 (PCA) is one of the classical feature extraction techniques that is widely
129 used in the areas of pattern recognition and computer vision since Turk and
130 Pentland (Turk and Pentland, 1991) used it for face recognition in 1991. From
131 that time, PCA has been widely used in face recognition and many other pattern
132 recognition applications such as dimensionality reduction (Moore, 1981), face
133 recognition (Turk and Pentland, 1991; Yang et al., 2004), and ear recognition
134 (Tharwat et al., 2012).

135 The PCA is an unsupervised method that is used to search for a new space
 136 (PCA space or eigen space), W_{PCA} , which reduces the d -dimensional feature
 137 vectors to k -dimensional feature vectors (where $k < d$).

138 Given $I = \{I_1, I_2, \dots, I_M\}$, where $I_i \in \mathcal{R}^d$ is the i^{th} pattern or sample, d
 139 is the dimension or the number of features of I_i , and M is the total number
 140 of samples. PCA searches for the PCA space (W_{PCA}) which represents the
 141 direction of the maximum variance of the given data. The PCA space consists
 142 of k orthonormal and uncorrelated Principal Components (PCs). The first step
 143 of the PCA method is to calculate the covariance matrix Σ as follows:

$$\Sigma = \frac{1}{M-1} D \times D^T, \quad (1)$$

$$D = \{d_1, d_2, \dots, d_M\} = \sum_{i=1}^M I_i - \mu \quad (2)$$

144 where $\mu = \frac{1}{M} \sum_{i=1}^M I_i$ is the mean of all samples. The eigenvalues ($\{\lambda_1, \lambda_2, \dots, \lambda_d\}$)
 145 and eigenvectors ($\{v_1, v_2, \dots, v_d\}$) of Σ are then calculated. The eigenvector
 146 with the highest eigenvalue represents the first principal component and it has
 147 the maximum variance as shown in Figure 1a (Turk and Pentland, 1991; Strang,
 148 2003). As shown in the figure, the first principal component (PC1) points to the
 149 maximum variance. Algorithm (1) summarizes the steps of the PCA technique.

150 3.1.2. An Overview of LDA

151 LDA is also a well-known algorithm for feature extraction and dimensional-
 152 ity reduction. LDA is widely used in different applications such as biometrics
 153 (Marcialis and Roli, 2002; Tharwat et al., 2014a), bioinformatics (Wu et al.,
 154 2009), and chemoinformatics (Mitchell, 2014). LDA is a supervised dimension-
 155 ality reduction and feature extraction method (Galdámez et al., 2015). It finds
 156 the projection space that maximizes the ratio of the between-class variance,
 157 S_B , to the within-class variance, S_W , and hence guaranteeing maximum class
 158 separability as shown in Figure 1b (Welling, 2005). From the figure, there are
 159 two sub-spaces that can be selected to represent the LDA space. As shown, in

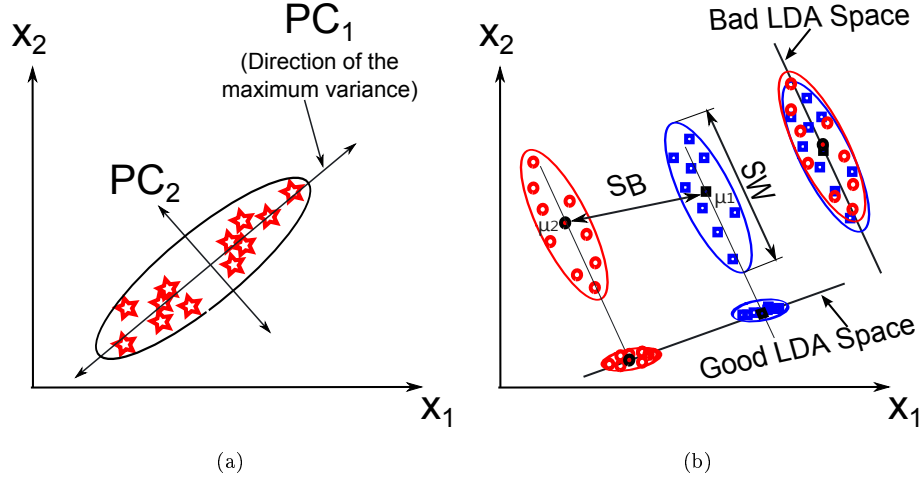


Figure 1: A visualization of the PCA and LDA techniques; (a) PCA, (b) LDA.

Algorithm 1 : PCA

- 1: Given a feature matrix which consists of all training samples, each sample is represented by a single column as follows, $I = [I_1, I_2, \dots, I_M]$, where M represents the total number of samples, I_i represents a training sample.
 - 2: Compute the mean of all classes (total mean) $\mu = \frac{1}{M} \sum_{i=1}^M I_i$.
 - 3: Subtract the mean from all training samples as follows, $D_i = I_i - \mu$.
 - 4: Compute covariance matrix $Cov = \frac{1}{M-1} \sum_{i=1}^M D_i * D_i^T$.
 - 5: Compute eigenvectors V and eigenvalues λ of the covariance matrix.
 - 6: Sort eigenvectors according to their corresponding eigenvalues.
 - 7: Select k eigenvectors that have the largest eigenvalues $W_{PCA} = \{v_1, v_2, \dots, v_k\}$. The selected eigenvectors represent the projection space of PCA (W_{PCA}).
-

160 the bad LDA space, the two classes cannot be discriminated because the S_B
 161 between the two classes decreased. On the other hand, in the good LDA space,
 162 S_W is decreased while S_B is increased and hence the two classes are perfectly
 163 discriminated.

164 Assume the training samples belong to C classes. The aim of the LDA

165 method is to search for the subspace, W_{LDA} , which maximizes S_B and minimizes
 166 S_W as follows:

$$J(w) = \frac{W_{LDA}^T S_B W_{LDA}}{W_{LDA}^T S_W W_{LDA}}, \quad (3)$$

$$S_B = \sum_{i=1}^C \frac{n_i}{M} (\mu_i - \mu)(\mu_i - \mu)^T, \quad (4)$$

$$S_W^i = \frac{1}{n_i} \sum_{j=1}^{n_i} (I_j^i - \mu_i)(I_j^i - \mu_i)^T, \quad (5)$$

$$S_W = \sum_{i=1}^C \frac{n_i}{M} S_W^i \quad (6)$$

167 where n_i is the number of samples of class i , $\mu_i = \frac{1}{n_i} \sum_{j=1}^{n_i} I_j^i$ is the mean of
 168 class i , $\mu = \frac{1}{C} \sum_{i=1}^C \mu_i = \frac{1}{M} \sum_{j=1}^M I_j^i$ represents the global mean or the mean of
 169 all samples, I_j^i is the j^{th} sample in the i^{th} class, $M = \sum_{i=1}^C n_i$, and S_W^i is the
 170 within-class matrix of the i^{th} class. Algorithm (2) summarizes the steps of the
 171 LDA technique.

172 In practice, S_W is always singular, this is the so-called singularity, Small
 173 Sample Size (SSS), or under-sampled problem. This problem is common in LDA
 174 technique and it results from high-dimensional pattern classification applications
 175 or a small number of training samples available for each class compared with the
 176 dimensionality of the sample space (Lu et al., 2005; Ye and Xiong, 2006). The
 177 SSS problem occurs when the S_W is singular². The upper bound of the rank³
 178 of S_W is $M - C$, while the dimension of S_W is $d \times d$ (Lu et al., 2005; Feng and
 179 Wu, 2014). Thus, in most cases $d \gg M - C$ which leads to SSS problem. For
 180 example, in face recognition applications, the size of the face image may reach

²A matrix is singular if it is square, does not have a matrix inverse, and/or its determinant is zero; hence not all columns and rows are independent (Strang, 2003).

³The rank of the matrix represents the number of linearly independent rows or columns (Strang, 2003).

181 to $100 \times 100 = 10000$ pixels, which represent high-dimensional features and it
 182 leads to a singularity problem.

183 There are two common solutions to SSS problem. The first solution is to
 184 use a non-singular intermediate, e.g. PCA space, to reduce the dimension of
 185 the original data to be equal to the rank of S_W , hence S_W becomes full-rank
 186 and S_W can be inverted. The second solution is to remove the null-space of S_B
 187 which contains no useful information for recognition by diagonalizing S_B and
 188 then diagonalizing S_W . These two solutions were used in this paper.

Algorithm 2 : Linear Discriminant Analysis (LDA)

- 1: Given a set of M samples $[I_i]_{i=1}^M$, each of which is represented as a column
 as follows, $I = [I_1, I_2, \dots, I_M]$ and each sample is represented by d features.
- 2: Compute the mean of each class, μ_i , and the total mean of all samples, μ .
- 3: Compute within-class scatter matrix, S_W , as in Equations (5 and 6) and
 the between-class scatter matrix S_B as in Equation (4).
- 4: Calculate the eigenvalues (λ) and eigenvectors (V) of $S_W^{-1}S_B$ as follows:

$$S_B V = S_W V \lambda \quad (7)$$

- 5: Sort the eigenvectors in descending order according to their corresponding
 eigenvalues, then use the first, k , eigenvectors as a lower dimensional space
 (W_{LDA}).
-

189 *3.1.3. One-Dimensional Feature Extraction Technique:*

190 The classical PCA (i.e. 1DPCA) and LDA (i.e. 1DLDA) use one-dimensional/vector
 191 form to calculate projection spaces as shown in Figure 2. In both methods, a
 192 two-dimensional image ($I_i(r \times c)$, $\forall i = 1, 2, \dots, M$) is first converted into one
 193 feature vector (column or row), where r and c represent the number of rows
 194 and columns of the image, respectively. All the feature vectors are then con-
 195 catenated to form a feature matrix ($I = \{I_1, I_2, \dots, I_M\}$), where M refers to
 196 the total number of images. The PCA and LDA spaces, W_{PCA} and W_{LDA} , of
 197 this matrix (I) can be calculated. The features are then extracted by project-

198 ing the feature matrix on the calculated spaces as follow, $Y = W^T I$, where W
 199 represents the lower dimensional space (i.e. PCA or LDA) (see Figure 3a).

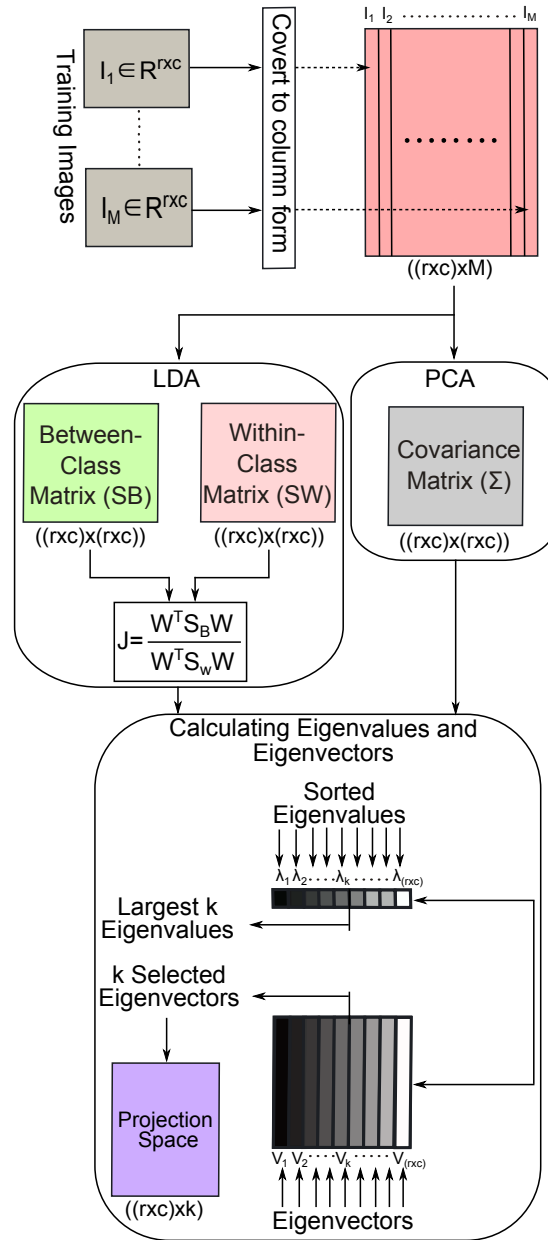


Figure 2: Visualized steps to calculate a projection space of one-dimensional PCA and LDA (1DPCA and 1DLDA) methods.

200 Vector representation may lead to a high-dimensional data. Hence, it is dif-
 201 ficult to calculate the covariance matrix in PCA due to its large size. Moreover,
 202 the high-dimensional data leads to SSS problem in LDA. These two problems
 203 can be solved using the two-dimensional methods, i.e. 2DPCA and 2DLDA.

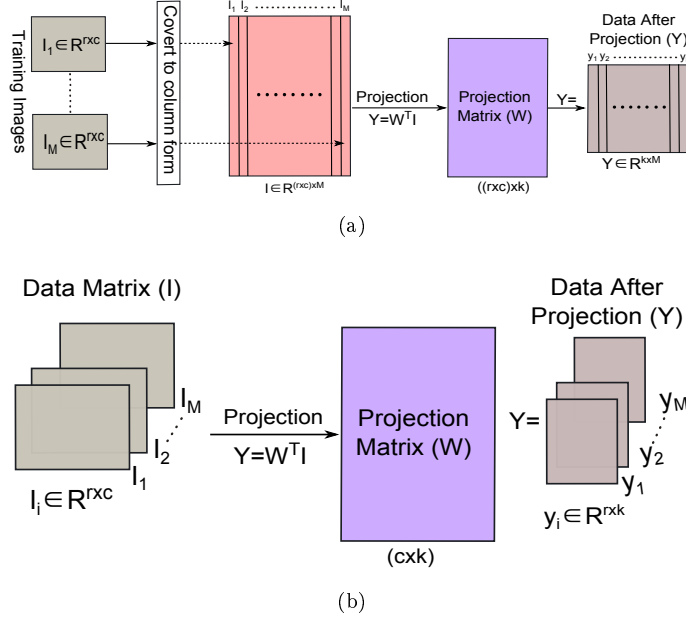


Figure 3: A visualization of the projection of one-dimensional and two-dimensional methods;
 (a) one-dimensional method, (b) two-dimensional method.

204 3.1.4. Two-Dimensional Feature Extraction Techniques

205 The spaces of the PCA and LDA techniques can be calculated in two-
 206 dimensional/matrix form, i.e. 2DPCA and 2DLDA, as shown in Figure 4.
 207 Hence, there is no need for the step of converting each image into one vec-
 208 tor prior to feature extraction step which saves more computational time. As in
 209 one-dimensional technique, the PCA and LDA spaces, W_{PCA} and W_{LDA} , are
 210 calculated and the features are then extracted by projecting the feature matrix
 211 on the calculated spaces as follows, $Y = W^T I$ (see Figure 3b).

212 *3.1.4.1. Two Dimensional PCA (2DPCA).* The aim of the 2DPCA method is
 213 to find the PCA space, W_{PCA} , to project the two-dimensional image ($I_i \in \mathcal{R}^{r \times c}$)
 214 as follows, $Y_i = W_{PCA}^T I_i$, where Y_i is the projected feature vector of the image
 215 I_i . First, the M two-dimensional images are used to calculate the covariance
 216 matrix ($\Sigma \in \mathcal{R}^{c \times c}$) as in Equation (8). The eigenvalues and eigenvectors of Σ
 217 are then calculated and k optimal eigenvectors, i.e. projection axes, are selected.
 218 In other words, the 2DPCA method then searches for the PCA space $W_{PCA} =$
 219 $\{v_1, v_2, \dots, v_k\}$ which maximizes the variance as in classical PCA, where v_i is
 220 the i^{th} principal component and k is the number of selected eigenvectors that
 221 represent the PCA space. This projection space is used for feature extraction of
 222 the image as follows, $Y_i = W_{PCA}^T I_i$, where $Y_i \in \mathcal{R}^{r \times k}$ represents the projected
 223 feature vectors, i.e. feature matrix or feature image, of the image I_i (Yang et al.,
 224 2004).

$$\Sigma = \frac{1}{M-1} \sum_{j=1}^M (I_j - \mu)^T (I_j - \mu) \quad (8)$$

225 where μ is the mean of all training images, M is the number of training images,
 226 and I_j represents the j^{th} training image.

227 *3.1.4.2. Two Dimensional LDA (2DLDA).* The aim of the 2DLDA method is
 228 to find the LDA space, W_{LDA} , to extract the features by projecting the two-
 229 dimensional image on the LDA space using $Y_i = W_{LDA}^T I_i$. Assume I_i represents
 230 one image and M two-dimensional images are used to calculate within-class
 231 matrix (S_W) and between-class variance (S_B). The eigenvalues and eigenvectors
 232 of $S_W^{-1} S_B$ are then calculated and k optimal eigenvectors are selected to form
 233 the LDA space, i.e. Fisher projection matrix using $W_{LDA} = \{v_1, v_2, \dots, v_k\}$
 234 which maximizes the ratio between S_B and S_W as in classical LDA, where v_i is
 235 the i^{th} eigenvector.

236 3.2. The Bagging Classifier

237 The Bagging classifier is one of the ensemble classifiers creating its ensemble
 238 by training different classifiers or weak learners on a random distribution of

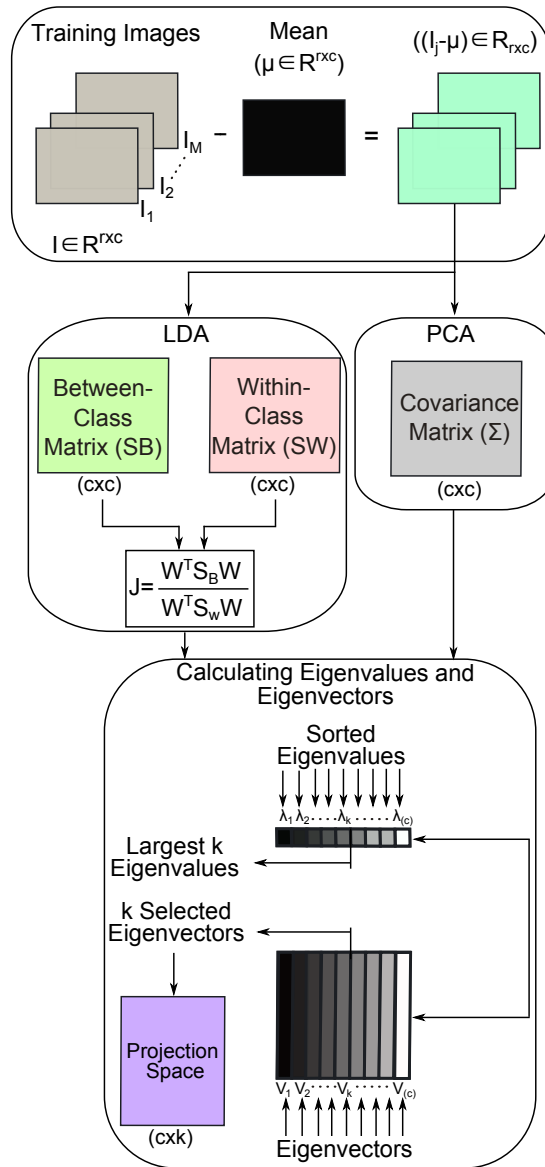


Figure 4: Visualized steps to calculate a projection space of two-dimensional PCA and LDA (2DPCA and 2DLDA) methods.

239 a training dataset. A weak learner is a simple, fast, and easy to implement
 240 classifier such as single level decision tree or simple neural networks (Kuncheva,
 241 2014).

242 Generally, as given in Algorithm (3), a Bagging classifier consists of two
 243 phases: training and testing. In the training phase, for each iteration, t , a
 244 number of training samples are selected randomly (S_t), and these samples are
 245 used to train one weak learner (C_t) as shown in Figure 5. In the testing phase, all
 246 the weak learners are used to classify an unknown sample (I_{test}). The outputs
 247 of all weak learners are combined using majority voting method to determine
 248 the final decision (Kuncheva, 2014).

Algorithm 3 Bagging Classifier Algorithm

- 1: Given a training set $I = (I_1, y_1), \dots, (I_M, y_M)$, where y_i represents the label of samples $I_i \in I$ and M denotes the total number of samples in the training set.
 - 2: **while** ($t < T$) **do**
 - 3: Select a sample S_t from I .
 - 4: Use S_t to train the current weak learner C_t .
 - 5: **end while**
 - 6: Given new test pattern I_{test} .
 - 7: Classify I_{test} using all weak learners.
 - 8: Combine the outputs of all weak learners to determine the final prediction.
-

249 **4. Proposed Approaches**

250 The proposed plant identification approach consists of two phases. In the
 251 first phase, two main feature extraction methods (1D-based and 2D-based) were
 252 used. In the 1D-based feature extraction method, 1DPCA, Direct LDA (DLDA),
 253 and (PCA+LDA) techniques were used while in the 2D-based method, 2DPCA
 254 and 2DLDA were applied for the feature extraction step. For the identification,
 255 in both techniques, the Bagging classifier was used to identify the type of the
 256 unknown leave image as shown in Figure 5. As shown in Figure 5, the proposed
 257 model has two main phases: training and testing phases.

258 *4.1. Training Phase*

259 In the training phase, M images ($I_{i=1}^M$) were used to train the proposed
260 model. In the 1D-based method, each image was first transformed into one
261 vector and then all training images' vectors were combined into a matrix, $I =$
262 $[I_1, I_2, \dots, I_M]$ (see Figure 2). In the 2D-based method, the training image was
263 not changed but represented as 2D matrix as seen in Figure 4. The PCA or LDA
264 spaces, W , of I were then constructed. The features were then extracted from
265 all training images by projecting the images on the space. These features were
266 used to train the Bagging model. The steps of the training phase are explained
267 in detail in Algorithm (4).

Algorithm 4 : Training Phase

- 1: Read the training images.
 - 2: **if** (1D-based method) **then**
 - 3: Convert all images $I_i(r \times c)$, $i = 1, \dots, M$ into vectors $I_i((r \times c) \times 1)$.
 - 4: Combine all feature vectors into a matrix ($I = [I_1, I_2, \dots, I_M]$).
 - 5: **else**
 - 6: Deals with images in 2D form (i.e. matrix representation).
 - 7: Combine all feature vectors into a matrix ($I = [I_1, I_2, \dots, I_M]$).
 - 8: **end if**
 - 9: Compute the projection space (W).
 - 10: Project I on the projection surface (W) to obtain the features as follows,
 $Y = W^T I$.
 - 11: Train the Bagging classifier using the extracted features, Y .
-

268 *4.2. Testing Phase*

269 In the testing phase, an unknown leave image (I_{test}) was tested for its plant
270 identification. To do so, firstly the leave features were extracted by projecting
271 it on the projection space, W , that was computed in the training phase, i.e.
272 $Y_{test} = W^T I_{test}$. The computed vector Y_{test} was classified using the Bagging

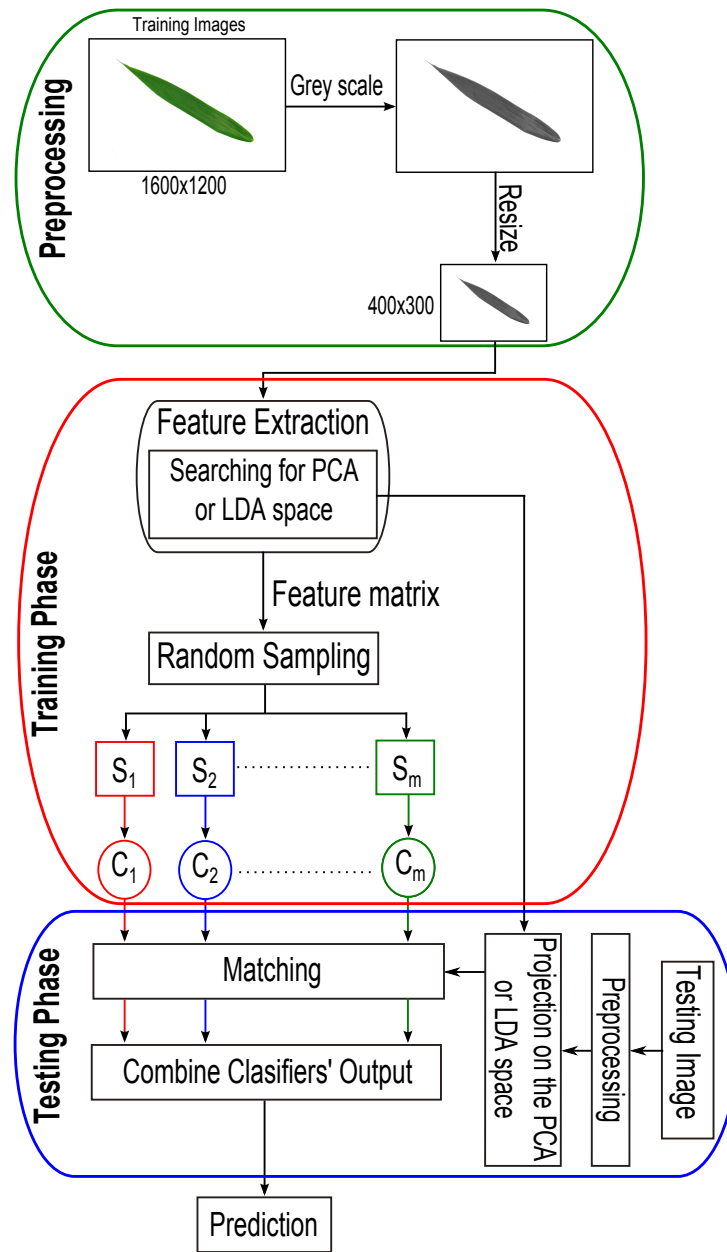


Figure 5: Plant identification system using leaves' images

273 classifier's model that has been also built in the training phase. Detailed steps
 274 of this phase are given in Algorithm (5)

Algorithm 5 : Testing Phase

- 1: Read an unknown leaf image (I_{test}).
 - 2: **if** (1D-based method) **then**
 - 3: Convert this image $I_{test}(r \times c)$ into a vector form, $I'_{test}((r \times c) \times 1)$.
 - 4: **else**
 - 5: Deals with the image in 2D form (i.e. matrix representation).
 - 6: **end if**
 - 7: Project the unknown 2D image on the projection space to get y_{test} .
 - 8: Match between y_{test} with Y using the Bagging model that built during the training phase to find the class label of the unknown image.
-

275 5. Experimental Results

276 To evaluate our proposed approach, the Flavia public dataset was used.
277 This dataset consists of 1907 colored leaves images with size (1600×1200)
278 and collected from 33 different species. The selected images are in different
279 orientations, illumination, and quality. In this paper, all colored images were
280 converted into grey scale images as shown in Figure 5. Next, all images were
281 resized to be 400×300 to reduce the computational time. Figure 6 shows
282 different samples from the dataset.

283 Four scenarios were designed to evaluate the performance and accuracy of the
284 proposed model (using 1DPCA, PCA+LDA, DLDA, 2DPCA, and 2DLDA). In
285 these scenarios, the Bagging classifier ensemble, with different numbers of weak
286 learners was used to match the unknown image with the trained images. Due
287 to the high dimensionality of the data, 1DLDA was not suitable for the feature
288 extraction. The reason of this high-dimensionality of the one-dimensional form
289 of the image was $d = 400 \times 300 = 120000$ and hence $d \gg M - C$ which leads to
290 SSS problem, where M is the total number of samples and C is the number of
291 classes. To avoid this problem, PCA+LDA and Direct LDA (DLDA) methods
292 were used for the feature extraction in the one-dimensional method.

293 In the first scenario, the accuracy of the two methods (1D-based and 2D-

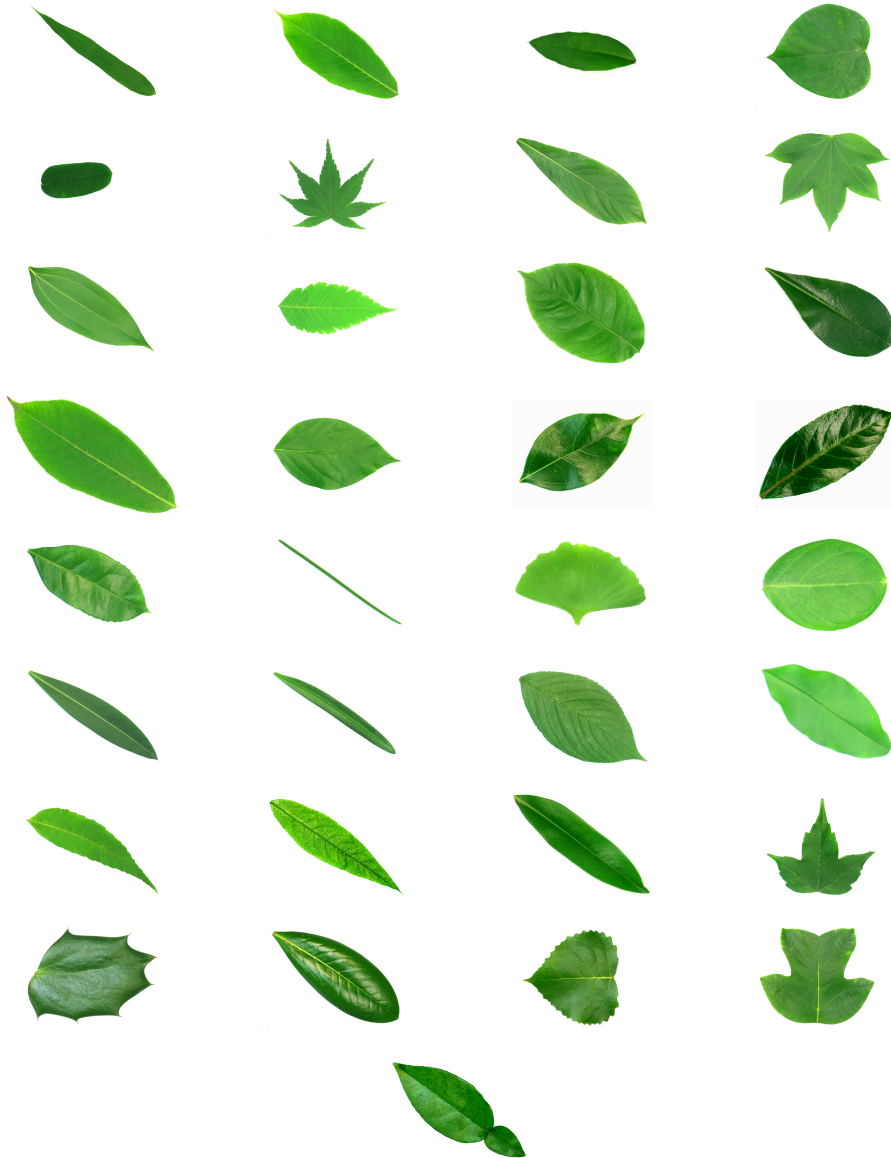
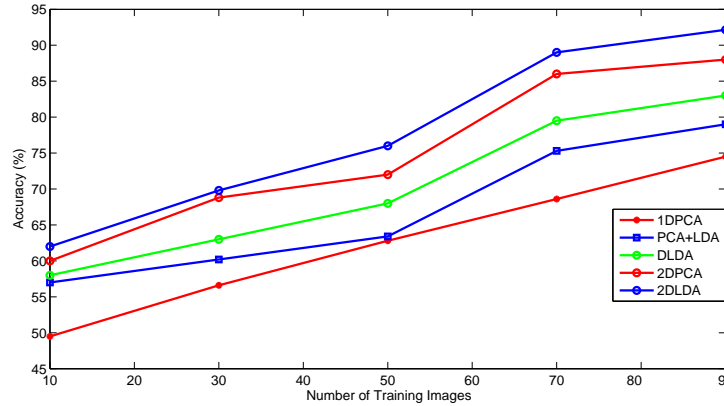


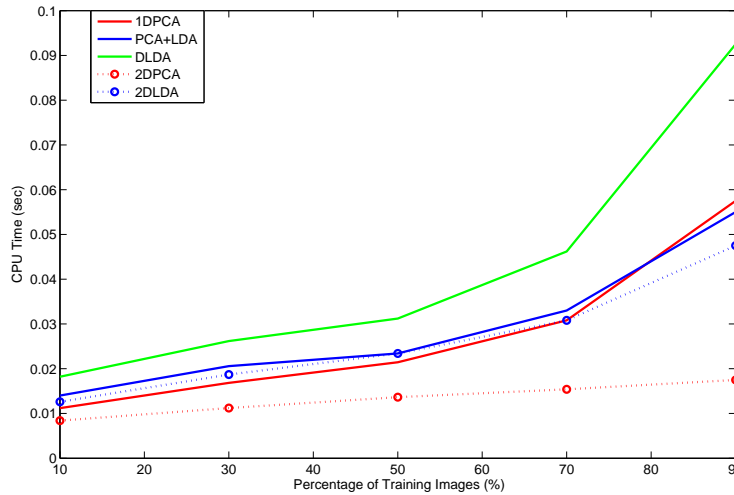
Figure 6: Sample of different leaves' images (one sample from each class or plant).

294 based) was investigated through testing different percentages of training images
295 of each plant type, i.e. class. The training images were selected randomly from
296 the database while the remaining images, were used during the testing phase.

297 In this scenario, the size of Bagging classifier was five. The accuracy and CPU
 298 time of this scenario are shown in Figure 7.



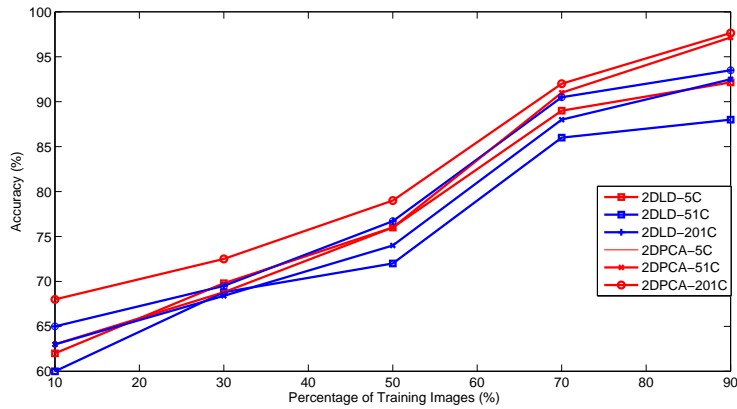
(a)



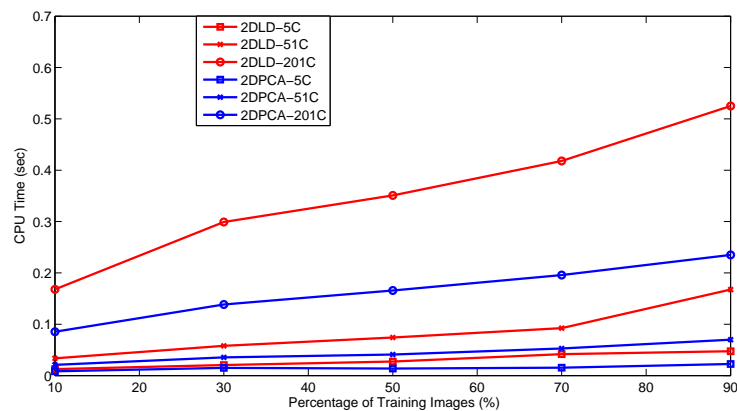
(b)

Figure 7: Accuracy and CPU time of the proposed model using 1DPCA, PCA+LDA, DLDA, 2DPCA, and 2DLDA with different percentages of the training images and five weak learners of the Bagging classifier; (a) Accuracy, (b) CPU time.

299 The second scenario was designed based on the results of the first one in



(a)



(b)

Figure 8: Accuracy and CPU time of the 2D-based method with different number of training images and weak learners of the Bagging classifier.

300 which the 2D-based methods gave better results than that of the 1D-based one.
 301 Thus, the aim of this scenario was to further understand the effect of changing
 302 the number of training images and to evaluate the accuracy and the performance
 303 stability over the standardize data. In this scenario, the 2DPCA and 2DLDA
 304 were used to extract the images' features. The Bagging classifier was then used
 305 in many experiments at different values of its weak learners (i.e. 5, 51, and

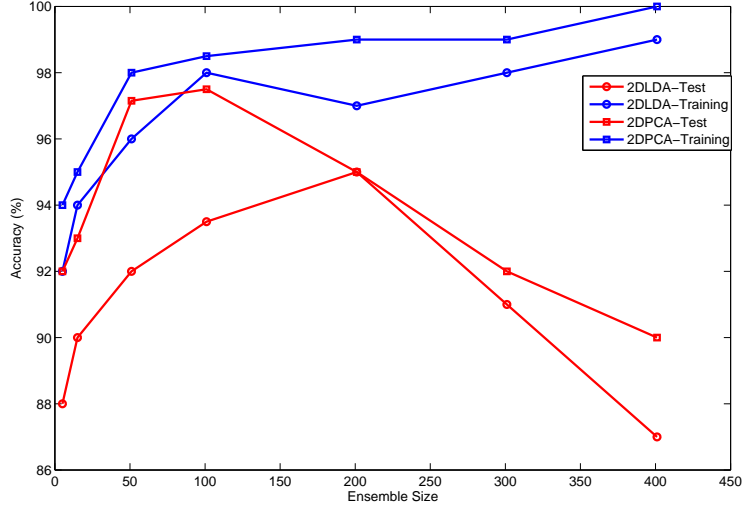
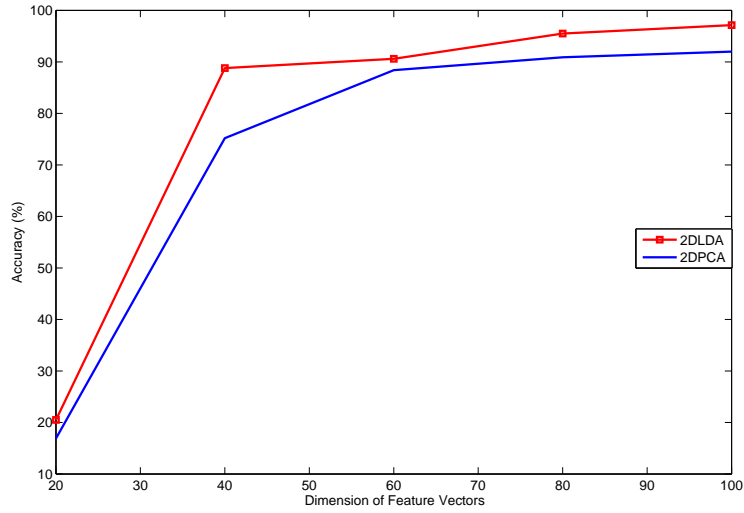


Figure 9: A comparison between the training and testing accuracy of 2DLDA and 2DPCA method using different ensemble sizes.

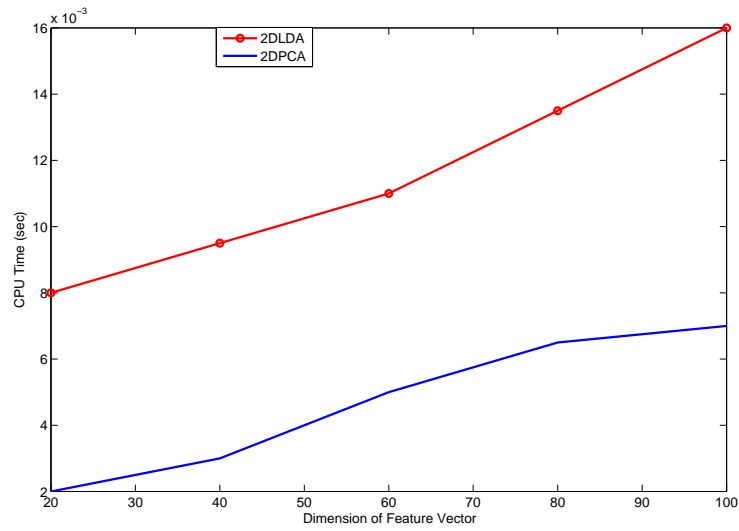
201). In addition, the percentage of training images was ranged from 10% to
 306 90%. The results obtained from this scenario are shown in Figure 8. Moreover,
 307 a comparison between the training and testing accuracy of the Bagging model
 308 is shown in Figure 9.

309 The third scenario was conducted to investigate the relationship between the
 310 accuracy and the dimension of the feature vectors of the 2DPCA and 2DLDA
 311 methods. In other words, the accuracy of the 2DPCA and 2DLDA was tested
 312 against different numbers of eigenvectors constructing the projection space. In
 313 this experiment, series of different dimensions were used. Moreover, 90% of the
 314 images from each class were used to train the model, while the other images
 315 were used to test the model. In addition, there were 51 weak learners in the
 316 Bagging classifier. Figure 10 shows the results of this experiment.

317 The fourth and last scenario was conducted to compare the accuracy of the
 318 2DLDA method when different classifiers (Bagging, k -NN, and MLP) were used.
 319 In all experiments of this scenario, 51 weak learners were used in the Bagging
 320



(a)



(b)

Figure 10: Accuracy of the two-dimensional methods (2DPCA and 2DLDA) with varying dimensions of the feature vectors; (a) Accuracy, (b) CPU Time.

Table 1: Accuracy rate of the proposed model using Bagging, k -NN, and MLP classifiers.

Class	Bagging	k -NN	MLP	Class	Bagging	k -NN	MLP	Class	Bagging	k -NN	MLP
1	98	94	98	12	100	94	92	23	98	94	96
2	100	90	98	13	100	86	94	24	100	90	96
3	97	90	95	14	96	86	92	25	100	92	94
4	100	94	96	15	98	92	92	26	98	94	94
5	96	96	96	16	92	90	92	27	98	94	96
6	98	90	92	17	96	92	92	28	98	90	96
7	100	92	88	18	96	82	88	29	100	92	97
8	96	85	90	19	98	94	96	30	98	90	94
9	94	88	86	20	96	92	96	31	92	87	92
10	98	92	94	21	92	87	90	32	98	86	92
11	98	84	92	22	86	81	82	33	100	96	96

321 classifier, five nearest neighbours ($k = 5$) in the k -NN classifier, and 30 and
 322 33 nodes for the hidden and output layers, respectively, in the MLP classifier.
 323 Moreover, 90% of the images from each class were used to train the model, while
 324 the other images were used to test the model. The accuracy of each class of this
 325 experiment are summarized in Table 1

326 6. Discussion

327 From the results of the first scenario, shown in Figure 7, the following re-
 328 marks can be drawn. Firstly, in terms of accuracy issues, the accuracy of all five
 329 variants (i.e. 1DPCA, PCA+LDA, DLDA, 2DPCA, and 2DLDA) was improved
 330 when the number of training images was increased. This can be explained, as
 331 reported in (Brain et al., 1999), using more training images will decrease the
 332 variance⁴ and hence decreases the overfitting. Secondly, the accuracy of the
 333 2D-based methods (i.e. 2DPCA and 2DLDA) was better than that of the 1D-
 334 based methods (i.e. 1DPCA, PCA+LDA, and DLDA). Thirdly, the 2DLDA
 335 method achieved the best accuracy and the 1DPCA-based one accomplished
 336 the worst accuracy. Fourthly, DLDA method achieved accuracy better than

⁴The variance is the error from sensitivity to small variations in training samples

337 PCA+LDA method because PCA+LDA method loses more information than
338 DLDA as mentioned in Section 3.1.2.

339 In terms of the CPU performance, from Figure 7b, it can be noticed that
340 the 2DPCA is the most efficient algorithm among all other methods and the
341 DLDA is the worst one. This can be explained as the high dimensionality of the
342 one-dimensional data. Mathematical interpretation of this point shows that the
343 size of the image covariance matrix using 2DPCA ($c \times c$) is much smaller than
344 in 1DPCA ($(r \times c) \times (r \times c)$). As a result, less time is required to determine
345 the corresponding eigenvectors when the 2DPCA is used. For example, in our
346 case, the size of the image after resizing it was 400×300 . Hence, to calculate
347 the covariance matrix of 2DPCA, it is required to multiply two matrices of
348 (300×300). But, when using the 1DPCA, all training images are converted into
349 one vector (1×120000), and the covariance matrix is computed by multiplying
350 two matrices $(M \times 120000) \times (120000 \times M)$, where M represents the total number
351 of training images. Thus, 2DPCA method takes CPU time much lower than
352 1DPCA method. Similarly, 2DLDA involves the eigen-decomposition of matrix
353 S_W and S_B which have dimensions much smaller than in 1DLDA method. This
354 reduction dramatically reduces the computational time and memory space of
355 2DLDA method (Ye et al., 2004). Moreover, in 1DLDA, S_W is singular in most
356 cases because the dimension of the samples is greater than the number of samples
357 in each class. However, 2DLDA overcome this problem efficiently because the
358 rank of any training image is equal to $\min(r, c)$. Hence, the rank of S_W is less
359 than or equal to $(M - C) \cdot \min(r, c)$ (Li and Yuan, 2005). Thus, in 2DLDA, S_W
360 is nonsingular when Equation (9) is true. In real practical problems, Equation
361 (9) is always satisfied. Thus, S_W is always nonsingular, hence, SSS problem can
362 be solved using 2DLDA (Li and Yuan, 2005).

$$M \geq C + \frac{c}{\min(r, c)} \quad (9)$$

363 From Figure 8 the following remarks can be noticed. Firstly, the higher
364 number of iterations of Bagging classifier used, the better classification accuracy

365 achieved. However, this was accomplished on the cost of taking more CPU time
366 (see Figure 8b). Secondly, the 2DLDA method achieved identification accuracy
367 better than that of the 2DPCA method, but this was also accomplished with
368 more CPU time. This is because of LDA searches in the space that extracts the
369 most discriminative features, while the PCA searches in the space that extracts
370 the data with the high variance. Thirdly, increasing the ensemble size led to the
371 complexity of the bagging model and hence took more CPU time and may lead to
372 the overfitting problem. Figure 9 shows a comparison between the training and
373 testing accuracy. In this figure, the training accuracy of 2DLDA and 2DPCA
374 methods was increased till it reached to an extent at which it remained constant.
375 On the other hand, the testing accuracy was increased when the ensemble size
376 was increased till it reached to an extent after which it reduced again. As shown
377 in the figure, the best ensemble size was approximately 201.

378 From Figure 10a, two remarks can be noticed. First, the accuracy of the
379 2DPCA and 2DLDA methods is proportional with the number of eigenvectors.
380 Second, a major change (about 60%) in the accuracy achieved when the percent-
381 age of the eigenvectors was increased from 20% to 40%. But, a minor change
382 (about 5%) in the accuracy achieved when the percentage of the accuracy ranged
383 from 40% to 100 %. This means that the most discriminative feature are con-
384 centrated nearly in the first half of the eigenvectors. In terms of CPU time and
385 from Figure 10b, it is clear the computational time of the 2DPCA and 2DLDA
386 methods increased when more eigenvectors were used to construct the PCA or
387 LDA space.

388 From Table 1, two remarks can be seen. First, the Bagging classifier achieved
389 the best accuracy rate (97.15%), while MLP and k -NN classifiers achieved
390 93.15% and 90.18%, respectively. The accuracy of the classes was ranged from
391 86% to 100% when Bagging classifier was used.

392 To further evaluate our proposed approach (2DPCA and 2DLDA which gave
393 the best results), a comparison was conducted with some state-of-the-art ap-
394 proaches which used different feature extraction methods and classifiers for the
395 same dataset. The results of this comparison are shown in Table 2. From this

Table 2: A comparison between our proposed plant identification method and some of state-of-the-art methods in terms of, classification accuracy, size of database images, feature extraction methods.

Author	Feature Extraction Method	Classification Method	Database Images	Results
(Arun Priya et al., 2012b)	Digital Morphological Features (DMFs) + PCA	k -NN SVM	5 classes (331 images)	k -NN (78%) SVM (94.5%)
(Caglayan et al., 2013)	Color+Shape	k -NN SVM NB RF	32 classes (1897 images)	k -NN (94.2%) SVM (92.9%) NB (88.95%) RF (96.32%)
(Satti et al., 2013)	Color+Shape	k -NN ANN	33 classes (1907 images)	k -NN (85.9%) ANN (93.3%)
(Chaki et al., 2015)	Texture+Shape	NFC MLP	31 classes (930 images)	NFC (81.6%) MLP (87.1%)
(Chaki et al., 2016)	Shape+Texture (statistical)	NFC	30 class (600 images)	NFC (97%)
Proposed Model	1DPCA, DLDA, PCA+LDA, 2DPCA, 2DLDA	Bagging	33 classes (1907 images)	1DPCA (72%) PCA+LDA (77%) DLDA (82%) 2DPCA (93.5%) 2DLDA (97.12%)

396 table, the following remarks can be drawn. Firstly, although the proposed ap-
397 proach and the one proposed by Satti *et al.* used all the classes of the Flavia
398 dataset (i.e, 33 classes), while the other approaches excluded some classes, our
399 proposed approach achieved the highest accuracy (97.12%). Secondly, Chaki *et*
400 *al.* also achieved high accuracy at (97%), but they used only 30 classes and
401 600 images while in our approach 33 classes and 1907 images were used in all
402 experiments.

403 As a general remark, from Figure 7 and Figure 8, it can be noticed that
404 the accuracy of the proposed approach with its variants is proportional to the
405 number of training images and the best accuracy is achieved when 90% of the
406 training images is used.

407 7. Conclusion

408 This paper presented a plant identification approach based on their 2D leaves
409 images. The approach consists of two main phases: feature extraction and clas-
410 sification. In the first phase, five algorithms (1DPCA, 1DLDA, Direct-LDA,
411 PCA+LDA, 2DPCA, and 2DLDA) were applied to extract the leaves features.
412 In the second phase, the Bagging classifier was employed to test which fea-
413 ture extraction technique could give the best accuracy and performance. The
414 five variants of the proposed approach were evaluated using all leave images of
415 Flavia dataset. The evaluation results showed the variants used the 2DPCA and
416 2DLDA were much better than the ones used the PCA, PCA+LDA, and Direct-
417 LDA. It also was found that the 2DLDA-based method was the best one. In
418 addition, experiments conducted for the Bagging classifier parameter (the size
419 of the weak learners) proved that the classification accuracy increased when this
420 parameter increased. Moreover, the results showed that the classification accu-
421 racy of the 2DPCA and 2DLDA methods was proportional with the number of
422 the selected eigenvectors and the highest accuracy was (97.12%) and achieved
423 using 2DLDA. Last but not least, a comparison with the most related work
424 showed that our approach achieved better accuracy under the same dataset and
425 same experimental setup. In the future work, deep learning techniques will be
426 investigated for plant identification using the same leaves' dataset.

427 Arora, A., Gupta, A., Bagmar, N., Mishra, S., Bhattacharya, A., 2012. A plant
428 identification system using shape and morphological features on segmented
429 leaflets: Team iitk, CLEF 2012. In: CLEF 2012 Evaluation Labs and
430 Workshop, Online Working Notes, Rome, Italy, September 17-20, 2012.
431 URL [http://ceur-ws.org/Vol-1178/CLEF2012wn-ImageCLEF-AroraEt2012.](http://ceur-ws.org/Vol-1178/CLEF2012wn-ImageCLEF-AroraEt2012.pdf)
432 pdf

433 Arun Priya, C., Balasaravanan, T., Thanamani, A. S., 2012a. An efficient leaf
434 recognition algorithm for plant classification using support vector machine. In:
435 Pattern Recognition, Informatics and Medical Engineering (PRIME), 2012
436 International Conference on. IEEE, pp. 428–432.

- 437 Arun Priya, C., Balasaravanan, T., Thanamani, A. S., 2012b. An efficient leaf
438 recognition algorithm for plant classification using support vector machine.
439 In: International Conference on Pattern Recognition, Informatics and Medical
440 Engineering (PRIME). IEEE, pp. 428–432.
- 441 Brain, D., Webb, G., Richards, D., Beydoun, G., Hoffmann, A., Compton, P.,
442 1999. On the effect of data set size on bias and variance in classification
443 learning. In: Proceedings of the Fourth Australian Knowledge Acquisition
444 Workshop, University of New South Wales. pp. 117–128.
- 445 Caglayan, A., Guclu, O., Can, A. B., 2013. A plant recognition approach using
446 shape and color features in leaf images. In: International Conference on Image
447 Analysis and Processing (ICIAP). Springer, pp. 161–170.
- 448 Chaki, J., Parekh, R., 2012. Plant leaf recognition using gabor filter. Interna-
449 tional Journal of Computer Applications 56 (10).
- 450 Chaki, J., Parekh, R., Bhattacharya, S., 2015. Plant leaf recognition using tex-
451 ture and shape features with neural classifiers. Pattern Recognition Letters
452 58, 61–68.
- 453 Chaki, J., Parekh, R., Bhattacharya, S., 2016. Plant leaf recognition using ridge
454 filter and curvelet transform with neuro-fuzzy classifier. In: Proceedings of
455 3rd International Conference on Advanced Computing, Networking and In-
456 formatics. Springer, pp. 37–44.
- 457 Feng, T.-t., Wu, G., 2014. A theoretical contribution to the fast implementation
458 of null linear discriminant analysis method using random matrix multiplica-
459 tion with scatter matrices. arXiv preprint arXiv:1409.2579.
- 460 Gaber, T., Tharwat, A., Snasel, V., Hassanien, A. E., 2015. Plant identification:
461 Two dimensional-based vs. one dimensional-based feature extraction methods.
462 In: 10th International Conference on Soft Computing Models in Industrial
463 and Environmental Applications. Springer, pp. 375–385.

- 464 Galdámez, P. L., Arrieta, A. G., Ramón, M. R., 2015. A small look at the ear
465 recognition process using a hybrid approach. *Journal of Applied Logic*.
- 466 Kuncheva, L. I., 2014. *Combining pattern classifiers: methods and algorithms*.
467 John Wiley & Sons, Second Edition.
- 468 Li, M., Yuan, B., 2005. 2d-lda: A statistical linear discriminant analysis for
469 image matrix. *Pattern Recognition Letters* 26 (5), 527–532.
- 470 Lowe, D. G., 1999. Object recognition from local scale-invariant features. In:
471 The proceedings of the seventh IEEE international conference on Computer
472 vision, 1999. Vol. 2. Ieee, pp. 1150–1157.
- 473 Lu, J., Plataniotis, K. N., Venetsanopoulos, A. N., 2005. Regularization studies
474 of linear discriminant analysis in small sample size scenarios with application
475 to face recognition. *Pattern Recognition Letters* 26 (2), 181–191.
- 476 Marcialis, G. L., Roli, F., 2002. Fusion of lda and pca for face verification. In:
477 *Biometric Authentication*. Springer, pp. 30–37.
- 478 Mitchell, J. B., 2014. *Machine learning methods in chemoinformatics*. Wiley
479 *Interdisciplinary Reviews: Computational Molecular Science* 4 (5), 468–481.
- 480 Moore, B., 1981. Principal component analysis in linear systems: Controllability,
481 observability, and model reduction. *IEEE Transactions on Automatic Control*
482 26 (1), 17–32.
- 483 Ojala, T., Pietikainen, M., Maenpaa, T., 2002. Multiresolution gray-scale and
484 rotation invariant texture classification with local binary patterns. *IEEE*
485 *Transactions on Pattern Analysis and Machine Intelligence* 24 (7), 971–987.
- 486 Salvador, E., Cavallaro, A., Ebrahimi, T., 2004. Cast shadow segmentation using
487 invariant color features. *Computer vision and image understanding* 95 (2),
488 238–259.

- 489 Satti, V., Satya, A., Sharma, S., 2013. An automatic leaf recognition system for
490 plant identification using machine vision technology. *International Journal of*
491 *Engineering Science and Technology (IJEST)* ISSN, 0975-5462.
- 492 Strang, G., 2003. *Introduction to linear algebra*. Wellesley-Cambridge Press,
493 Massachusetts, Fourth Edition.
- 494 Tharwat, A., Gaber, T., Hassanien, A. E., 2014a. *Advanced Machine Learning*
495 *Technologies and Applications: Second International Conference, AMLTA*
496 *2014, Cairo, Egypt, November 28-30, 2014. Proceedings*. Springer Interna-
497 *tional Publishing, Cham, Ch. Cattle Identification Based on Muzzle Images*
498 *Using Gabor Features and SVM Classifier*, pp. 236-247.
499 URL http://dx.doi.org/10.1007/978-3-319-13461-1_23
- 500 Tharwat, A., Gaber, T., Hassanien, A. E., Hassanien, H. A., Tolba, M. F.,
501 2014b. Cattle identification using muzzle print images based on texture fea-
502 tures approach. In: *Proceedings of the 5th International Conference on In-*
503 *novations in Bio-Inspired Computing and Applications, IBICA, June 23-25,*
504 *2014, Ostrava, Czech. Springer*, pp. 217-227.
- 505 Tharwat, A., Gaber, T., Hassanien, A. E., Shahin, M., Refaat, B., 2015. Sift-
506 based arabic sign language recognition system. In: *Afro-European Conference*
507 *for Industrial Advancement*. Vol. 334. Springer, pp. 359-370.
- 508 Tharwat, A., Ibrahim, A., Ali, H., 2012. Personal identification using ear images
509 based on fast and accurate principal component analysis. In: *8th International*
510 *Conference on Informatics and Systems (INFOS)*. IEEE, pp. 56-59.
- 511 Turk, M. A., Pentland, A. P., 1991. Face recognition using eigenfaces. In: *Pro-*
512 *ceedings IEEE Computer Society Conference on Computer Vision and Pattern*
513 *Recognition CVPR'91*. IEEE, pp. 586-591.
- 514 Uluturk, C., Ugur, A., 2012. Recognition of leaves based on morphological fea-
515 tures derived from two half-regions. In: *International Symposium on Innova-*
516 *tions in Intelligent Systems and Applications (INISTA)*. IEEE, pp. 1-4.

- 517 Valliammal, N., Geethalakshmi, S., 2011. Automatic recognition system using
518 preferential image segmentation for leaf and flower images. *An International*
519 *Journal of Computer Science & Engineering (CSEIJ)* 1 (4), 13–25.
- 520 Welling, M., 2005. Fisher linear discriminant analysis. Department of Computer
521 Science, University of Toronto.
- 522 Wu, M. C., Zhang, L., Wang, Z., Christiani, D. C., Lin, X., 2009. Sparse linear
523 discriminant analysis for simultaneous testing for the significance of a gene
524 set/pathway and gene selection. *Bioinformatics* 25 (9), 1145–1151.
- 525 Yang, J., Zhang, D., Frangi, A. F., Yang, J.-y., 2004. Two-dimensional pca: a
526 new approach to appearance-based face representation and recognition. *IEEE*
527 *Transactions on Pattern Analysis and Machine Intelligence* 26 (1), 131–137.
- 528 Ye, J., Janardan, R., Li, Q., 2004. Two-dimensional linear discriminant analysis.
529 In: *Neural Information Processing Systems, NIPS, December 13-18, 2004,*
530 *Vancouver, British Columbia, Canada*]. pp. 1569–1576.
- 531 Ye, J., Xiong, T., 2006. Computational and theoretical analysis of null space
532 and orthogonal linear discriminant analysis. *The Journal of Machine Learning*
533 *Research* 7, 1183–1204.