

# 1 Progressive collapse: past, present, future and beyond

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## 7 **Abstract**

The world has seen a surge in rigorous study efforts on the progressive collapse of structures in the past few decades. These events have led to new standards and provisions in building codes of practice, many of which are still being developed and updated today. Although there have been some excellent reviews covering different aspects of progressive collapse, the sheer volume of research performed in this area in recent years means that highly relevant investigation methods and research findings are not covered by them. To fill this void, this review article aims to provide an up-to-date and comprehensive overview of progressive collapse research on building structures. The review is organised into eight sections that cover: (1) essential background information; (2) prominent collapse cases; (3) progressive collapse typology; (4) design standards; (5) investigation methods; (6) prevention and mitigation strategies; (7) structural types and characteristics that require special consideration; and (8) future research needs. In addition to the fundamental concepts, this review encompasses recent advances, such as employing physics and game engines, and machine learning to study progressive collapse. It also explores the potential future applications of these new concepts in research. Furthermore, the review emphasises recent progress in improving the robustness of timber and modular structures. Therefore, this review provides a crucial resource to acquire a global overview of current state-of-the-art progressive collapse research and future requirements,

making it valuable to both novice and experienced practitioners and researchers.

*Keywords:*

Progressive collapse, disproportionate collapse, robustness, stability, and integrity of structures.

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## 1. Introduction

Amidst the backdrop of climate change and geopolitical tensions, buildings and bridges are becoming increasingly exposed to more frequent and severe extreme events. In this context, the need to design more resilient structures is now well recognised. Extreme events often cause local-initial failures in structures that can propagate to other parts of the structural system through a phenomenon known as progressive collapse. This usually results in a final collapse that is disproportionate to the initial failure. To avoid this situation, there has been a growing interest from the scientific community in studying progressive collapse and how to prevent it [1]. It is arguably one of the most active research areas in the field of structural engineering, as reflected not only by the increasing number of publications on the topic [1], but also by the development of new standards [2] and the inclusion of new provisions addressing it in the next generation of Eurocodes [3, 4].

Progressive collapse, as defined by Starossek, is a mechanism of structural failure initiated with one or a few elements and sequentially spreading throughout the entire structure [5]. Disproportionate collapse refers to the final damage that significantly exceeds the original localised damage [6, 7]. Although in some cases disproportionality has been defined in terms of the initial cause of failure [8, 9], this article evaluates and advocates disproportionality based on the ratio of final to initial damage rather than the magnitude of the initiating event [10]. The interchangeability of "progressive" and "disproportionate" in industry and codes of practice stems from the tendency for progressive collapse to be inherently disproportionate. The General Services Administration (GSA)'s definition

36 of progressive collapse emphasises the need for guidelines that focus on collapse  
37 disproportionality as the main structural concern, necessitating comprehensive  
38 prevention measures [9].

39

40 Robustness, a term employed in design guidelines, denotes the structural  
41 quality of insensitivity to local failure, allowing the structure to endure dam-  
42 age without experiencing significant failure [11]. Collapse resistance, distinct  
43 from robustness, depends on structural and non-structural measures [5]. Ro-  
44 bust structures are collapse-resistant, but not all collapse-resistant structures  
45 are robust. Eurocode EN 1991-1-7 defines robustness as a structure’s ability  
46 to withstand abnormal events without disproportionate damage [10]. In this  
47 paper, robustness is construed as the structure’s capacity to endure deviations  
48 from the original design and initial damage from abnormal structural events,  
49 exclusive of nonstructural measures.

50

51 Various factors contribute to progressive collapse, with abnormal events be-  
52 ing a primary cause. Abnormal events (resulting from fires, natural disasters,  
53 human error, wars, or terrorist attacks) have a low probability but significant  
54 consequences. These events introduce unanticipated dynamic loads, often over-  
55 looked in conventional design processes [5]. Construction, material, and design  
56 flaws are other common causes of progressive collapse. For example, corrosion, a  
57 material flaw, can overload a member or joint, leading to failure and subsequent  
58 collapse of nearby structural components [12]. Design and construction errors  
59 may cause misjudgements to a member’s capacity, causing failure when sub-  
60 jected to design loads. Thus, preventing progressive collapse is, to some extent,  
61 based on the strength of the individual members. However, a comprehensive  
62 design considers the overall interaction among structural elements, ensuring a  
63 thorough understanding and predictability of structural behaviour. The redun-  
64 dancy and ductility of the entire structural system significantly enhances its  
65 resistance to progressive collapse [13].

66

67 Several high-quality review articles have been produced on progressive col-  
 68 lapse in recent years. Some of these reviews have covered general aspects  
 69 [12, 14, 1, 15, 16, 17, 18] or particular types of structure [19, 20, 21], while others  
 70 have focused specifically on experimental studies [22, 23, 24, 25] or computa-  
 71 tional simulations [26, 27]. Although these reviews provide a useful overview of  
 72 different aspects of progressive collapse, the high volume of research performed  
 73 worldwide in this field means that they do not cover highly relevant investiga-  
 74 tion methods and research findings on more modern forms of construction. As  
 75 such, this work aims to complement and build on these existing papers to pro-  
 76 vide an up-to-date and comprehensive introduction to progressive collapse. The  
 77 most relevant studies in this field are critically reviewed to deepen the reader's  
 78 understanding of progressive collapse. Where appropriate, existing review pa-  
 79 pers have been signposted to ensure all areas of this topic are effectively covered.

80  
 81 This article is organised into seven sections. First, Section 2 provides an  
 82 overview of the most well-known cases of progressive collapse, including a very  
 83 recent case and those that have had a marked influence on the advancement of  
 84 knowledge in the field. This is followed by a description of progressive collapse  
 85 typology (Section 3) and a critical review of some of the most relevant stan-  
 86 dards that address the issue of progressive collapse (Section 4). An analysis of  
 87 investigation methods used to study progressive collapse is then presented in  
 88 Section 5. This includes some of the most recent methods, such as the use of  
 89 general-purpose physics and game engines to perform simulations and the use of  
 90 machine learning to predict structural response and assist design. An overview  
 91 of methods for preventing and mitigating progressive collapse is provided in  
 92 Section 6, including the latest trends and new proposals. Section 7 deals with  
 93 structural types and characteristics that require special consideration with re-  
 94 spect to their progressive collapse behaviour. In particular, this section includes  
 95 a comprehensive review of progressive collapse research performed on timber and  
 96 modular structures, which has not been included in any other general review on  
 97 progressive collapse. Finally, section 8 summarises the most significant findings

98 and gaps that require further investigation.

## 99 **2. Historic Events**

100 This section provides a brief overview of prominent progressive collapse in-  
101 cidents, elucidating their conceivable origins and preventative methodologies  
102 capable of mitigating such occurrences. These notable cases of progressive col-  
103 lapse have wielded considerable influence over both scholarly investigations and  
104 structural design standards.

105 The Ronan Point incident in 1968 involved the collapse of a residential tower  
106 after a gas explosion on the 18th floor caused a load-bearing corner panel to  
107 fail, which in turn triggered the progression of collapse to the entire corner of  
108 the building due to the impact loading of falling debris, as shown in Figure  
109 1(a) [28]. The subsequent collapse demonstrated the potential for a small event  
110 to trigger the failure of an entire section of a building. Researchers proposed  
111 that adequate ties between panels could have prevented the progression [29],  
112 leading to the development of progressive collapse Codes of Practice (CoPs) in  
113 the United Kingdom.

114 The Alfred P. Murrah Federal Building in Oklahoma City suffered a pro-  
115 gressive collapse in 1995 due to a truck bomb, leading to the loss of key columns  
116 supporting a transfer girder, shown in Figure 1(b) [30]. The disproportionate  
117 collapse was attributed to a significant portion of the building relying solely on  
118 the girder, emphasising the need for mitigation methods, such as alternative  
119 load paths and enhanced structural reinforcement [29].

120 The Sampoong Department Store collapse in 1995 revealed structural issues  
121 from subpar construction quality control, inappropriate design decisions, and  
122 a lack of supervision [28]. Known problems, including reduced column cross-  
123 sectional areas and increased dead load, were neglected, leading to a collapse  
124 that might have been mitigated with proper attention and action [31].

125 The collapse of the World Trade Centre (WTC) 1 and 2 towers in 2001,  
126 triggered by the impact of hijacked planes, showcased the challenge of halting  
127 the progression of collapse in the face of severe initial damage, as shown in

128 Figure 1(c) [32]. The steel structure’s properties and potential irregularities in  
129 core stiffness could have possibly influenced the collapse, raising questions about  
130 the impact of stiffness irregularities on progressive collapse resistance [29].

131 The Champlain Towers South collapse in 2021 involved a sudden partial  
132 collapse of a condominium in Florida, as shown in Figure 1(d). While the exact  
133 cause is still under investigation, deterioration in concrete and reinforcement  
134 near the pool deck area and drainage issues were noted in re-certification reports  
135 [33]. Adequate waterproofing and retrofitting measures might have prevented  
136 the collapse, highlighting the importance of structural maintenance and safety  
137 measures in ageing buildings.

138 Additionally, Table 1 provides a concise overview of several instances of  
139 progressive collapse, exemplifying the severe consequences of this phenomenon.  
140 The table further states the possible factors contributing to such failures and  
141 highlights the disproportionate nature of their impact. More detailed reviews  
142 of progressive collapse events can be found in [34, 35].

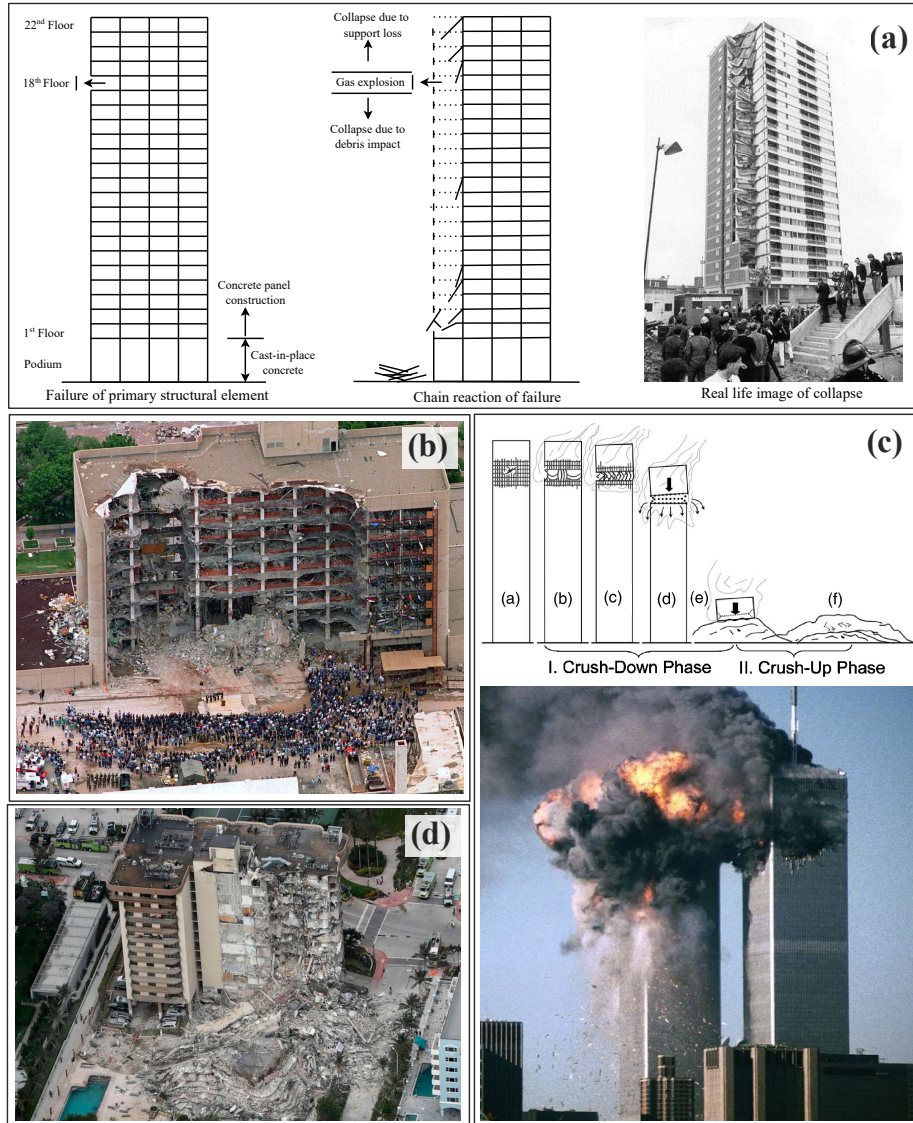


Figure 1: Progressive collapse events: (a) Ronan point collapse sequence, adapted based on [36]; (b) Alfred P. Murrah Building after collapse [37]; (c) Predicted collapse scenario of WTC 1 and 2 [32] and Initial damage endured by WTC Twin Towers [38]; and (d) Champlain Towers South after partial collapse [39].

Table 1: Historic progressive collapse events

| Incident                               | Year | Location                  | Structural system          | No. floor | Triggering Event                | Initial Damage | Final Damage | Disproportionate |
|----------------------------------------|------|---------------------------|----------------------------|-----------|---------------------------------|----------------|--------------|------------------|
| Ronan Point [16]                       | 1968 | London, UK                | Large-panel                | 22        | Gas Explosion                   | Minor          | Partial      | Yes              |
| Skyline Plaza Towers [16]              | 1973 | Fairfax, US               | RC frame                   | 26        | Premature removal of shoring    | Minor          | Partial      | Yes              |
| Hotel New World [16]                   | 1986 | Little India, Singapore   | RC frame                   | 6         | Static Fatigue                  | Minor          | Total        | Yes              |
| L'Ambiance Plaza [16]                  | 1987 | Bridgeport, US            | Steel frame/ Lift-slab     | 16        | Failure of lifting system       | Minor          | Total        | Yes              |
| Alfred P. Murrah Federal Building [16] | 1995 | Oklahoma City, US         | RC frame with shear wall   | 9         | Truck bomb                      | Moderate       | Partial      | Yes              |
| Sampoong Dept Store [16]               | 1995 | Seoul, South Korea        | RC frame                   | 5         | Overload                        | Minor          | Partial      | Yes              |
| Khobar Towers [16]                     | 1996 | Khobar, Saudi Arabia      | Pre-cast concrete building | 8         | Bomb explosion                  | Moderate       | Partial      | No               |
| Pipers Row Car Park [5]                | 1997 | Wolverhampton, UK         | RC frame/ Lift-slab        | 5         | Deterioration, poor maintenance | Minor          | Partial      | Yes              |
| WTC Bldg 1 [16]                        | 2001 | New York, US              | Steel frame                | 110       | Aircraft impact and fire        | Severe         | Total        | No               |
| WTC Bldg 2 [16]                        | 2001 | New York, US              | Steel frame                | 110       | Aircraft impact and fire        | Severe         | Total        | No               |
| WTC Bldg 7 [16]                        | 2001 | New York, US              | Steel frame                | 47        | Debris impact and fire          | Minor          | Total        | Yes              |
| Windsor Tower [16]                     | 2005 | Madrid, Spain             | Steel frame-RC core        | 32        | Fire                            | Moderate       | Partial      | No               |
| I-35 W Bridge [40]                     | 2007 | Minnesota, US             | Steel truss-arched bridge  | -         | Deterioration, poor maintenance | Moderate       | Total        | Yes              |
| Pyne Gould Corporation [16]            | 2011 | Christchurch, New Zealand | RC frame                   | 5         | Earthquake                      | Minor          | Total        | Yes              |
| Rana Plaza [16]                        | 2013 | Savar, Bangladesh         | RC frame                   | 8         | Misuse, overload                | Minor          | Partial      | Yes              |
| Texas Railroad Bridge [5]              | 2013 | Texas, US                 | Wooden trestle bridge      | -         | Fire                            | Moderate       | Total        | Yes              |
| Plasco Building [16]                   | 2017 | Tehran, Iran              | Steel frame                | 17        | Fire                            | Moderate       | Total        | Yes              |
| Surfside, Miami [33]                   | 2021 | Florida, US               | RC frame                   | 12        | Corrosion, poor maintenance     | Minor          | Partial      | Yes              |

### 3. Types of Progressive Collapse

There are different types of progressive collapse. Each type can be characterised depending on the nature of the collapse progression through a structure. The main progressive collapse categories are the pancake, zipper, domino, section, instability, and mix-type [41]. Figure 2 helps to visualise the most common types of progressive collapse. These types are also grouped into broader categories depending on the mechanism behind the type of collapse. For example, pancake- and domino-type collapses can be grouped into the impact category, as they are caused by the sudden dissipation of the potential energy of the failed elements into kinetic energy. Furthermore, zipper and section collapse types can be attributed to the ‘redistribution’ group since they mainly occur due to the redistribution of forces from failed members to other parts of a structure [1]. In this section, the different collapse types, their possible causes, and potential susceptible types of structures will be explored further.

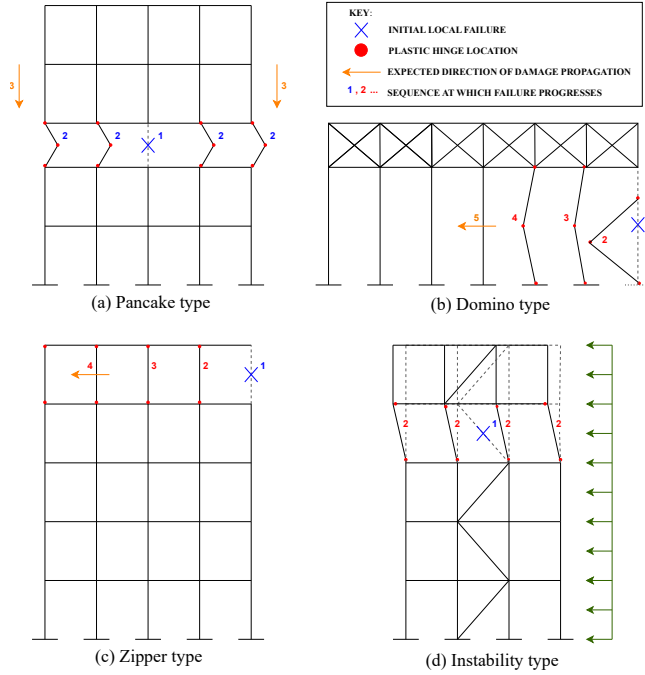


Figure 2: Demonstration of different collapse mechanisms



Figure 3: (a) Pancake collapse of a reinforced concrete structure following an Earthquake in Islamabad, Pakistan [42], (b) Domino collapse of a wooden trestle bridge in Texas, the USA [43], and (c) Pipers Row Car Park partial collapse, Wolverhampton, the UK [44].

### 157 3.1. Pancake Collapse

158 The primary cause of the pancake-type collapse is the loss in vertical load-  
 159 bearing capacity caused by an unusual event, such as a fire or a blast. This  
 160 then causes the failure of members, which consequently starts falling as debris  
 161 on members in lower stories. This debris exerts a high dynamic impact load on  
 162 the stories below, in many cases, subjecting these storeys to loadings estimated  
 163 to be up to four times higher than the static loadings they have been designed  
 164 for, causing their collapse [45]. This type of collapse is prevalent mainly in high-

rise structures. Although many high-rise buildings can be highly redundant and have the ability to develop alternative load paths (ALPs) in case of column loss, they do not have the capability to stop this type of progressive collapse. This is likely attributed to the increase in debris and impact forces with the number of stories in a building.

A prominent example of pancake-type collapse in tall buildings is the collapse of the WTC Twin Towers. Following jet collisions, fires, and initial failures, the resultant debris from the initial failure and subsequent failures possessed a significant amount of kinetic energy that could not have been dissipated without collapsing the storeys below[46]. Pancake-type collapse can occur in low-rise buildings as well. Along with the loss of vertical load-bearing capacity, its primary features include vertical failure propagation and punching shear failures in slabs. Figure 3 (a) shows an example of this type of failure. In order to ensure the efficiency of a building while maintaining its robustness against pancake-type collapses, solutions such as energy absorption devices would potentially be implemented [47]. Refer to Section 6.2.2.3 for more information on this mitigation technique.

### 3.2. Domino Collapse

Domino collapse is another type of impact collapse [48]. In domino collapses, firstly, a member fails due to an initialising event. This failed member then hits a neighbouring member laterally, causing the same overturning failure, which then propagates to neighbouring members. The primary feature that distinguishes domino-type collapse from pancake-type collapse is that the forces that cause this form of collapse, such as gravity, are orthogonal to the direction of failure propagation [5]. However, in pancake collapses, as can be interpreted, failure-inducing forces are parallel to the direction of collapse progression. Due to its mechanism, domino-type collapse occurs mainly in bridges or horizontal structures due to the failure of piers or other slender supporting members [16]. An example of a domino-type collapse is the failure of a wooden trestle railroad

bridge in Texas in 2013. The bridge completely collapsed due to a fire that started in one of the wooden trestles, which then collapsed and impacted nearby members, as shown in Figure 3(b). This type of failure can be prevented by strengthening or retrofitting the members to withstand potentially induced loads from neighbouring member failures.

### 3.3. *Zipper Collapse*

Zipper collapse is one of the most common types of collapse since it can affect most structural arrangements. As mentioned above, zipper collapse is a type of redistribution collapse. This type of collapse occurs when the ALP, which was supposed to carry the load when load redistribution is required due to member failure, also fails [16]. Failure of an ALP can be attributed to the sudden need for dynamic load re-redistribution. Unlike several other collapse types, impact loadings do not typically play a significant role in zipper type collapses. The failure of the top floor of Pipers Row Car Park, UK, in 1997 (shown in Figure 3(c)) can be considered an example of this type of collapse. This failure was initiated as one column punched through the top floor slab. The load was then redistributed to other neighbouring columns, which could not sustain the additional loading and eventually punched through the slab [5, 49]. The most current guidelines, which focus on the use and enhancement of ALPs, aim to prevent this type of failure. Different approaches can be followed to enhance the performance of ALPs; these approaches will be discussed in detail in Section 6.

### 3.4. *Section Collapse*

Section collapse is another type of redistribution collapse that is conceptually similar to zipper collapse. Section collapse, however, can be considered to occur in element sections. An example of this type of collapse can be the failure of a cross section in a tensioned bar. This failure causes further failure in the contiguous parts of the collapsing element due to the inability of the load to be redistributed adequately. Thus, it can be concluded that section collapse does not occur in objects containing structured, independent, but connected units. However, it occurs in single continuous units, such as cables and shells.

225 Due to its abrupt and dependent nature, in many instances, the failure brought  
226 on by this kind of collapse can be described as a quick fracture rather than a  
227 progressive one [5].

### 228 3.5. *Instability Collapse*

229 The failure of components, primarily intended to stabilise a structure, results  
230 in instability-type collapses. One of these components is bracing. For instance,  
231 bracing is necessary for pinned steel frames to ensure a structure’s stability un-  
232 der lateral loading. If the bracing fails, the structure cannot withstand lateral  
233 loading. Instability failures can lead to immediate or progressive disproportion-  
234 ate collapses, depending on the function and location of the damaged element  
235 [5].

### 236 3.6. *Mixed-type Failure*

237 It is uncommon for a structure to experience only one type of collapse in  
238 real-world failures. Therefore, mixed-type collapses predominate [16]. Mini-  
239 mal in-depth research has been conducted to focus on the categorisation and  
240 combination of different collapse types. However, according to Starossek [5], a  
241 famous example of a mixed-type failure is the collapse of Sampoong Superstore  
242 in Seoul. In that structure, the failure began as columns were punched through  
243 the slabs, and when the load was redistributed, the failure spread horizontally  
244 to other columns, inducing zipper-type collapse. This caused a loss of vertical  
245 load-bearing capacity in the slabs, which caused pancake collapse.

246  
247 Another example of this type of collapse is the Alfred P. Murrah Building, USA,  
248 in 1995 (refer to section 2 for more details). In that building, the prevalent type  
249 of collapse was pancake collapse, which occurred due to the loss of vertical load-  
250 bearing capacity as the columns and, subsequently, the girders were damaged.  
251 Investigating the remains of the building also indicated that a domino-type col-  
252 lapse might have occurred. The columns may have been subjected to lateral  
253 forces from the initial detonation, which could have caused overturning forces

254 and partially caused the columns to collide laterally.

255

256 Finally, another example of a structure that underwent a mixed-type collapse  
257 is WTC 7. To date, the exact cause of the failure of WTC 7 is still being  
258 studied. However, based on the evidence gathered by the National Institute  
259 of Standards and Technology (NIST) [50], the most likely cause of failure is  
260 thermal expansion, which may have caused a girder to slide off the column it  
261 was resting on. This then led to the pancake failure of the floor area that was  
262 supported by that girder. Furthermore, it led to the loss of lateral support and  
263 buckling in the column that the girder was restraining. This resulted in the  
264 redistribution of the loads to other members, which had extremely large spans,  
265 leading to their failure in a zipper-type collapse. A combination of the two  
266 collapses spread throughout the building, causing it to collapse completely in  
267 seconds.

### 268 3.7. Summary

269 From studying the various failure cases, it can be concluded that the pro-  
270 gression of vertical failure is mainly attributed to pancake-type collapse. In  
271 contrast, horizontal progression is mainly caused by zipper-type and domino-  
272 type collapses. The most challenging issue in mixed-type failures is that a  
273 mitigation technique for one collapse can increase a building’s susceptibility to  
274 other collapse types. This issue will be discussed further in later sections. Table  
275 2 summarises the most common collapse types and their possible mitigation  
276 techniques.

## 277 4. Codes of Practice and Design Guidelines

278 In building design, addressing progressive collapse is a relatively novel con-  
279 cept. Thus, only a few CoPs explicitly provide guidance on how to design  
280 against progressive collapse. Mainly, CoPs follow either a threat-dependent or  
281 a threat-independent approach. The choice of approach depends on various fac-  
282 tors, including engineering judgement, economic considerations, and the nature

Table 2: Summary of most common progressive collapse types

| Collapse Type | Example                                                                                                  | Possible Mitigation/Prevention Techniques                                                                                           |
|---------------|----------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------|
| Pancake       | -WTC Twin Towers (2001)<br>-Sampoong Department Store (1995)<br>-Alfred P. Murrah (1995)<br>-WTC7 (2001) | Energy absorption devices to be applied to ensure impact from pancaking does not cause further vertical collapse propagation        |
| Domino        | -Wooden Trestle Railroad Bridge, Texas (2013)<br>-Alfred P. Murrah (1995)                                | Retrofitting members to withstand loading along minor axes                                                                          |
| Zipper        | - Sampoong Department Store (1995)<br>-WTC7 (2001)                                                       | -Ensuring ALPs are well designed<br>-Proper detailing at column-slab connections to ensure the prevention of punching shear failure |

of the proposed structure. Some of the most commonly adopted current codes within Europe and overseas, as well as their adopted design approaches, will be reviewed and discussed in this section. These codes are: Eurocode EN:1991-1-7 [10], General Services Administration (GSA) Alternative Path Analysis & Design Guidelines for Progressive Collapse Resistance 2016 [9], United Facilities Criteria (UFC) UFC 4-023-03 [6] and the American Society of Civil Engineers (ASCE) ASCE 76-23 [8]. The readers are referred to Adam et al. [1] for a summary of the progressive collapse prevention methods proposed in several other international design standards and guidance documents.

#### 4.1. Types of Approaches

Design standards employ threat-dependent and threat-independent approaches, as discussed in this section.

#### 295 4.1.1. *Threat-dependent Approach*

296 A threat-dependent approach mainly depends on designing a structure to be  
297 collapse-resistant to a specific threat [16]. This technique is particularly useful  
298 in cases where the elements of a building are at high risk from certain known  
299 events. An example is a highway bridge or a building constructed close to a  
300 highway. In both types of structure, there is a very significant risk that the  
301 columns or piers, in the former case, may be struck by a fast-moving vehicle  
302 in the event of a highway accident. In such cases, it must be ensured that, for  
303 example, these incidents do not lead to a progressive collapse of the structure.  
304 Generally, most CoPs require consideration of events whose occurrence can be  
305 predicted and characterised, such as fires, earthquakes, and impacts. In the  
306 following sections, steps on how to achieve this will be described as per the  
307 directives from the various CoPs.

#### 308 4.1.2. *Threat-independent Approach*

309 Contrary to the threat-dependent approach, the threat-independent approach  
310 is not based on a specific event. The threat-independent method seeks to design  
311 a structure with improved strength, ductility, and redundancy levels to prevent  
312 progressive collapse under many undetermined risk scenarios [51]. Moreover,  
313 IStructE's Manual for Systematic Risk Assessment (2013) [52], for example,  
314 proposes adopting a threat-independent design approach as the main risk miti-  
315 gation technique in a structure. This approach can be effective for several other  
316 hazards, and it can help decrease the sensitivity of the design to underlying as-  
317 sumptions usually made in an initial risk assessment. This decreased sensitivity  
318 comes from minimising the presence of what it refers to as 'cliff edges' in the  
319 structural response. In other words, it no longer matters whether the loads are  
320 slightly higher than what was assumed in the design or if the strength is slightly  
321 lower. Thus, the 'cliff edge' defined by the ultimate capacity has been elim-  
322 inated. Furthermore, several CoPs also guide following a threat-independent  
323 approach against progressive collapse design [53, 11, 52, 6, 9, 54].

## 324 4.2. Design Approaches

325 This section will discuss the design approaches most commonly incorporated  
326 within progressive collapse CoPs. The main techniques that will be examined  
327 include key element design, alternative load path methods, and prescriptive  
328 tie requirements. In further sections, the application of those approaches to  
329 building CoPs will be discussed.

### 330 4.2.1. Key Element Design

331 Key element design is a threat-dependent approach applied through locally  
332 strengthening elements. This method aims to reduce the probability of initial  
333 local failure rather than mitigating collapse propagation. In this method, key el-  
334 ements in a structure and their supporting members are designed to withstand  
335 the general minimum prescribed loadings or loadings from certain identified  
336 events, such as the impact of a vehicle or an explosion. A key element can be  
337 defined as an element whose failure leads to the collapse of a ‘significant area’ of a  
338 structure [11]. That ‘significant area’ and the loading that should be considered  
339 are defined differently in various CoPs. In a structure where several elements are  
340 considered key elements, ensuring their collapse-resistant design can be very un-  
341 economic. Additionally, disregarding strengthening other elements makes them  
342 more vulnerable to potential attacks, even though their structural significance  
343 might be less. Thus, to ensure that the benefits of key element design are op-  
344 timised, this method should be used in conjunction with other global methods,  
345 such as incorporating ties and other redundancy measures. This will ensure the  
346 robustness of a structure under various threat scenarios.

### 347 4.2.2. Alternative Load Path Method

348 ALPs can be described as paths in a structure through which loads can be  
349 redistributed after loss of an element, enabling the structure to bridge local  
350 failure [56], as illustrated in Figure 4. Moreover, according to Starossek and  
351 Wolff [30], the ability of a structure to develop ALPs can be used as a measure  
352 of its redundancy. Several CoPs highly depend on developing ALPs as the main  
353 progressive collapse mitigation technique [9, 8]. To ensure the effectiveness of

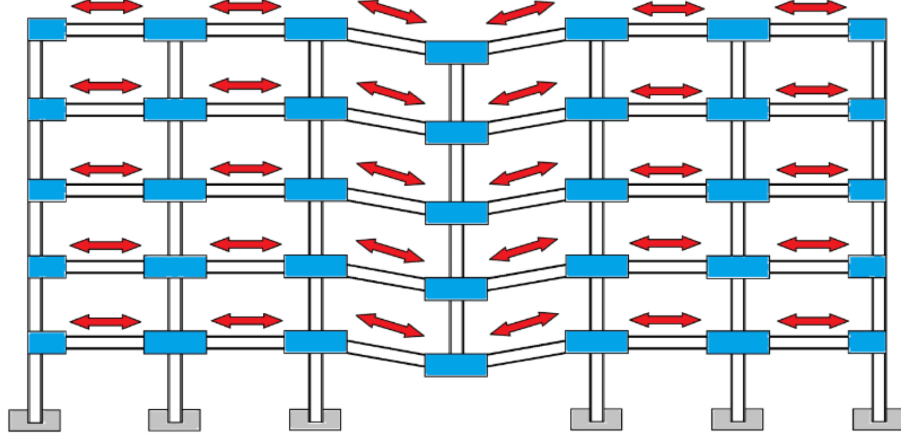


Figure 4: Load redistribution by alternative load paths (ALPs) under column loss scenario at the catenary stage [55]

354 this method, the adequacy of ALPs under additional, potentially redistributed  
 355 loads should be considered. To investigate this, detailed analyses should be  
 356 performed to help understand the behaviour of a structure following the loss of  
 357 various load-bearing elements. In structural design, the development of ALPs  
 358 can be enhanced by means of structural ties, strength, and ductility [1]. The  
 359 incorporation of ties will be further discussed in the following section. Due  
 360 to the fact that the ALP method depends on enhancing a structure's overall  
 361 robustness and collapse resistance, it can be considered a threat-independent  
 362 approach. Other means of enhancing alternative load paths can be considered  
 363 in the original structural layout design process. An effective structural form or  
 364 arrangement, in the form of a regular floor layout, for example, can help in the  
 365 efficient and inherent incorporation of ALPs into a structure [8].

#### 366 4.2.3. Prescriptive Tie Requirements

367 For ALPs to develop, continuity must be ensured in a structure. The incor-  
 368 poration of ties is one of the main methods through which continuity can be  
 369 achieved. In the partial collapse of Ronan Point, the structural panels adjacent  
 370 to the explosion location were not strong enough to withstand the resulting pres-  
 371 sure. However, the main issue is that the building was not redundant enough,

372 i.e., it could not develop ALPs. This was because appropriate tying did not exist  
 373 between the precast concrete panels [57]. In addition to having enough tying  
 374 (continuity) between elements in a structure, the structural members should  
 375 also be able to develop tie forces for an ALP to fully develop [58]. Ties are  
 376 link members embedded within a structure. One of the main functions of ties  
 377 is to ensure that the elements of a structural system do not undergo excessive  
 378 displacements in extreme events, thus preventing the elements from reaching  
 379 their rotation or strain limits and failing. This helps to ensure that load redis-  
 380 tribution can still occur throughout a structure [11]. Several design guidelines  
 381 propose prescriptive tie-force requirements [11, 10]. Therefore, the tie elements  
 382 designed using these guidelines will be based on uniform predetermined require-  
 383 ments rather than those determined based on the demand of a system identified  
 384 following detailed structural analysis procedures.

385  
 386 According to Mann et al. [11], the types of ties include peripheral, internal,  
 387 horizontal, and vertical. Peripheral ties are located on the exterior of a structure  
 388 since they are arguably the most vulnerable part of it in terms of external  
 389 threats. All peripheral ties should be connected to internal ones for anchoring  
 390 purposes. Moreover, internal ties are expected to form straight lines across  
 391 the structure in two orthogonal directions. Internal ties should be designed  
 392 with high ductility levels to ensure maximum benefit utilisation. To address  
 393 the possibility of walls or columns being pushed outwards, following an internal  
 394 blast, for example, walls and columns should be tied back to the main structure  
 395 using horizontal ties. Finally, vertical ties should exist between vertical elements  
 396 to help identify a clear line of load transfer [11]. Figure 5 shows the different  
 397 types of ties recommended for an in-situ concrete structure. Different CoPs have  
 398 unique guidelines for tie requirements for different types of buildings. However,  
 399 continuity might not be considered a positive aspect in all cases. This is because  
 400 it can lead to further collapse as loads from members that fail get redistributed  
 401 to others that cannot withstand all the additional loading on them [5]. Thus,  
 402 the concept of continuity can be implemented with segmentation to help prevent

collapse from progressing to further sections of a structure. Segmentation will  
be discussed in depth in Section 6.2.2.1.

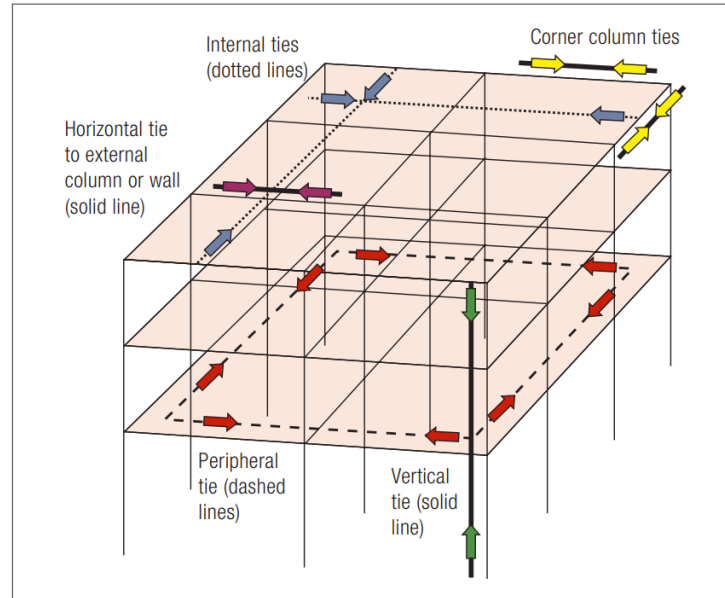


Figure 5: Types of ties in reinforced concrete structures [11]

#### 4.3. Eurocodes (EN:1991-1-7) [10]

After the Ronan Point incident in 1968, the UK started incorporating design guidance against progressive collapse in the British Code of Practice 110 issued in 1972 (CP 110: Part 1: 1972 [59]). This code was one of the earliest national CoPs to provide guidance for progressive collapse resistance design [15]. This document was then followed by the Building Regulations Approved Document A, which was first published in 1992 [60]. Similarly, the Eurocodes also started incorporating progressive collapse design in various versions, of which the latest, Eurocode 1-Actions on structures-Part 1-7: General actions-Accidental actions (EN:1991-1-7) last amended in 2014, incorporating guidance from the British codes as well. This section will discuss the guidance in EN:1991-1-7 regarding progressive collapse.

417

418 In its design guidance, EN:1991-1-7 implements both threat-dependent and  
419 independent approaches. Some of the methods adopted by the Eurocode include  
420 key element design and the incorporation of ties and redundancy to ensure the  
421 ability to develop ALPs. The mitigation and prevention methods that need  
422 to be adopted in the design of a structure depend on its consequence class.  
423 Consequence classes are risk categories that help determine the criticality of a  
424 building based on its size and purpose. Four main consequence classes are de-  
425 fined in EN:1991-1-7: Consequence Class (CC) 1, 2A, 2B and 3. For example,  
426 smaller structures, such as residential buildings not exceeding four stories, lie  
427 within CC 2A. Effective horizontal ties or anchorage of floors to walls should be  
428 provided for such buildings. Larger structures, such as buildings exceeding 15  
429 stories, are classified under CC3. For this category, a systemic risk assessment  
430 should be undertaken to provide an understanding of the foreseeable and unfore-  
431 seeable hazards and, therefore, design the structure accordingly. It is important  
432 to note that EN:1991-1-7 provides prescriptive guidance for tie incorporation in  
433 different types of structures. Finally, although this Eurocode does not specify  
434 acceptable analysis methods for progressive collapse investigations, it guides the  
435 loadings that should be considered for several identified threats. For example,  
436 recommended design loads are provided for scenarios such as vehicular impact  
437 from a highway and ship impact from a waterway.

#### 438 4.3.1. Discussion

439 The Eurocodes provide a set of general requirements for progressive col-  
440 lapse design. Following these guidelines alone might, however, be considered  
441 insufficient for erecting structures that can be considered adequately ‘collapse  
442 resistant’. This can be attributed to the fact that rigorous design and analy-  
443 sis procedures are not proposed by the code. For example, the code does not  
444 clearly state the requirement of certain types of analysis procedures for higher-  
445 risk structures, such as Consequence Class 3 buildings. Moreover, although  
446 guidance is provided for estimating dynamic impact loads or an equivalent static  
447 load for various scenarios, a comprehensive method for ensuring that all relevant

dynamic effects are accounted for is not included.

Additionally, the code emphasises the importance of having adequate tying within all the structure, sufficient levels of ductility and continuity between members to ensure the activation of ALPs as a measure of robustness for the structure. However, this does not consider modern research claiming that having high levels of continuity in a structure can lead to further collapse progression [30]. Furthermore, since different types of buildings are more susceptible to certain types of collapse (e.g. tall buildings can be more susceptible to pancake rather than domino-type collapse), the mitigation technique utilised in a structure should address its expected collapse type.

Some initial recommendations for the enhancement of this current code include:

- Dynamic amplification factors can be implemented when following static analyses to generally consider the dynamic effect of loading typically associated with progressive collapse.
- The concept of segmentation can be applied by either having stiffer or weaker elements in the structure to isolate collapse within segment boundaries, ensuring that damage does not further propagate to other areas in a structure.
- Comprehensive design recommendations for higher-risk structures should be outlined.
- Acceptable analysis methods and their applications should be identified.
- The notional accidental load of 34 kPa recommended for use in key element design is not appropriate for most accidental design situations. More specific guidance should be provided in this regard.
- Prescriptive rules for designing continuity reinforcement should be updated to account for research findings of the past decade (such as [3, 4]).

It is important to note that the next generation of the Eurocodes aims to address some of the acknowledged gaps of the current code. Examples include

potentially updating the current prescriptive tie methods and incorporating segmentation as a robustness measure [3, 4].

#### 4.4. GSA (*Alternative Path Analysis & Design Guidelines for Progressive Collapse Resistance 2016*) [9]

The GSA 2016 progressive collapse guidelines could be considered a combination of the different CoPs historically used in the USA, including the Department of Defence (DoD), Unified Facilities Criteria (UFC) and the Interagency Security Committee (ISC) guidelines. The main aim of this document is to bring alignment within the industry by reducing discrepancies between previous guidelines. The GSA guidelines follow a threat-independent approach, which focuses on limiting the progression of initial damage in a structure mainly through ensuring the development of ALPs and redundancy but does not explicitly consider the cause of initial failure. This is assessed by analysing the effect of various load bearing elements' removal scenarios. This document mainly applies to all new GSA construction and Federal buildings undergoing major structural renovation.

The GSA categorises structures into different facility security levels (FSLs). The design procedures and analysis methods to be adopted in the progressive collapse design of a structure depend on its FSLs. FSLs are determined based on security/ risk related factors such as target attractiveness, value and criticality. Given that, FSLs are usually determined by specialist bodies. Unlike the Eurocodes, the GSA provides detailed guidance on the acceptable analysis methods that can be adopted by design engineers in progressive collapse investigations. The applicability of an analysis method depends on a structure's regularity, Demand Capacity Ratio (DCR) and number of stories. The analysis methods proposed in this code are linear static, nonlinear static, and nonlinear dynamic analyses. Linear static analyses are more applicable to regular structures not exceeding 10 stories. For irregular structures above 10 stories, non-linear dynamic analyses could be adopted. Following the analysis process, various column removal scenarios are considered. The performance of a structure is assessed based on certain acceptance criteria. These acceptance criteria

are mainly adapted from the Life Safety and Collapse Prevention limits defined by ASCE 41-06 for seismic design. Adopting these criteria ensures a structure’s collapse resistance rather than direct habitability to provide safety while maintaining an economical design.

#### 4.4.1. Discussion

The GSA guidelines provide detailed procedures for designing against progressive collapse. The main aim of the guideline is to ensure the development of ALPs under various member removal scenarios. Interestingly, prescriptive tie force requirements were included in previous versions of the GSA guidelines. However, these prescriptive rules have been completely removed in the latest version. In the current guidance, each structure is analysed in detail, and the performance is assessed based on a set of criteria to ensure the adequacy of the design. Although these guidelines might be considered one of the most rigorous [12], they still have some drawbacks.

Some drawbacks include that not all the initial damage caused by the original cause of element failure is considered [61]. For example, if a bomb exploded near a structure, which led to a column loss, it might also damage other areas of the structure, which can significantly reduce its capacity. However, the GSA guidelines only consider the impact of column loss on structural integrity.

Another issue that can be considered in the GSA guidelines is that it depends only on one technique, which is the development of ALPs. In certain structures (e.g. tall structures with large spans), developing ALPs without having any element failure can lead to designing overly conservative, uneconomic structures. Thus, implementing additional collapse prevention methods with ALPs, including segmentation [5] and energy absorption devices [47], can provide more economical and practical solutions.

#### 535 4.5. UFC (4-023-03) [6]

536 The UFC progressive collapse guidelines are mainly aimed towards the de-  
537 sign of structures that the DoD of the USA personnel will occupy. In these  
538 guidelines, both direct and indirect, as well as threat-dependent and indepen-  
539 dent design approaches, are adopted. The alternative path method and the  
540 enhanced local resistance (ELR) methods are considered for direct design ap-  
541 proaches. As with the GSA, the main aim of the alternative path method is  
542 to ensure that a structure is capable of bridging over local failure. Moreover,  
543 ELR refers to the local strengthening of elements to ensure sufficient strength  
544 for a structure to resist a specific threat. In terms of indirect design approaches,  
545 general minimum levels of strength, continuity and ductility are to be adopted.  
546 In the UFC, this can be achieved by the prescribed tie recommendations.

547  
548 Like the Eurocode and GSA, the UFC groups buildings into different risk  
549 categories based on a structure's occupancy level and function or criticality.  
550 A structure's risk category determines the acceptable mitigation techniques  
551 that can be applied in its design process. Where adopting the alternative path  
552 method is allowable, a detailed analysis assessing the performance of the struc-  
553 ture following a vertical load-bearing element loss should be undergone. More-  
554 over, similar to the GSA, three main acceptable analysis methods exist: linear  
555 static, nonlinear static and nonlinear dynamic methods. The performance of  
556 the structure is then assessed based on the acceptance criteria adopted from  
557 ASCE 41 [62].

##### 558 4.5.1. Discussion

559 The UFC adopts various design approaches with their applicability depen-  
560 dent on a structure's risk category and the designer's judgement. For example,  
561 for a lower risk category, such as RC II, designers can adopt ties and ELR or  
562 alternative path design. Such options help ensure that lower risk structures  
563 are designed safely and efficiently since only the methods more suitable to the  
564 considered structural arrangement can be adopted. As with the GSA, in terms

565 of the alternative path assessment method adopted in this code, the loss of  
566 a single vertical load-bearing element should be considered at a time. As dis-  
567 cussed previously, this excludes various initial local damage scenarios that could  
568 potentially affect the resulting behaviour of a structure.

#### 569 4.6. ASCE (76-23) [8]

570 ASCE's primary code for design against disproportionate collapse is ASCE  
571 76-23. This code adopts guidance from various existing CoPs, including GSA  
572 2016 [9], UFC 4-023-03 [6] and EN:1991-1-7 [10]. Moreover, this standard  
573 addresses the design of new and existing buildings. In ASCE 76-23, threat-  
574 independent and threat-dependent methodologies are considered, in addition  
575 to direct and indirect design approaches. Similar to the GSA 2016 code, this  
576 standard adopts the alternative load path method to determine the robustness  
577 of a structure. Despite the similarities, there are several differences, which are  
578 outlined in this section.

579  
580 Similar to the GSA and the Eurocode guidance, ASCE 76-23 proposes clas-  
581 sifying buildings into different Collapse-Resistant Design Categories (CRDCs),  
582 CRDCs A, B, C and D. These categories are assigned following a risk assessment  
583 procedure which considers the likelihood of a hazard, vulnerability of the struc-  
584 ture, the consequences associated with the risk and the building risk category  
585 (determined according to ASCE 7-16 [63]). The acceptable approach to be fol-  
586 lowed in the design process, whether hazard-independent or hazard-dependent,  
587 depends on the CRDC of the structure. If a threat-independent design proce-  
588 dure is followed, different Hazard-Independent Damage Scenarios (HIDS) should  
589 be applied to a structure to assess its performance. In the analysis process, a  
590 different suite of HIDSs should be considered for each CRDC, as defined by the  
591 code. The main aim of the analysis process in this code is to ensure the ability  
592 of a structure to develop ALPs. Like the GSA, the approved analysis methods  
593 are the linear static, nonlinear static and nonlinear dynamic procedures. Linear  
594 static procedures can be adopted for structures that meet the regularity require-

595 ments. Irregular structures that do not meet certain DCR requirements should  
596 adopt the nonlinear static or dynamic procedure.

597

598 The acceptable damage to a structure is then determined based on a struc-  
599 ture's CRDC and the considered HIDS. In this code, this is assessed based on  
600 acceptance and performance criteria. The acceptance criteria adopted in this  
601 code are similar to those adopted in the GSA code. In terms of the performance  
602 criteria, the overall performance of a structure is assessed rather than focusing  
603 on individual elements. It is interesting to note that, in this code, partial col-  
604 lapse is acceptable. However, when determined, the impact of debris loading on  
605 the structure should be considered when evaluating the extent of failure.

606

#### 607 4.6.1. Discussion

608 ASCE 76-23 addresses various shortcomings of previous CoPs. For example,  
609 instead of having specified element removal scenarios, this code provides damage  
610 volumes to be applied to structures. Additionally, for CRDC D, multi-column  
611 removal scenarios or an equivalent damage volume should be considered follow-  
612 ing the defined HIDS. These recommendations provide a better representation  
613 of the initial damage that a structure may have sustained from a potential trig-  
614 gering event in real-life situations. Moreover, this code follows a more robust,  
615 systematic way in terms of risk categorisation, considering various aspects of a  
616 structural system considering both factors relevant to a potential hazard and  
617 a building's properties. In terms of recommendations, similar to the GSA, one  
618 issue with this code is the high dependence on the development of ALPs. As  
619 mentioned previously, this could have negative implications on taller buildings  
620 or buildings of larger spans. Although this code briefly discussed segmenta-  
621 tion, detailed recommendations for its potential applications have not yet been  
622 covered. Similarly, this code recommends undergoing an analysis for debris im-  
623 pact in cases where partial collapse is permitted. However, guidance on how to  
624 analyse debris impact has not been provided.

#### 625 4.7. Codes Comparison and Summary

626 Generally, three main design approaches are adopted in current international  
627 disproportionate collapse codes. As discussed previously, these approaches are  
628 key element design (local strengthening), alternative load path method and  
629 prescriptive tie recommendations. Each of the different codes discussed adopts  
630 some or all of these approaches. As noted, a very high similarity is observed be-  
631 tween the analysis and performance assessment methods adopted in GSA 2016,  
632 UFC 4-023-03 and ASCE 76-23. This is because these three codes adopt this  
633 guidance from ASCE 41's seismic performance recommendations.

634

635 Moreover, as can be concluded from this section, there are still gaps in  
636 the guidelines provided by all the discussed codes in terms of disproportionate  
637 collapse. Table 3 provides a summary and comparison between the discussed  
638 CoPs' approaches to progressive collapse design. Furthermore, to address some  
639 of the CoPs' gaps and issues highlighted within this section, Section 6.3 proposes  
640 a framework for progressive collapse design that satisfies current code guidance  
641 while incorporating proposals from the literature, which will be explored in  
642 Section 6.

Table 3: Comparison between the Eurocode, GSA, UFC, and ASCE disproportionate collapse guidance

| Code                                                              | EN:1991-1-7 [10]                                                                                                                                                                                                                                  | GSA 2016 [9]                                                                                                                                                                                                                               | UFC 4-023-03 [6]                                                                                                                                                                                                                           | ASCE 76-23 [8]                                                                                                                                                                                                                             |
|-------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Type of Approach                                                  | Threat dependent and independent                                                                                                                                                                                                                  | Threat independent                                                                                                                                                                                                                         | Threat dependent and independent                                                                                                                                                                                                           | Threat dependent and independent                                                                                                                                                                                                           |
| Risk Categories                                                   | Consequence classes: 1, 2A, 2B and 3                                                                                                                                                                                                              | Facility security level (FSL): I, II, III, IV and V                                                                                                                                                                                        | Risk Category (RC): I, II, III and IV                                                                                                                                                                                                      | Collapse-Resistance Design Category (CRDC): A, B, C and D                                                                                                                                                                                  |
| Ties                                                              | Vertical, horizontal, internal and perimeter ties                                                                                                                                                                                                 | No specific guidance provided                                                                                                                                                                                                              | Vertical and horizontal ties                                                                                                                                                                                                               | No specific guidance provided                                                                                                                                                                                                              |
| Acceptable Damage Progression Area                                | 100 m <sup>2</sup> or 15% of floor area, whichever smaller, in any two adjacent stories                                                                                                                                                           | -15% of the floor area for exterior column removal<br>-30% of the floor area for internal column removal                                                                                                                                   | No damage to the floor is allowed                                                                                                                                                                                                          | Acceptable damage area is determined based on a structure's CRDC and considered HIDS                                                                                                                                                       |
| Key Element Design                                                | Key elements to be designed to sustain a load of 34 kN/m <sup>2</sup> in any direction                                                                                                                                                            | NA                                                                                                                                                                                                                                         | Enhanced Local Resistance can be used as a design approach for RC II, III and IV                                                                                                                                                           | Local Strengthening could be implemented to reduce the consequences of an identified hazard                                                                                                                                                |
| ALP                                                               | Incorporated through general robustness and ductility measures                                                                                                                                                                                    | Considered the main collapse prevention method applied in the GSA code; their formation is ensured by analysing different column removal scenarios                                                                                         | Alternative Path method can be used as a design approach for RC II, III and IV                                                                                                                                                             | Considered the main collapse prevention method applied in the ASCE code; their formation is ensured by analysing different damage volume scenarios                                                                                         |
| Column Removal Scenario Requirement for Threat Independent Design | Notional removal of each column or each beam supporting a column one at a time at each storey of the building (columns within a plan diameter of 2.25H are to be removed simultaneously; where H is the inter-storey height of the columns [11]). | Different internal and external load-bearing elements removal scenarios should be considered. Generally, a single element removal should be considered at a time.                                                                          | For the Alternative Path approach, Column/ load-bearing wall removal locations are determined based on a structure's RC. Generally, a single element removal should be considered at a time.                                               | Initial damage is applied in the form of notional damage volume defined based on a considered HIDS. For each CRDC, a suite of HIDS should be applied to a structure.                                                                       |
| Accidental Loading Calculation                                    | -An equivalent static load can be acquired for several dynamic sources from tables in the code<br>-A dynamic load can be calculated for impact cases from Annex C of EN:1991-1-7.                                                                 | In the static analyses, dynamic loading is accounted for using amplification factors applied to the proposed load combinations.                                                                                                            | In the static analyses, dynamic loading is accounted for using amplification factors applied to the proposed load combinations.                                                                                                            | In the static analyses, dynamic loading is accounted for using amplification factors applied to the proposed load combinations.                                                                                                            |
| Acceptance Criteria                                               | NA                                                                                                                                                                                                                                                | Elements are classified into deformation-controlled and force-controlled. For each type of analysis (linear static, non-linear static or non-linear dynamic), different acceptance criteria are available for the different element types. | Elements are classified into deformation-controlled and force-controlled. For each type of analysis (linear static, non-linear static or non-linear dynamic), different acceptance criteria are available for the different element types. | Elements are classified into deformation-controlled and force-controlled. For each type of analysis (linear static, non-linear static or non-linear dynamic), different acceptance criteria are available for the different element types. |

## 643 5. Investigation Methods

644 Three main methods are used for structural purposes to analyse problems:  
645 analytical, numerical, and experimental. Analytical methods aim to find ex-  
646 act solutions to a problem, which can be difficult to achieve in more complex  
647 problems. In such cases, numerical methods offer approximate solutions with  
648 reasonable precision. The benchmark for most currently used numerical and  
649 analytical methods is usually experimental. Experimental analysis helps to rep-  
650 resent real-life conditions in lab-controlled situations, providing a better under-  
651 standing of the various factors that affect a structure. This section discusses  
652 these three analysis methods and their applications in the study of progressive  
653 collapse.

### 654 5.1. Numerical Methods

655 Numerical methods are used to ensure time and resource efficiency by util-  
656 ising computation. The approach depends on the method and software package  
657 used, the level of understanding required and the problem size. Typically, multi-  
658 physics packages are used in civil engineering. Moreover, open-source game en-  
659 gines offer rapid animation and approximate behaviour for objects, making them  
660 potentially useful in progressive collapse studies. Hence, this section discusses  
661 the multi-physics engineering packages and game engines separately.

#### 662 5.1.1. Structural and Multi-Physics Engineering Packages

663 For multi-physics engineering packages, the most widely adopted methods  
664 are the finite element method (FEM) and the discrete element method (DEM).  
665 Additionally, the applied element method (AEM), a hybrid between continuum  
666 and discrete methods, has recently gained traction in civil engineering appli-  
667 cations, as this simplifies the complexity and overcomes the drawbacks of con-  
668 tinuum and discrete element approaches. Moreover, each method has its own  
669 structural and computational idealisations behind it. Currently, in an attempt  
670 to overcome issues associated with each approach, some commercial software  
671 have been updated to incorporate more than one numerical approach.

672

673 The amount of complexity and modelling strategy used in a numerical model  
674 should be considered depending on the goal of the research and the available re-  
675 sources. Micro- and macro-modelling are the main techniques typically adopted  
676 in numerical models. Micromodels are models with a high level of detail that  
677 aim to mimic real structures. However, this approach is not feasible to study  
678 the global behaviour of large structural systems due to the significant compu-  
679 tational resources required [1]. On the other hand, macro models implement  
680 simplifications to represent the collapse behaviour of whole structures.

681  
682 Figure 6 summarises the main features of each numerical method, followed  
683 by a summary of the numerical methods in this section. An in-depth review and  
684 discussion of the progressive collapse studies conducted using these methods can  
685 be found in [1, 64].

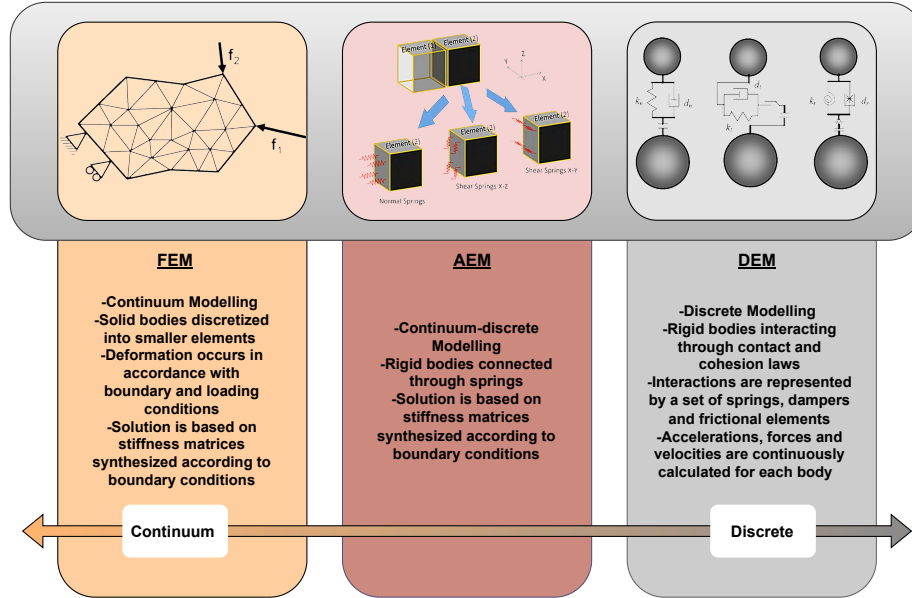


Figure 6: Main features of commonly adopted numerical methods in progressive collapse studies. Figures adapted from [65], [66] and [67]

#### 686 5.1.1.1 Finite Element Method

687 FEM is a type of continuum modelling which assumes a structure is divided  
688 into smaller analysis units connected at nodes [68]. Due to its nature, FEM  
689 can generally be considered reliable from stages of initial loading to non-linear  
690 deformations. However, it can be challenging to use for modelling separation,  
691 failure, falling and collision [51, 69]. What makes FEM a very versatile and  
692 widely adopted analysis method is that it can be used for a wide array of in-  
693 vestigations: macro- or micro-models [1]; explicit [70, 41] or implicit [71] cal-  
694 culations; linear and nonlinear analyses; static or dynamic behaviour; 2D or  
695 3D models; and for different types of structure. Some of the most used soft-  
696 ware packages that incorporate Finite Element (FE) Analysis and have been  
697 used in progressive collapse analysis include ABAQUS [72, 73, 16, 1], ANSYS  
698 [74, 75, 76], LS-DYNA [70, 64, 61, 77] and OpenSEES [78, 79, 80].

699  
700 Several researchers incorporated methods such as material erosion [64] and  
701 fibre discretisation [81, 82] within their FE studies to provide better represen-  
702 tations of aspects such as material failure and rebar interaction. Moreover,  
703 typically, researchers introduce idealisations and simplifications to their FE  
704 models to ensure optimised computation demand levels. For example, most  
705 of the research conducted thus far on entire structures has included simplifica-  
706 tions, including modelling RC structures using similar shell and frame elements  
707 [83, 84, 85, 41]. Although this might introduce more sources of deviation and  
708 uncertainty to a model, it can still provide reliable results when done adequately,  
709 as demonstrated by comparisons with experimental results.

#### 710 5.1.1.2 Discrete Element Method

711 The discrete element method is based on the concept that a modelled object  
712 is divided into smaller rigid bodies. These rigid bodies can interact through  
713 springs, dampers, and frictional elements, where the solutions are obtained by  
714 solving equilibrium and compatibility conditions [67]. DEM is particularly use-

ful in modelling granular materials or engineering structures where large deformations and separations occur at a pre-existing interface. Unlike FEM, the discrete element method has the ability to model failure and collapse.

718

The main issue with using DEM is that it requires very high computational resources. However, technological advances made it possible to introduce progressive collapse analysis into DEM [86, 87, 88]. DEM can be combined with FEA to provide a complete structure analysis from the point of initial loading to the final collapse state, providing accurate representations and moderate computational demand [1].

### 5.1.1.3 Applied Element Method (AEM)

AEM virtually discretises structural members into smaller elements connected by distributed shear and normal springs. These springs represent stiffness and deformations as well as transfer stresses [68, 89]. Once the load or deformation threshold is exceeded, these springs fail, deleting any present connections and the elements start behaving as free rigid bodies [64]. Therefore, this method combines aspects from both FEM and DEM [90] and thus can be used to model and analyse a structure from the point of initial load application to the final collapse at reduced computational demand, as can be seen in Figure 7. Currently, the only software that implements AEM is Extreme Loading for Structures (ELS), which has been used to analyse the collapse of different buildings and bridges [91, 92, 80, 93, 51, 58, 69, 90, 64, 68, 89].

737



Figure 7: Pyne Gould building collapse comparison between real (left) and simulated (right) collapse shape [64]

AEM can potentially be a powerful tool for progressive collapse studies. However, to further understand the capabilities of this new method, more research is needed. In most considered projects, AEM was used to model low to mid-rise structures or ones with high regularity. To test the full performance of AEM, it should be used to study the effects of dynamic events on irregular structures and high-rise buildings. Furthermore, results from these analyses must be verified against more large-scale experiments or real-life events, and compared to results from more well-established methods to further validate the AEM.

#### 5.1.2. General Purpose Physics and Game Engines

Several open-source game engines, also known as physics engines, have been developed in response to the high demand from game developers. Game engines are designed to simulate the laws of physics, including gravity, collision detection, and object interactions, within a virtual environment by implementing physics at their back-end [94]. However, the varying scale of physical behaviour has been embedded in different game engines. It should be emphasised that the primary objective of game engines was to simulate real-world behaviours as accurately as possible with the quickest rendering time possible to fulfil the performance requirements for games. Hence, the earliest physics/game engines (Box2D and Bullet) were simplistic and thus required minimal processing capabilities. Recently, due to advancements in the capabilities of computer processors, the newest game engines (Unreal Engine and Unity) have started to embed

759 more complex behaviours.

760

761 The use of game engines has gained traction in civil engineering due to the  
762 freedom they offer engineers/developers to define and iterate the physical mech-  
763 anisms used [95, 96, 97]. More recently, the use of physics engines in progressive  
764 collapse studies is gaining traction, as large deformations, damage, and debris  
765 impact can be modelled in the game engine, and the collapse mechanism can  
766 be rendered with minimal resources. It should be noted that established multi-  
767 physics engineering software packages can handle certain aspects of progressive  
768 collapse better than game engines, especially in the early stages of progressive  
769 collapse. Additionally, engineering software packages make it simple to regu-  
770 late and extrapolate progressive collapse models. Therefore, some researchers  
771 tried to use hybrids between typical methods, such as FEM and physics (game)  
772 engines in progressive collapse investigations [98]. The application of physics  
773 engines in investigations relating to progressive collapse and collapse resistance  
774 to date is summarised in Table 4.

775

776 The advantages of the game engines lie in their ability to quickly implement  
777 collapse mechanisms during rescue situations, prioritising life-saving efforts. By  
778 enabling rapid simulations and focused rescue strategies, it provides an inval-  
779 uable tool for responders to efficiently and effectively carry out life-saving oper-  
780 ations in critical situations. Another benefit of game engines is their ability to  
781 develop multiple demolition strategies, aiding in identifying the best approach  
782 to minimise impact and enhance safety during controlled demolitions of historic  
783 structures. This enables engineers to assess various options and make informed  
784 decisions that prioritise preservation while ensuring public safety.

785

786 The difficulty of correctly simulating real-world civil engineering problems,  
787 which sometimes include several interacting systems, presents one of the hur-  
788 dles when employing a physics engine for engineering investigations. In addition,  
789 the computational resources required to simulate large-scale, high-fidelity engi-

neering systems can be demanding, requiring efficient algorithms and powerful hardware. To pursue this line of research, it is crucial to have a thorough grasp of programming, coding, software development, and structural behaviour. Due to recent advances in AI and simplicity in coding, this research area is expected to expand significantly in the coming decades. To assist and outline potential directions for future research in the field of progressive collapse, the following topics have been identified:

- Multiscale modelling: Progressive collapse modelling requires a multiscale approach as the failure is localised in certain areas. At the same time, the large deformation occurs elsewhere without changes in the system's strain energy. Multiscale modelling using a physics engine, where the scale of focus varies between segments, offers a significant advantage compared to traditional computational techniques.
- Dynamic loading: Progressive collapses are often initialised by dynamic loadings. Current practices and analytical techniques offer guidance to isolate the failure of certain elements, while dynamic loadings can affect multiple structural components at the same time. Furthermore, the redistribution of strain energy due to initial failure influences the sequence of failure. This area of research may significantly benefit from the use of a physics engine.
- Debris impact: Another loading scenario that is critical to progressive collapse is kinetic energy due to moving objects. As identified, impact influences the sequence of failure. Hence, using a physics engine can help enhance the current understanding of progressive collapse.
- Structural design optimisation and retrofitting strategies: the use of physics engines for adaptive structural design optimisation and retrofitting strategies will enable real-time adjustments to environmental conditions and unexpected events and simulate resilience and retrofitting strategies for existing structures.

Table 4: Summary of the collapse-related studies using general purpose physics and game engines

| Reference                     | Physics Engine                              | Description of the work carried out                                                                                |
|-------------------------------|---------------------------------------------|--------------------------------------------------------------------------------------------------------------------|
| Xu et al. 2013 [97]           | PhysX                                       | Investigated the progressive collapse resistance mechanisms of a bridge under localised failure in an arch segment |
| Xu et al. 2014 [99]           | PhysX                                       | Studied the collapse resistance of a multi-storey building under seismic loading                                   |
| Hamano et al. 2016 [100]      | PhysX, Bullet and Open Dynamic Engine (ODE) | Simulated the collapse of a house due to seismic loading using different physics engines                           |
| Walter and Kostack 2017 [101] | Blender and Bullet                          | Simulated the collapse mechanisms of a multi-storey building                                                       |
| Zhou et al. 2017 [102]        | Direct3D                                    | Simulated the collapse mechanism of different structures due to seismic loading                                    |
| Xu et al. 2019 [103]          | PhysX                                       | Simulated the damage to a building's ceiling due to seismic loading                                                |
| Zheng et al. 2020 [98]        | Blender                                     | Simulated the progressive collapse of a building - a hybrid approach between FEM and physics engine                |
| Lu et al. 2021 [33]           | Blender and Bullet                          | Simulated the progressive collapse of Champlain Towers South in Surfside, Florida                                  |
| Wang et al. 2023 [104]        | Unity                                       | Simulated a multi-storey structure's progressive collapse under column removal scenarios at various locations      |

- Real-time simulation and visualisation: Post-disaster rescue strategies and prediction of structural behaviour under extreme conditions require real-time simulation and visualisation. The physics engine can be a vital tool.

Nevertheless, the use of the physics engine in progressive collapse is not restricted to the aforementioned research topics. Research is anticipated to expand as knowledge advances with ongoing technological advances and quantum computing.

### 5.1.3. Comparison

Each of the methods adopted in multi-physics engineering packages and physics and game engine packages have their own advantages and disadvantages. Table 5 compares and critiques all the discussed numerical techniques, which will help the reader in selecting a suitable method based on the focus of their study and the resources available.

Table 5: Summary comparison between different numerical methods

| Method                                            |     | Advantages                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | Disadvantages                                                                                                                                                                                                                                                                                                                                                                                                                                       |
|---------------------------------------------------|-----|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Structural and multi-physics engineering packages | FEM | <ul style="list-style-type: none"> <li>• Accurate representation of initial loading stages to non-linear deformations due to the implementation of continuum modelling. This method discretises elements into smaller deformable units, accurately capturing real-life behaviour at smaller deformation phases.</li> <li>• A versatile method that enables the incorporation of various tools that can facilitate the investigation of different concepts related to progressive collapse.</li> </ul> | <ul style="list-style-type: none"> <li>• The need to incorporate additional methods such as material erosion to model cracking/separation at larger deformations.</li> <li>• Increased computational time due to the complexity of progressive collapse modelling considerations.</li> </ul>                                                                                                                                                        |
|                                                   | DEM | <ul style="list-style-type: none"> <li>• Accurate representation of separation and large deformations.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                     | <ul style="list-style-type: none"> <li>• Reduced accuracy for modelling smaller deformations since elements are assumed to be composed of non-deformable bodies interacting through deformable springs.</li> <li>• High computational demand.</li> </ul>                                                                                                                                                                                            |
|                                                   | AEM | <ul style="list-style-type: none"> <li>• Reliable modelling from linear deflections to collapse [64].</li> <li>• Accurate representation of large displacements, collision, separation and collapse progression.</li> <li>• Simple incorporation of reinforcement through spring properties.</li> <li>• Reduced computation time due to rigid body and spring application.</li> <li>• Automated crack propagation and element separation.</li> </ul>                                                  | <ul style="list-style-type: none"> <li>• Slightly reduced accuracy when compared to FEA in initial loading stages due to the utilisation of rigid bodies connected by springs [66]. In this arrangement, deformation only takes place at springs.</li> <li>• Further validation is required to confirm reliability due to the method's novelty.</li> <li>• Only one commercial AEM software package is currently available on the market</li> </ul> |
| Physics/ game engines                             |     | <ul style="list-style-type: none"> <li>• Highly versatile and accommodating</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                | <ul style="list-style-type: none"> <li>• Requires substantial understanding of programming/coding and software development</li> </ul>                                                                                                                                                                                                                                                                                                               |

## 833 5.2. *Experimental Methods*

834 If set up correctly, experimental methods can accurately represent a struc-  
835 ture’s progressive collapse behaviour. Material, physical, and structural prop-  
836 erties naturally exist in studied specimens and real-life structures. However,  
837 computational and analytical modelling require assumptions to accurately rep-  
838 resent these aspects. Full-scale experimental testing has limitations like cost  
839 and spatial demands, making its application in modern laboratories challeng-  
840 ing. Overcoming these barriers led to the simplification of the specimens or  
841 scaling them down. For example, several researchers studied sub-assemblies or  
842 2D sections of a prototype structure to simplify. Others studied fully scaled-  
843 down versions of prototypes. An in-depth review of progressive collapse-related  
844 experiments conducted to date can be found in [22, 1, 23, 24, 25, 18]. More-  
845 over, Table 6 summarises and discusses the most commonly used experimental  
846 methods employed by various researchers. This section will discuss examples  
847 of alternative testing methods and factors contributing to the quality of exper-  
848 imental data.

Table 6: Experimental arrangements used in progressive collapse studies (for the last column, please refer to Figure 8)

| Type        |                | Example                | Specimen                                                                                                | Aim                                                                                                          | Comments                                                                                                                                   | Scale | Refer to Figure |
|-------------|----------------|------------------------|---------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|-------|-----------------|
| Full-scale  | Full structure | Fang and Linzell [105] | 13-storey existing structure to be demolished                                                           | To examine progressive collapse robustness of an RC building                                                 | -Current conditions of the studied structure need to be thoroughly investigated and considered<br>-High associated cost                    | -     | Figure 8(a)     |
|             | Sub-assembly   | Codina et al. [106]    | Column arrangements with supports represented by concrete blocks                                        | To study the performance of sacrificial cladding in protecting RC members under blast loading                | -Representing restraints by concrete blocks<br>-Influence of gravity might be distorted since columns were tested horizontally             | -     | Figure 8(b)     |
| Scaled down | 2D frame       | Yi et al. [107]        | 3 storey 2D scale model used to represent a 4-bay 8-storey structure                                    | To investigate the progressive failure of a RC frame due to the loss of a lower storey column                | -Upper storeys were only represented in the form of applied loads but their redistribution effects were ignored                            | 1/3   | Figure 8(c)     |
|             | Sub-assembly   | Alogla et al. [108]    | Two-bay beam sub-assemblies                                                                             | To study the effect of additional reinforcement bars in RC beams in terms of progressive collapse resistance | -Global effects are ignored<br>-Lack of lateral restraint                                                                                  | 1/2   | Figure 8(d)     |
|             | Single storey  | Dinu et al. [92]       | Two-bay by two-bay single story model used to represent a four-bay by four-bay 6-storey steel structure | To investigate the response of two-way steel frame systems under column loss scenarios                       | -ALP contribution from upper storeys is ignored<br>-Upper storeys effects only represented by connected tubular sections (See figure 8(b)) | 3/8   | Figure 8(e)     |

### 849 5.2.1. Demolition

850 Structures scheduled for demolition can be used for progressive collapse stud-  
851 ies [109]. This approach was employed, for example, by Fang and Linzell [105]  
852 to study the robustness of high-rise concrete structures. In their research, Fang  
853 and Linzell [105] performed a controlled demolition of two 13-storey buildings  
854 at the University of Nebraska-Lincoln. A non-linear dynamic FE analysis was  
855 then performed using LS-DYNA, and the results were validated and compared  
856 with the controlled demolition event, as shown in Figure 8(a). This approach  
857 offers the benefits of full-scale testing, providing reliable data at a dramati-  
858 cally reduced cost. Data from such tests can also help in the calibration of  
859 numerical models. Current building conditions, including any degradation or  
860 anomalies, are crucial factors that need special consideration while evaluating  
861 existing structures before demolition.

### 862 5.2.2. Scaling Laws

863 Various experimental studies in the progressive collapse field adopted scaled  
864 models. The majority of such studies only focused on scaling the geometric  
865 properties of a structure or sub-assembly rather than considering different as-  
866 pects such as material properties and loading conditions. The main drawback  
867 of such models is that issues such as inertia, strain-rate and scale effects are  
868 not taken into consideration, thus leading to the distortion of the considered  
869 models and consequently the acquired results. In order to overcome such issues,  
870 researchers in several fields, such as seismic engineering and solid mechanics,  
871 adopted the use of scaling laws. In some of these fields, scaling can be consid-  
872 ered a well-established concept which mainly resulted from the need to model  
873 full structures rather than sub-assemblies, or simply due to spatial and cost con-  
874 straints. This led to the development of sets of scaling laws that guide scaling,  
875 not only of geometry, but also of various aspects of models that might have an  
876 impact on structural and dynamic behaviour. Currently, there are different sets  
877 of scaling laws directed towards different applications. These scaling laws enable  
878 the development of models of almost any scale provided a suitable material can

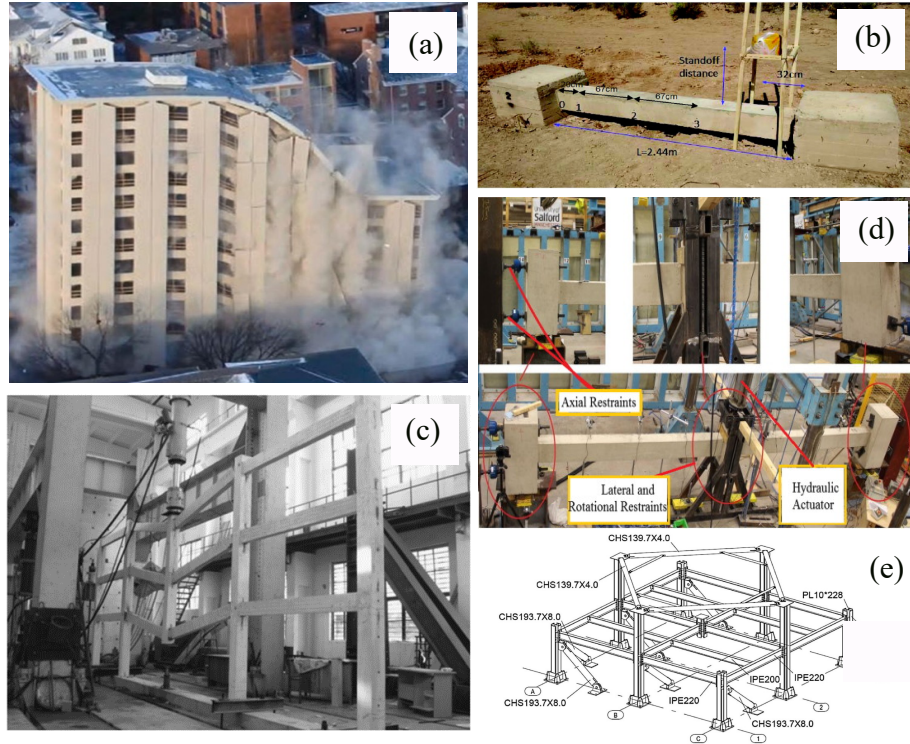


Figure 8: Experimental investigations to study progressive collapse: (a) 13-storey structure scheduled for demolition [105]; (b) Full-scale single column sub-assembly [106]; (c) 3-storey 2D scale model [107]; (d) Two-bay beam sub-assembly [76]; and (e) Scaled-down single storey model [92].

879 be utilised.

880

881 One of the first sets of seismic scaling laws was developed by Moncarz and  
882 Krawinkler [110]. According to Pitilakis et al. [111], this set of laws (Table 7)  
883 has become one of the most common scaling laws for gravity dynamic models.  
884 An example of its use can be found in a study by Qaftan et al. [112]. The  
885 main aim of this research was the verification of an FE model of a multi-storey  
886 RC structure under dynamic loading. When the proposed scaling laws were  
887 applied, Qaftan et al. [112] found a discrepancy of only about 3.5% between  
888 the frequency expected based on the scaling laws experimentally and the results  
889 from their ETABS model. To satisfy the considered scaling laws, the model,  
890 shown in Figure 9, was constructed using materials that were different from  
891 that of the prototype. For example, in the model, steel plates and tubes were  
892 used to represent the prototype's slabs and columns respectively. The choice of  
893 materials had comparatively less of an effect on the results because the mass  
894 and frequency were the primary focus of the investigation. This might not be a  
895 suitable approach for progressive collapse studies. This is because the materials  
896 that are to be used in the progressive collapse studies must precisely depict  
897 phenomena such as strain, fracture formation, and other characteristics at the  
898 large deformations. In terms of solid mechanics, an example of a developed set  
899 of scaling laws is that by Oshiro and Alves [113, 114, 115] This set of laws mainly  
900 applies to structures subject to impact loading, considering aspects such as wave  
901 velocity and strain rate [113, 114, 115]. Both sets of scaling laws discussed in  
902 this section could potentially be adopted to study different areas of progressive  
903 collapse. For example, the aforementioned seismic laws can be used to study  
904 the overall structural behaviour in collapse events. Additionally, impact scaling  
905 laws can be used to study the impact of debris on the remaining structural  
906 elements in advanced stages of a collapse.

Table 7: Scaling laws for dynamic models in terms of length scale factor  $\lambda$  [111]

|                       | Dimension    | Prototype | Model                      |
|-----------------------|--------------|-----------|----------------------------|
| Stress, pressure      | $ML^{-1}T^2$ | 1         | $\frac{1}{\lambda}$        |
| Strain                |              | 1         | 1                          |
| Length, displacement  | $L$          | 1         | $\frac{1}{\lambda}$        |
| Velocity              | $LT^{-1}$    | 1         | $\frac{1}{\sqrt{\lambda}}$ |
| Acceleration, gravity | $LT^{-2}$    | 1         | 1                          |
| Mass                  | $M$          | 1         | $\frac{1}{\lambda^3}$      |
| Volume                | $L^3$        | 1         | $\frac{1}{\lambda^3}$      |
| Force                 | $MLT^{-2}$   | 1         | $\frac{1}{\lambda^3}$      |
| Time                  | $T$          | 1         | $\frac{1}{\sqrt{\lambda}}$ |
| Frequency             | $T^{-1}$     | 1         | $\sqrt{\lambda}$           |

### 907 5.2.3. Dynamic Loading

908 It is important to note that although considering dynamic effects is extremely  
909 critical in progressive collapse events, most experiments are currently performed  
910 statically or quasi-statically due to cost constraints and practical limitations in  
911 most laboratories. This issue should be considered when assessing and analysing  
912 data acquired from such experiments since dynamic events and load applications  
913 typically have more adverse effects on structures. In progressive collapse events,  
914 for example, when a column is removed dynamically, the structure would be ex-  
915 pected to distribute most loads carried by a lost member instantaneously to the  
916 members at closest proximity to it. This load will then be redistributed through  
917 the structure to other neighbouring members until equilibrium is reached or fail-  
918 ure occurs. If the dynamic effects were disregarded and the structural members  
919 were not designed for the predicted sudden surge in loading, elements neigh-  
920 bouring a lost column might undergo different types of non-ductile failures. An  
921 example of this can be punching shear failures at nearby column locations [116].  
922 Thus, performing experimental testing under dynamic loading conditions would  
923 be highly recommended to produce representative results [117, 118, 119].

### 924 5.2.4. Initial Failure

925 In most progressive collapse studies, single or multi-column removal scenar-  
926 ios are considered as the initial step in the collapse process. The cause of the

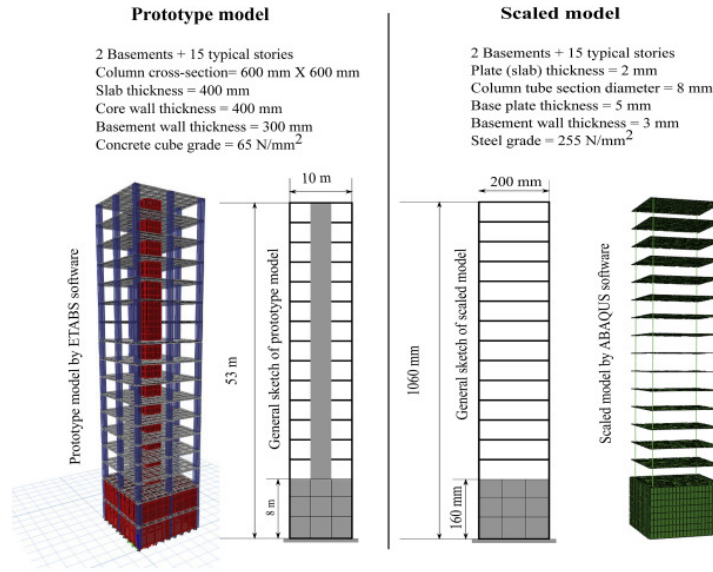


Figure 9: Seismic prototype and model constructed to scaling laws [112]

member loss is often ignored. Because of the important role of vertical load bearing elements for ensuring global stability, their notional removal is an effective way of verifying the effectiveness of alternative load paths. This, however, might lead to misrepresenting real-life events. For example, if an explosion occurs near a structure, the impact from the blast could potentially cause damage to several structural members rather than only a single column [61]. Even if only columns are usually severely damaged, damage to the other structural members should be considered due to the overall degradation in strength and ductility this can result in. One major risk associated with such cases is the overestimation of initial stiffness and premature failure of elements due to unaccounted for local damage. Therefore, it is extremely important to understand the initial cause of damage in a structure and the implications associated with it to provide an adequate representation in relevant studies and experimentation.

940

This issue is not exclusive to experimental models and should also be considered in numerical studies. Numerically, this problem was addressed by researchers in different ways. For example, the NIST [50] represented the damage

943

caused by an initial fire on the elements of the WTC7 steel frame using notches and indentations. This resulted in weakened sections to represent the equivalent damage that the fire could have caused. To address this issue, ASCE 76-23 proposes assuming initial failure in terms of damage volumes for different HIDS, as explained in Section 4.6. Additionally, for structures classified as Category D, the highest risk category identified by the code, the consideration of multi-column removal scenarios is proposed [8].

### 5.3. Analytical Methods

Analytical techniques may be beneficial for finding exact solutions to straightforward issues. These methods, however, might not be suitable for more complex problems with a higher number of variables due to the extensive complexity this might lead to. Thus, as problems get more complicated, researchers tend to focus only on a limited number of impactful variables, disregarding the rest. While this might result in simpler methods and solutions, it could affect the accuracy and usefulness of derived conclusions. This is the main issue with most proposed analytical methods related to progressive collapse. In this field, proposed analytical solutions can be divided into three main sections: robustness quantification, collapse resistance capacities and dynamic amplification factors that help to estimate the dynamic effect of progressive collapse.

#### 5.3.1. Robustness Quantification

To assess the risks and hazards associated with a structure in terms of progressive collapse, it is important to understand a structure's susceptibility to threats. To achieve this, researchers proposed different methods to quantify robustness. These methods can be divided into two main categories, deterministic and reliability/risk-based. Additionally, deterministic approaches can be classified further depending on whether they are threat-dependent or threat-independent. An in-depth summary of the methods proposed in the literature is provided in [1, 120]. Another potential approach to robustness quantification could be based on assessing the risk-independent properties of a structure

describing a structure’s general ability to resist collapse rather than its vulnerability to certain threats [120]. This approach could help in the classification process of structures and consequently the assignment of appropriate collapse resistance/ prevention techniques.

### 5.3.2. *Collapse Resistance Capacity*

Calculating the collapse resistance capacity of a member, sub-assembly or entire frame can have significant benefits in understanding the collapse resistance mechanisms of a structure. Therefore, various researchers investigated analytical methods aimed at this issue. Table 8 summarises and compares several analytical methods proposed in the literature. Most of the developed methods to date focus on calculating a frame’s load carrying capacity at the different stages of load resistance mechanisms, especially at catenary action. Although the error observed between the experimental results and various of the analytically predicted results was relatively low (between 7% and 15% [70, 121]), an important limitation of these comparisons with experimental results are that the considered tests in most cases have been performed on sub-assemblies.

Table 8: Proposed collapse resistance capacity determination methods summary

| Type                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | Reference | Purpose                                                                                                                                      | Method                                                                                                                                                                 |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|----------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Member capacity                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [70]      | Progressive collapse resistance capacity of frame beams                                                                                      | $P_{uy} = \frac{(L_1+L_2)V_u A_{th} f_y}{L_1 L_2}$                                                                                                                     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [70]      | Progressive collapse resistance capacity of slabs                                                                                            | $P_{us} = R_{sGJK}^{tm} + R_{sHIK}^{tm}$                                                                                                                               |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [83]      | Progressive collapse response of beams with a mid-span partial strength connection at compressive arch stage under column loss scenario      | $P = 76.8 \frac{EI}{L^3} u_s; u_s \leq (u_s^b = \frac{M_p L^2}{9.6 EI})$                                                                                               |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [83]      | Progressive collapse response of beams with a mid-span partial strength connection at transient catenary stage under column loss scenario    | $P = \frac{8}{L} [M_p + \frac{2K_e}{L} (u_s - u_s^b)(u_s - r_p)(u_s + u_s^b - 2r_p)]; u_s^b \leq u_s \leq (u_s^d = r_p + \sqrt{(r_p - u_s^b)^2 + \frac{F_p L}{2K_e}})$ |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [83]      | Progressive collapse response of beams with a mid-span partial strength connection at final catenary stage under column loss scenario        | $P = 8 \frac{F_p u_s}{L}; u_s^d \leq u_s$                                                                                                                              |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [45]      | Upperbound capacity demand of columns on lower storeys under pancake type collapse                                                           | $F_{c,req} = 4.28 \bar{m} g h$                                                                                                                                         |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [122]     | Ultimate load capacity of RC beams under columns removal scenarios                                                                           | $P = 2N \sin(\theta); \sin(\theta) = \frac{\delta_u}{L_2}, N = f_u A_s$                                                                                                |
| Sub-assembly capacity                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | [121]     | Progressive collapse resistance capacity of a beam-column sub-assembly at beam stage                                                         | $R^b = \frac{M_1 + M'_1}{L_1} + \frac{M_2 + M'_2}{L_2}$                                                                                                                |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [121]     | Progressive collapse resistance capacity of a beam-column sub-assembly at transient stage                                                    | $\frac{M}{M_p} + \alpha (\frac{F}{F_p})^2 = 1; \beta \frac{M}{M_p} + \frac{F}{F_p} = 1$                                                                                |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [121]     | Progressive collapse resistance capacity of a beam-column sub-assembly at catenary stage                                                     | $R^c = \frac{(L_1+L_2)y}{L_1 L_2} F_1$ ; where $F_1 = F_2$                                                                                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [13]      | Progressive collapse resistance capacity of a beam-column sub-assembly under curve type catenary mechanism pre-tension yielding of beams     | $R_L^c = \frac{64 E_1 A_1}{3(L_1+L_2)^3} \Delta^3$                                                                                                                     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [13]      | Progressive collapse resistance capacity of a beam-column sub-assembly under curve type catenary mechanism post tension yielding of beams    | $R_N^c = \frac{8 F_1 y}{(L_1+L_2)} \Delta$                                                                                                                             |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [13]      | Progressive collapse resistance capacity of a beam-column sub-assembly under straight type catenary mechanism pre-tension yielding of beams  | $R_L^c = \frac{E_1 A_1 (L_1+L_2)}{2 L_1^3 L_2} \Delta^3$                                                                                                               |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [13]      | Progressive collapse resistance capacity of a beam-column sub-assembly under straight type catenary mechanism post tension yielding of beams | $R_L^c = \frac{(L_1+L_2) F_1 y}{L_1 L_2} \Delta$                                                                                                                       |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [83]      | Progressive collapse response of a single storey under column loss scenario                                                                  | $P = \frac{1}{\alpha} \sum_i \alpha_i \beta_i P_i$                                                                                                                     |
| Frame capacity                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | [107]     | Progressive collapse resistance of a three-storey frame at plastic stage                                                                     | $P_u = 3 \frac{4M_p}{L}$                                                                                                                                               |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [107]     | Progressive collapse resistance of a three storey frame at catenary stage                                                                    | $P_{cable} = 3 \frac{2\psi}{N \sin \alpha}$                                                                                                                            |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | [73]      | Progressive collapse resistance of a multi-storey steel-braced frame considering bending, catenary and Vierendeel action                     | $P_B = \frac{(\Sigma M + M_o)(L+L')^2}{L(L')^2} + \frac{F_o w(L+L')}{LL'}$                                                                                             |
| <p>where, <math>L_1</math> and <math>L_2</math>: lengths of beam 1 and beam 2 in a two-span beam-column sub-assembly; <math>V_u</math>: vertical displacement at the removed column location within a sub-assembly; <math>A_{th}</math>: area of steel reinforcement through the whole span; <math>f_y</math>: yield stress of steel bars in frame beams; <math>R_{sGJK}^{tm}</math> and <math>R_{sHIK}^{tm}</math>: progressive collapse resistance of first and second span slabs in a two-span beam-slab sub-assembly subject to column removal; <math>EI</math>: beam flexural stiffness; <math>L</math>: beam length; <math>u_s</math>: maximum deformation at beam section; <math>r_p</math>: is the ratio of connection plastic moment to axial force capacities; <math>K_e</math>: equivalent stiffness of beam and supports; <math>\bar{m}</math>: mass per unit height of a building; <math>h</math>: original height of a building undergoing pancake collapse; <math>N</math>: axial force on a beam; <math>\theta</math>: rotation of beam section; <math>\delta_u</math>: maximum beam deflection at ultimate load; <math>L_2</math>: beam length at ultimate load; <math>f_u</math>: ultimate tensile strength of reinforcement; <math>A_s</math>: area of tensile reinforcement; <math>M'_1</math>, <math>M'_2</math>, <math>M_1</math> and <math>M_2</math>: hinge moment of Beam 1 and Beam 2 at a two-span beam column sub-assembly; <math>M</math> and <math>F</math>: bending moment and axial tension of beam sections; <math>M_p</math> and <math>F_p</math>: maximum bending moment and axial tension; <math>\alpha</math> and <math>\beta</math>: functions of beam section parameters; <math>F_1</math> and <math>F_2</math>: axial tension of beam 1 and beam 2; <math>y</math>: mid span vertical deflection of beam; <math>E_1</math>: elastic modulus of longitudinal reinforcement bars; <math>A_1</math>: cross sectional area of longitudinal reinforcement bars; <math>\Delta</math>: maximum vertical displacement; <math>F_1 y</math>: yield force of beam 1 at sub-assembly; <math>\alpha</math>: work related factor that depends on gravity load distribution; <math>\alpha_i</math>: non-dimensional work factor which depends on load distribution on a beam; <math>\beta_i</math>: a term that relates component and system deformation; <math>P_i</math>: load intensity; <math>M_p</math>: the plastic moment capacity of a cross-section; <math>L</math>: the span of a section; <math>\psi</math>: strain adjustment coefficient; <math>N</math>: the total tension force in a cross-section; <math>\alpha</math>: rotation angle of member corresponding to final collapse; <math>\Sigma M</math>: resultant bending moment at left side of a considered beam; <math>M_o</math>: moment formed by axial forces of each storey at left side of a considered beam; <math>L</math>: span of the first beam in a beam column sub-assembly; <math>L'</math>: span of the second beam in a beam column sub-assembly; <math>F_o</math>: resultant axial forces on the left side of a considered beam; <math>w</math>: deflection above failed column.</p> |           |                                                                                                                                              |                                                                                                                                                                        |

### 990 5.3.3. *Dynamic Amplification Factor*

991       Dynamic amplification factors (DAF) are factors applied to non-dynamically  
992 performed analyses to represent dynamic contributions. The application of these  
993 factors can dramatically reduce the time, cost, expertise and computational  
994 demand required for performing dynamic analyses. Currently, some CoPs adopt  
995 the application of DAFs in their simplified analyses [9, 83]. DAFs can be derived  
996 in different ways and can have a wide array of applications. For example, DAFs  
997 can be applied on an elemental and structural level [13], in force-controlled  
998 and deformation-controlled cases [9], for linear and non-linear static analyses  
999 [123, 124], and to study various mechanisms such as catenary action [13, 125].  
1000 Typically, for force-controlled linear-static scenarios, a DAF of 2 is adopted  
1001 [124, 9]. When non-linear static responses are considered, adopting a DAF of  
1002 2 has proven to be overly conservative [124]. Recently, several methods have  
1003 been developed to help derive more representative estimations of DAFs. In  
1004 addition to the methods included in Kiakojour et al.'s [16] review article, Table  
1005 9 provides a summary of different amplification factors proposed in the context  
1006 of progressive collapse.

Table 9: DAF proposals summary

| Reference                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | Description                            | Method                                                                                                                                 |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|
| Tsai [124]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Displacement based DAF                 | $DAF_{\Delta} = \frac{(2\alpha+\gamma-2)+\sqrt{(\gamma-2)^2+4\alpha(\gamma-1)}}{2\alpha+\gamma-2}$ ; for $2.0 < \gamma, \alpha \neq 0$ |
| Tsai [124]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Force based DAF                        | $DAF_p = \frac{2\mu[1+\alpha(\mu-1)]}{1+\alpha(\mu-1)^2+2(\mu-1)}$ ; for $\mu \geq 1$                                                  |
| Li et al. [126]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Energy based DAF                       | $DAF = (2 - \beta) \frac{\mu}{\mu-1}$                                                                                                  |
| Khuyen and Iwasaki [127]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | Stress based DAF                       | $DAF_i = \frac{\sigma_{idm}}{\sigma_{is}}$                                                                                             |
| Mashhadi and Saffari [128]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Damping ratio based DAF                | $DIF = (2 - 2.54\zeta) - \frac{(0.9-1.81\zeta)(\theta_p/\theta_y)}{(0.84-2.15\zeta)+(\theta_p/\theta_y)}$                              |
| Mashhadi and Saffari [128]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Post-elastic stiffness ratio based DAF | $DIF = (1.1 + 2\eta) + \frac{0.56-\eta}{0.65+(\theta_p/\theta_y)}$                                                                     |
| Scalvenzi et al. [129]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | Plastic rotation based DAF             | $DAF = 1.04 + \frac{0.45}{\frac{\theta_{pra}}{\theta_y} + 0.48}$                                                                       |
| Shi et al. [61]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Strain rate based DAF (for steel bars) | $DIF = (\frac{\dot{\epsilon}}{10^{-4}})^{\alpha}$ ; $\alpha = 0.074 - 0.040 \frac{f_y}{414}$                                           |
| Amiri et al. [130]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | Elastic stage DAF                      | $DIF = \frac{24-8\max(\frac{M_u}{M_y})}{\max(\frac{M_u}{M_y})+9.5}$ ; for $0.5 \leq \max(\frac{M_u}{M_y}) < 1$                         |
| Amiri et al. [130]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | Post yield stage DAF                   | $DIF = \frac{1.18\max(\frac{M_u}{M_y})-1.165}{\max(\frac{M_u}{M_y})-0.99}$ ; for $\max(\frac{M_u}{M_y}) \geq 1$                        |
| Where, $\alpha$ : post-stiffness ratio; $\gamma$ : force ratio; $\mu$ : displacement ductility demand; $\beta$ : yield factor; $\mu$ : ductility factor of RC frame substructure under the beam mechanism; $\sigma_{idm}$ : maximum dynamic stress factor of a member; $\sigma_{is}$ : corresponding static stress of the $i^{th}$ member; $\zeta$ : damping ratio in a considered model; $(\frac{\theta_p}{\theta_y})$ : maximum ratio of plastic and yield rotations of a member in the impacted bay of a structure; $\eta$ : post-elastic stiffness ratio; $\theta_{pra}$ : plastic rotation associated with a prescribed performance level; $\theta_y$ : yield rotation of beams; $\dot{\epsilon}$ : strain rate of a steel bar; $f_y$ : yield strength of a steel bar; $M_u$ : moment demand calculated using the original un-amplified gravity loads in a structure with a removed column; $M_y$ : yield moment capacity of beams within the affected bays directly adjacent to and above the removed column. |                                        |                                                                                                                                        |

#### 1007 5.4. Machine Learning and Statistical Approaches

1008 Machine learning can be a valuable tool in progressive collapse studies, aiding  
1009 engineers and researchers in understanding the behaviour of structures under  
1010 extreme loading conditions. A complete dataset of structural conditions and  
1011 responses to progressive collapse for a case that has to be investigated is needed  
1012 to use machine learning in such studies. For this purpose, numerical outputs  
1013 from computational tools or experimental results are used as input in machine  
1014 learning tools. For example, Fu [131] studied the effect of fire on two-storey  
1015 steel structures using machine learning with the results obtained from numeri-  
1016 cal studies.

1017  
1018 Moreover, numerous machine learning models have been developed. How-  
1019 ever, the applicability of those models depends on the characteristics of the data  
1020 that is used. Zhu et al. [132] have compared various machine learning mod-  
1021 els to understand the dynamic effect on the progressive collapse behaviour of  
1022 steel structures, where the data was taken from numerical simulations. Datasets  
1023 that consider structural geometry, material properties, applied loads, and cor-  
1024 responding collapse behaviour were used in all those studies [133].

1025  
1026 It should be noted that the accuracy of the models developed depends on the  
1027 datasets that were used to train them. Additionally, different machine learning  
1028 models can lead to different prediction accuracies for the same datasets [134].  
1029 Therefore, selecting machine learning models requires careful consideration of  
1030 the dataset and the predictive behaviour. Machine learning models can be  
1031 broadly classified into various types, including supervised, unsupervised, and  
1032 reinforcement learning. Supervised learning models learn from labelled data to  
1033 make predictions or classifications. Unsupervised learning models discover pat-  
1034 terns in unlabeled data. Reinforcement learning models learn through trial and  
1035 error, interacting with an environment to maximise rewards. As per physics  
1036 engine-related research, machine learning provides a valuable tool for structural  
1037 engineering applications. By leveraging the power of machine learning, pro-

1038 gressive collapse studies can benefit from improved predictive capabilities, an  
1039 enhanced understanding of structural behaviour, and the development of more  
1040 robust and resilient designs. For this reason, Table 10 summarises the different  
1041 collapse studies conducted using machine learning. However, to assist future  
1042 research in the area of machine learning, the following areas of research have  
1043 been identified:

- 1044 • Predictive modelling: The machine learning approach can help to de-  
1045 velop predictive models that can assess and quantify the risk of structural  
1046 collapse based on various parameters, including material properties, envi-  
1047 ronmental conditions, and historical data.
- 1048 • Structural health monitoring, assessment, and anomaly detection: Un-  
1049 derstanding the state of structure at present and the weaker structural  
1050 components that help prevent progressive collapse is vital. A machine  
1051 learning tool that links up with the structural response is the way forward  
1052 to minimise these catastrophic events.
- 1053 • Structural design optimisation and retrofitting strategies: Understanding  
1054 structural behaviour using machine learning can help to develop optimum  
1055 design strategies or prevention strategies against progressive collapse.
- 1056 • Assisting with the development of design standards: Machine learning can  
1057 enhance civil engineering design standards by analysing large structural  
1058 performance datasets, identifying patterns, and optimising designs for ef-  
1059 ficiency and safety. Continuous learning can provide data-driven insights  
1060 and predictive modelling for informed decision-making and thus develop  
1061 design standards.

1062 As mentioned, future research directions using machine learning are not limited  
1063 to the aforementioned topics. As the current understanding expands, research  
1064 areas in this field are expected to expand.

Table 10: Summary of progressive collapse studies conducted using machine learning

| References                        | Description of the work                                                                                                                                                                                                    |
|-----------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Esfandiari and Urgessa 2020 [133] | A machine learning algorithm was developed to find optimal design solutions in reinforced concrete structures subjected to progressive collapse.                                                                           |
| Fu 2020 [131]                     | A machine Learning framework developed to predict failure patterns and collapse potential of steel framed buildings in fire.                                                                                               |
| Hwang et al 2021 [135]            | A machine learning model was developed to reliably predict the seismic response and structural collapse classification of ductile reinforced concrete frame buildings under earthquake events.                             |
| Padilha Alves et al. 2022 [136]   | A statistical model was developed to improve the reliability in predicting guyed transmission line towers resistance against progressive collapse.                                                                         |
| Zhang et al. 2022 [137]           | The reliability of RC frame structures under progressive collapse was investigated using polynomial chaos expansion and pushdown analysis.                                                                                 |
| Zhu et al. 2022 [132]             | A machine learning framework was developed for assessing the dynamic increase factor (DIF) used in nonlinear static analyses (push-down).                                                                                  |
| Esfandiari et al. 2023 [138]      | Machine learning was used to carry out a progressive collapse analysis of 3D RC frames. Results showed that the analytical framework ensures system solutions meet structural integrity and constructability requirements. |
| Gan et al. 2023 [134]             | Machine learning models were developed to predict the progressive collapse resistance of RC frames.                                                                                                                        |
| Lin et al. 2023 [139]             | A machine learning model was developed to quantify progressive collapse resistance of RC beam-column substructures under middle column removal scenarios.                                                                  |
| Wang et al. 2023 [104]            | A horizontal collapse propagation prediction method and a machine learning model were developed to anticipate the internal collapse zone in progressive collapse events.                                                   |

## 1065 **6. Exploration of Prevention and Mitigation Methods**

1066 Over the last decades, researchers have made an effort to understand pro-  
1067 gressive collapse, investigate it, and come up with feasible solutions. Design  
1068 solutions against progressive collapse fall into two main categories: enhancing  
1069 inherent collapse-resisting mechanisms within structural elements and employ-  
1070 ing external solutions to prevent or limit progressive collapse. This section will  
1071 discuss both design techniques and their associated methods.

### 1072 *6.1. Inherent Collapse-Resisting Mechanisms*

1073 Different types of structures can inherently develop collapse-resisting mech-  
1074 anisms without incorporating any foreign elements into the structural system.  
1075 Most of these mechanisms help redistribute loads from a failed member and  
1076 occur mostly locally at the member level. However, they can be optimised and  
1077 incorporated into a structural system as beneficial global mechanisms. For ex-  
1078 ample, in framed structures, the main localised collapse-resisting mechanisms  
1079 typically develop within beam and slab elements. Moreover, in buildings such  
1080 as braced steel structures, bracing members can help in collapse resistance. Ad-  
1081 ditionally, non-structural elements such as masonry infill walls were also found  
1082 to contribute to load redistribution through a structure in extreme events. In  
1083 this section, the main collapse-resisting mechanisms in framed structures will  
1084 be explored based on the elements through which they develop.

#### 1085 *6.1.1. Beam Mechanisms*

1086 The three main collapse-resisting mechanisms for beams are flexural (beam)  
1087 action, compressive arch action (CAA) and catenary action. The flexural action  
1088 of the beam resists the moment applied at the early stage, followed by the CAA  
1089 as the deformation of the beam increases. Finally, catenary action, the final  
1090 line of collapse defence, is activated when plastic hinges develop and undergo  
1091 extreme plastic deformation.

### 6.1.1.1 Flexural Action

After loss of a column in a structure, the area above the removed column, originally designed to resist tension, is subjected to high compression forces and vice versa, as shown in Figure 10. This is one of the first concerns of a structure after a column loss. To accommodate that, the structure tries to develop bending resistance at the beam ends on both sides of the removed column to resist major deflections and fractures [121]. This mechanism is mostly present in elastic deformation stages. At this stage, most damages are concentrated at the beam-column connections [140]. Flexural action, sometimes referred to as beam action, is highly dependent on beam depth, as it is proportional to a beam's flexural capacity.

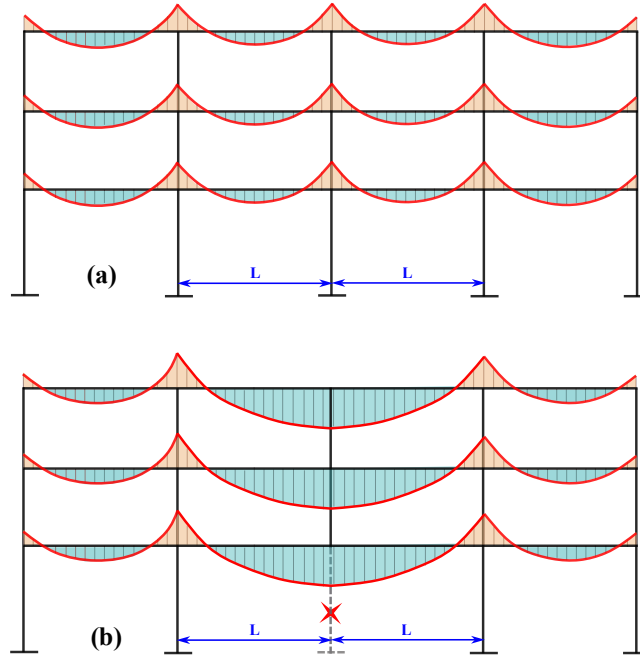


Figure 10: Typical distribution of bending resistance of moment frame: (a) before column loss and (b) after column loss, adapted based on [108]

### 1103 6.1.1.2 Compressive Arch Action

1104 Compressive arch action can be defined as the development of diagonal com-  
1105 pression forces in beams. This mechanism is similar to the mechanism used by  
1106 an arch bridge to resist external load. In framed structures, when beams deflect  
1107 beyond a certain limit because they have non-negligible depths, their ends need  
1108 to be pushed outward slightly as they rotate due to positive bending. When  
1109 there is sufficient lateral restraint opposing this outward movement, compressive  
1110 stresses are induced in the beam following the shape of an arch, as illustrated  
1111 in Figure 11. This creates additional vertical resistance to the downward force  
1112 on the beam. During the transition from flexural action to CAA, flexure and  
1113 compression forces can be present in the beams. Further deflections make the  
1114 compression forces more dominant (Figure 12). One characteristic of CAA is  
1115 that columns supporting the deflecting beams are pushed outwards during that  
1116 mechanism. At this stage, flexural damages, which typically do not propagate  
1117 through the full depth of sections, start developing at beam ends [141].

1118  
1119 The three main factors that contribute to the effects of CAA are the span-to-  
1120 depth ratio of a beam, longitudinal reinforcement, and lateral restraint. Higher  
1121 span-to-depth ratios in beams lead to milder CAA due to this effect on the  
1122 geometry of a compressive arch. This is in addition to its impact on the flexural  
1123 capacity of beams and thus the development of bending moments [82, 108].  
1124 Reinforcement also has a similar effect on CAA. For compressive forces and thus  
1125 CAA to develop, adequate axial restraint should be available in a structure [14].  
1126 For example, in their research, Long et al. [141] increased the column sizes of  
1127 their tested sub-assemblies to increase lateral restraint. This led to critically  
1128 increasing CAA in the considered beams and decreasing forces in the columns.  
1129 Overall, with the appropriate span-to-depth ratio, reinforcement and lateral  
1130 restraint, CAA can increase the load-carrying capacity of a beam by up to 60%  
1131 [23]. When the discussed factors are optimised, CAA can lead to an increase of  
1132 up to 160% in the load-carrying capacity of a beam [82].

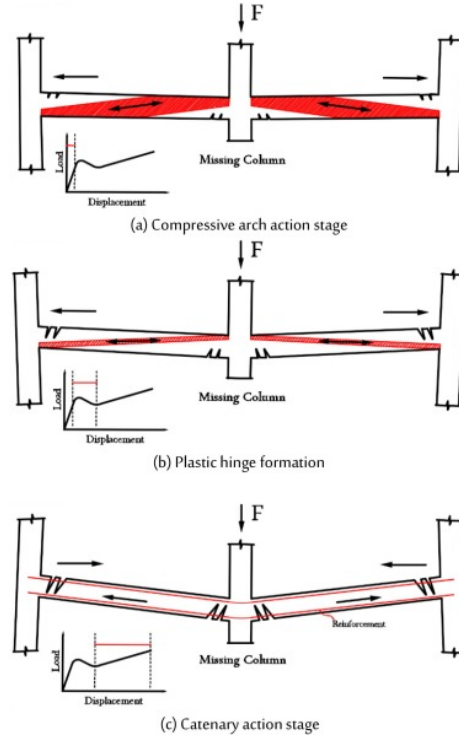


Figure 11: Illustration of CAA and catenary action [23]

### 6.1.1.3 Catenary Action

Catenary action, also referred to as catenary tensile action (CTA), is one of the most investigated concepts in this field, as it is the last inherent collapse prevention mechanism in a building [30]. Catenary action utilises the final plastic reserve in a structure. Moreover, after reaching its peak, the structure encounters a loss in load-bearing capacity until it stabilises or fails [51]. To ensure catenary action develops, adequate lateral restraint must be present [70, 141]. Additionally, continuity of beams must be ensured since it is one of the main contributors to catenary action [41, 79, 30, 81]. The main indicator that catenary action is activated is when forces in the entire cross section of a beam all change from compression to tension [142]. This usually occurs when beam deformations start exceeding their depths [108, 23, 61, 76]. Unlike in CAA, damages in catenary action occur along the entire depth of the

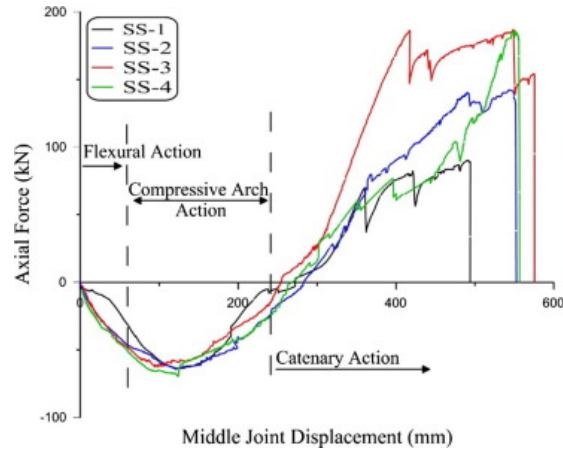


Figure 12: Onset of collapse resisting mechanisms in relation to axial load and displacement [108]

beam, since they are caused by tension rather than flexure [125]. Additionally, longer span-to-depth ratios can have a positive impact on catenary action, since, although it limits CAA, it triggers earlier mobilisation of catenary action [141]. Finally, when compared to CAA, the onset of catenary action can be more easily identified [108]. This is attributed to the fact that compression forces and bending moments exist in both flexural action and CAA. However, catenary action solely depends on tensile forces. Figure 12 demonstrates this behaviour as the catenary phase starts in the tested specimen when the axial forces completely change from compression to tension. From their research, Alshaikh et al. [23] concluded that fully restrained specimens with horizontal ties experience an increase in load-bearing strength of circa 2.89 times when compared to the flexural capacity. Also, Alogla et al. [108] concluded that catenary action can increase progressive collapse resistance by 67%. A visualisation of CAA and catenary action can be seen in Figure 11 with their associated compressive and tensile forces in addition to their impact on the movement of the outer columns of the presented specimen.

1162

Due to the development of tension in the beams during this type of mechanism, the columns are pulled inward [14, 70]. This phenomenon might lead to further

1164

collapse propagation in a structure and should be further studied. Most testing in this area has only been done using sub-assemblies and not whole structures because of cost, time, and spatial restrictions. Thus, the global effect of catenary action has not yet been studied and accounted for. Moreover, although some CoPs highly depend on the development of catenary action based on continuity [10], there is not enough evidence to support the theory that catenary action will fully develop under the highly dynamic nature of progressive collapse events. This can be attributed to the fact that most of the experimental tests conducted to date adopted static or quasi-static loading conditions. This might lead to an inadequate representation of how a structure will behave in a real-life dynamic collapse event. Due to the importance of catenary action and its potential role in collapse prevention, various researchers have studied different methods to help better use it.

#### 6.1.2. Floor Slab Mechanisms

Floor slabs have a significant positive impact on progressive collapse resistance. Disregarding these effects in modelling and studying skeletal structures can lead to overly conservative, costly, and unsustainable structural designs [23, 90, 58]. The main contribution that slabs have in structures after a column loss incident is load redistribution. This can mainly be attributed to the membrane or diaphragm effect imposed by slabs in a structural system. In addition to the linear load redistribution, slabs develop mechanisms similar to CAA and CTA that develop in beams. However, the main difference is that these effects happen along two axes rather than one [13]. The mechanisms are compressive membrane action (CMA) and tensile membrane action (TMA).

The main structural concepts behind CMA and TMA are almost the same as those behind CAA and CTA. For example, CMA starts to develop at much smaller deflections than TMA. Moreover, additional reinforcement in a slab results in enabling the activation of TMA at lower deflections and eventually higher ultimate load resistance [143]. The membrane actions of the slabs under

1195 large deflections are illustrated in Figure 13. In general, the most dominant and  
 1196 beneficial contribution of slabs can be attributed to the tensile action rather  
 1197 than the compressive action. In fact, from their research, Alshaikh et al. [23]  
 1198 concluded that slabs can lead to a 2.5-fold increase in overall tensile action in  
 1199 the building, which can be enhanced through anchorage and optimisation of  
 1200 the concrete cover of the bottom bars [79]. Consequently, this can lead to an  
 1201 overall reduction in deflection, further load redistribution and enhancement in  
 1202 collapse prevention [90, 56]. Moreover, slabs were estimated to contribute to  
 1203 around 26 to 34% of a structure's progressive collapse resistance. This conclu-  
 1204 sion was reached by comparing the performance of beam/column only structures  
 1205 to structural frames with slabs, based on results from both numerical analyses  
 1206 and laboratory experiments [70, 58, 144].

1207

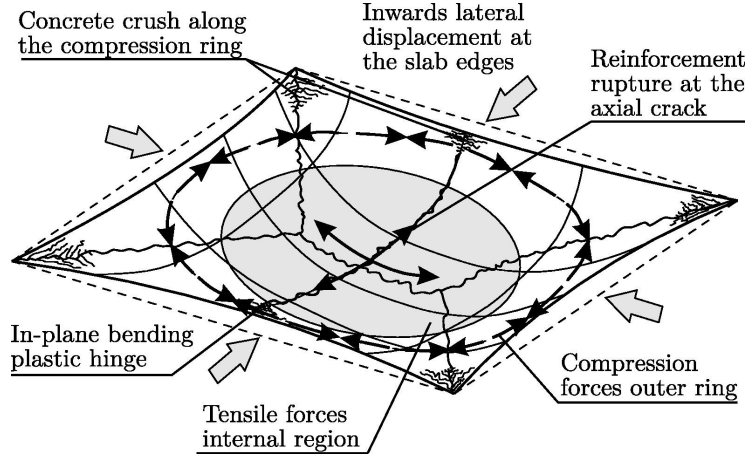


Figure 13: Slab membrane forces under large displacements [145]

1208 Although slabs can have very beneficial effects on progressive collapse resistance  
 1209 when their mechanisms are utilised, failures in slabs can be detrimental to a  
 1210 structure's integrity. One of the most common causes of progressive collapse  
 1211 events is the punching shear failure of columns through flat slabs [12]. One  
 1212 common prevention method for this issue is ensuring adequate continuity of  
 1213 reinforcement at column-slab connections. Another economical solution is to

1214 increase the reinforcement and slab thickness at column locations, forming drop  
1215 panels, while designing the rest of the slab for the typical structural loads. This  
1216 helps employ materials effectively while eliminating the risk of punching shear  
1217 failure.

### 1218 *6.1.3. Bracing*

1219 Bracing is usually incorporated into structures for lateral stability purposes.  
1220 In the case of wind loading, bracing primarily helps redistribute loads through  
1221 columns to the foundations. In progressive collapse events, bracing can help  
1222 redistribute additional gravity loads due to a potential element loss. The addi-  
1223 tional contributions of bracing were successfully investigated and applied ade-  
1224 quately for seismic cases, but very little research was done regarding the pro-  
1225 gressive collapse applications of this solution. This field of inquiry is pivotal  
1226 in the examination of the resilience of existing structures against progressive  
1227 collapse. Qian et al. [144] investigated the benefit of three different types of  
1228 braces through laboratory experiments and computational simulations using  
1229 LS-DYNA FE software. Figure 14 illustrates the different types of braces con-  
1230 sidered within this research, which are the X, V and inverted V braces. This  
1231 study concluded that the addition of bracing can increase the load-bearing ca-  
1232 pacity of a structure between 72% and 152% after a column removal event. In  
1233 addition, X-braces achieved the highest resisting capacity and ductility levels.  
1234 Consequently, the failure of X-braces also had the most detrimental effects on  
1235 the structure.

1236

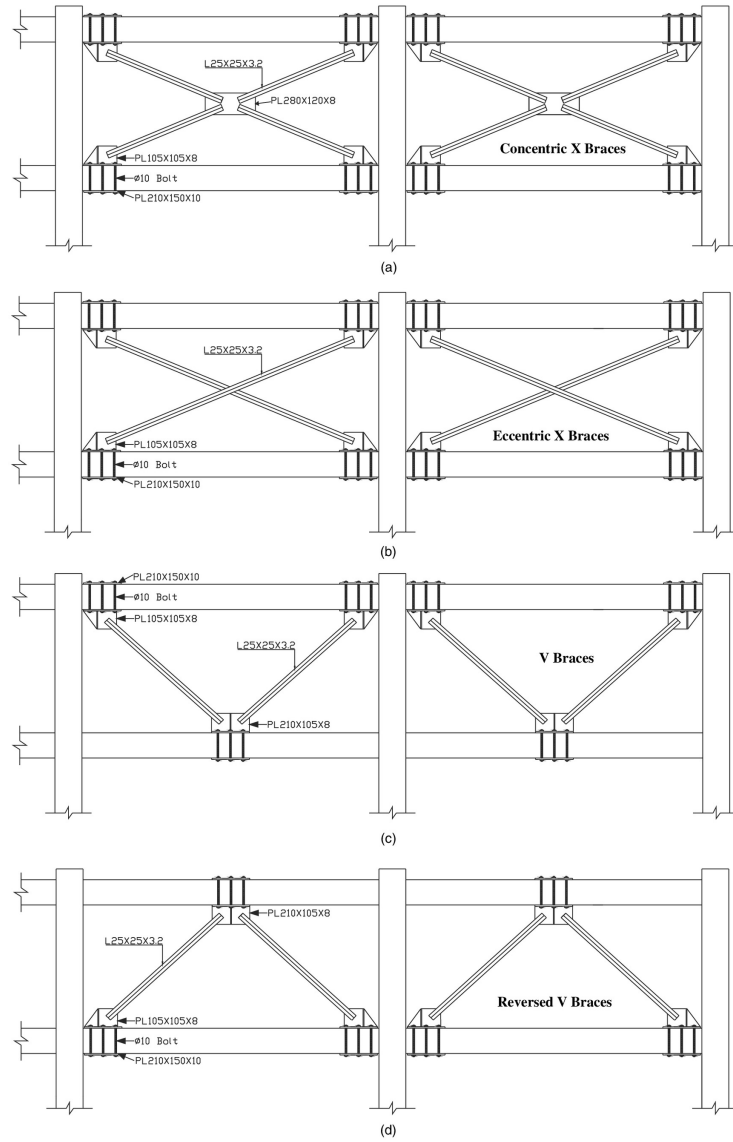


Figure 14: Bracing types tested under progressive collapse scenarios [144]: (a) Concentric X braces; (b) Eccentric X braces; (c) V braces and (d) Reversed V braces

1237 Similarly, Qiao et al. [73] tested the efficiency of vertical and horizontal in-  
 1238 verted V bracing in the prevention of progressive collapse. For their work, Qiao  
 1239 et al. [73] completed investigations using pushdown analyses in ABAQUS and  
 1240 concluded that a combination of vertical and horizontal bracing proved to have

1241 a significant effect on load redistribution to other bays of a structure after a  
1242 column loss event. This combination also contributed to enhancements in CAA  
1243 and the overall collapse resistance of the tested structure. Moreover, Qiao et al.  
1244 [73] noted that when bracing is added in all bays of the top storey, the best load  
1245 redistribution performance is noticed. This is due to the additional stiffness and  
1246 load attraction this can lead to. Although potentially beneficial for progressive  
1247 collapse, increased stiffness in only one storey, and thus stiffness irregularity,  
1248 can lead to issues with the seismic performance of the structure. Therefore, its  
1249 use in zones of high seismicity should be considered with utmost caution.

1250

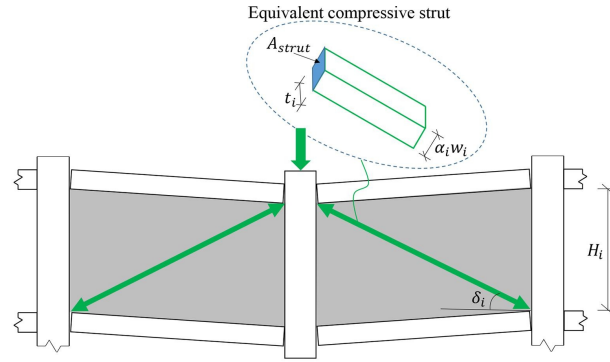
1251 Generally, bracing has had various applications and has a high potential of being  
1252 a beneficial collapse resistance tool in low to medium-rise buildings. This can  
1253 mainly be attributed to the minimal costs related to its material, application,  
1254 and maintenance, in addition to its potentially high effectiveness and efficiency.

#### 1255 6.1.4. *Masonry Infill Wall Mechanisms*

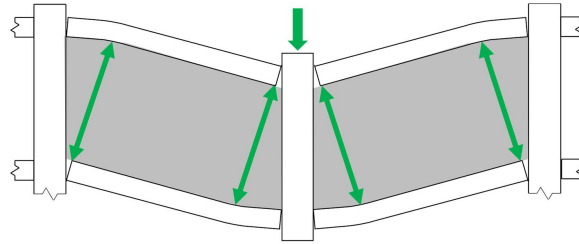
1256 Masonry infill walls are non-structural members that can be used in different  
1257 types of structures. Lately, the effect of these elements on progressive collapse  
1258 has been of researchers' interest due to the potential benefits these members  
1259 can offer. From various experiments and computer analyses, it was determined  
1260 that fully infilled walls can highly increase a building's robustness and load  
1261 redistribution ability [12, 144]. Under large deformations, compression zones  
1262 can develop in these walls, which then locally behave as struts/ bracing elements  
1263 [23, 125], as shown in Figure 15. This helps reduce deformations and damage to  
1264 the overall structure by assisting in developing ALPs. Consequently, infill walls  
1265 can help increase the ultimate strength and collapse resistance of a structure.

1266 Potentially, such walls can be strategically placed in buildings to act as  
1267 structural load redistribution systems in extreme events, offering a practical,  
1268 cost-effective collapse prevention method. Despite their benefits, one major  
1269 drawback of masonry infill walls is that once larger cracks start to develop in  
1270 them with higher loads and deformations, sudden deterioration in strength is

usually noted in the considered structural frames. Additionally, their incorporation can highly increase the restoration costs of a frame [146].



(a) Compressive strut action in the initial stage



(b) Compressive strut action in the plastic and catenary stages

Figure 15: Compressive strut in masonry infill walls [125]

#### 6.1.5. Additional Contributions

In addition to the considered members in this section, other structural and non-structural elements incorporated within a structure can affect its progressive collapse resistance. For example, the contribution of shear walls, transfer elements and non-structural cladding should be investigated. Although some of these members may have negligible benefits, it is important to understand the impact of all elements within a system to ensure it is best optimised. Additionally, the combined stiffness of such elements might affect the load distribution

1281 within a structure.

1282

1283       Moreover, most conducted studies to date focus on the contribution of indi-  
1284 vidual members or the mechanisms that develop at a sub-assembly level rather  
1285 than at a global level. This can mainly be attributed to the limitations asso-  
1286 ciated with full-scale testing and computer modelling. Examples of beneficial  
1287 global mechanisms that could be further investigated in terms of progressive  
1288 collapse resistance are Vierendeel and global arching actions. Vierendeel action  
1289 refers to the mechanism adopted by Vierendeel frames to carry and distribute  
1290 loads. In such frames, rigid connections transfer shear loading through chords  
1291 (horizontal members) by developing bending moments. As a result, all mem-  
1292 bers in a Vierendeel frame experience combined axial, shear and bending stresses  
1293 [147]. In framed structures, in case of a column loss and as the structure expe-  
1294 riences global vertical deflections, Vierendeel action develops globally through  
1295 the rectangular frames to help resist further deflections and redistribute loads  
1296 to other structural members.

1297

1298       Furthermore, similar to local arching in beams, when a structure deflects  
1299 globally, it can experience global arching action. In this mechanism, forces can  
1300 be redistributed throughout the structure in the form of an arch. The ability of  
1301 a structure to develop and mobilise a load distribution arch depends on several  
1302 factors, including its height, width and the stiffness of its members. Vierendeel  
1303 and global arching actions can be utilised together to help redistribute loads in a  
1304 structure and resist collapse following local failure. The beneficial contributions  
1305 of such mechanisms need to be further investigated and optimised. Figure 16  
1306 helps illustrate the correlation between various elements in a structure and their  
1307 potential collapse-resisting mechanisms discussed within this section.

## 1308 6.2. Proposed Methods

1309       There are two main philosophies typically adopted in progressive collapse  
1310 solutions. The first philosophy aims to completely prevent collapse, which can

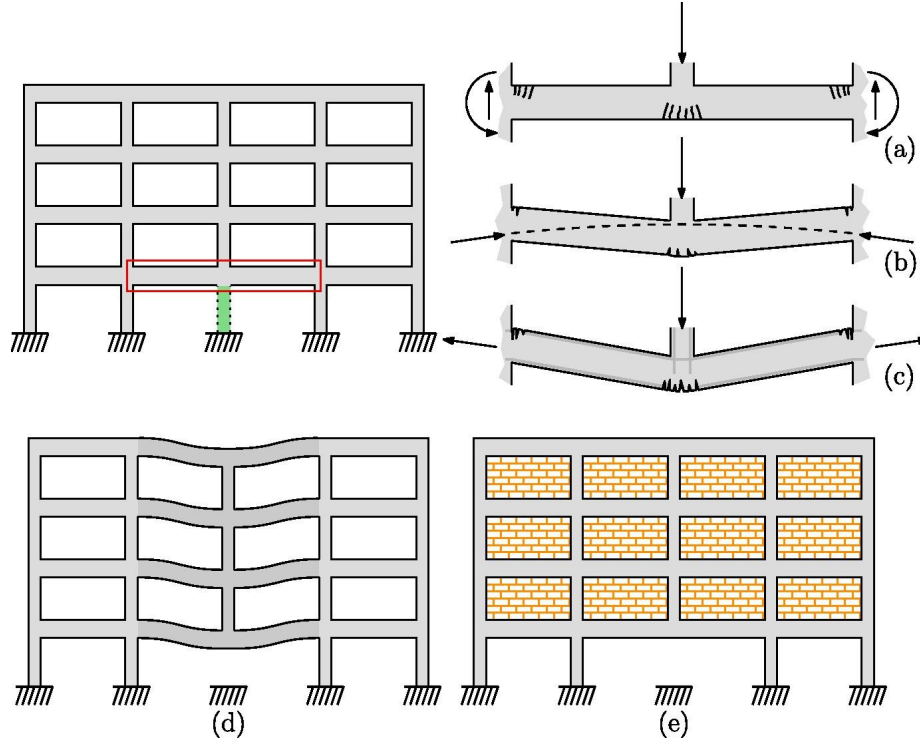


Figure 16: Collapse-resisting mechanisms in progressive collapse events: (a) flexural; (b) arch action; (c) catenary action; (d) Vierendeel action; and (e) contribution of non-structural elements [16]

1311 be achieved through designing a structure to bridge over a lost element. Al-  
 1312 though this can be effective in structures of smaller spans and single-element  
 1313 loss scenarios, this class of solutions can be impractical and extremely costly in  
 1314 larger-scale projects. The second set of solutions proposes limiting or mitigat-  
 1315 ing collapse rather than preventing it. To achieve this, for example, a structure  
 1316 can be divided into sections within which collapse is allowable as long as it  
 1317 does not propagate to other parts of the structure. This section discusses the  
 1318 two main philosophies adopted for most progressive collapse solutions as well as  
 1319 their attributed methods proposed in the literature.

#### 1320 6.2.1. Prevention Methods

1321 To date, most progressive collapse design proposals aim at preventing col-  
 1322 lapse rather than limiting it. Some proposed prevention methods, which will

1323 be discussed in this section, include member retrofitting, the implementation of  
1324 steel cable systems, additional reinforcement and seismic design parameters in  
1325 addition to other non-structural measures.

#### 1326 **6.2.1.1 Steel Cable Systems**

1327 Cable systems were proposed as a prevention technique for new and retrofitted  
1328 structures [148, 75, 149, 150]. One of the proposed systems consists of cables  
1329 connected at beam ends running parallel to the columns. These cables are then  
1330 connected to trusses located at the top of the structure, as shown in Figure  
1331 17. The main function of this proposed system is to re-transfer loads from  
1332 a lost column to other members in the structure through cables and trusses.  
1333 Moreover, tension forces developing in the cables above the removed column  
1334 can help critically reduce deflections in the members around and above the re-  
1335 moved columns. This can help keep larger sections of the structure performing  
1336 linearly to reduce the cost of any associated damages and restoration needed  
1337 after the column loss event. Hadi and Alrudaini [75], Izadi and Ranjbaran [148]  
1338 and Alrudaini [151] studied the applicability of this system using the nonlinear  
1339 dynamic analysis procedure proposed by the United Facilities Criteria [UFC]  
1340 (2009). Hadi and Alrudaini [75] used the analysis software ANSYS while Izadi  
1341 and Ranjbaran [148] used SAP2000 but still came to similar conclusions. An  
1342 alternative implementation for steel cables as a progressive collapse prevention  
1343 measure is that proposed by Astneh-Asl et al. [149, 150]. This method proposes  
1344 placing cables within slabs or on top of girders along the exterior column lines  
1345 of structures. The main function of this system is to ensure that if a perimeter  
1346 column is lost, the structure can redistribute loads through the cables using  
1347 catenary action. This system was experimentally tested using a full-scale spec-  
1348 imen representing one floor of a steel structure. Both cable systems proved  
1349 to successfully help in load redistribution, deformation reduction and thus pre-  
1350 vented progressive collapse. Cable systems can be beneficial in structures  
1351 with no architectural or cost constraints. However, they might not be appli-  
1352 cable to all types of structures, and these constraints become more apparent

1353 in lower-rise structures where the cost of installation and maintenance of this  
 1354 type of system might form a significant portion of the overall cost of the project.  
 1355

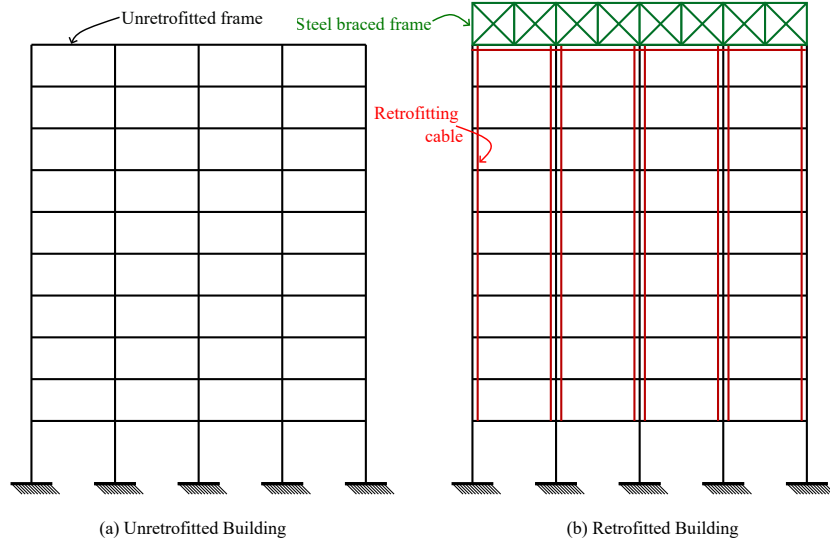


Figure 17: Progressive collapse resistance cable system, adapted based on [75]

#### 1356 6.2.1.2 Member Retrofitting

1357 To limit the impact of an extreme event such as a blast, some researchers have  
 1358 proposed retrofitting members in a structure. Retrofitting can be applied to  
 1359 new and existing buildings and usually has one of three main aims: mecha-  
 1360 nism enhancement, strengthening, and energy absorption. Retrofitting aimed  
 1361 at mechanism enhancement focuses on trying to enhance the collapse-resisting  
 1362 mechanisms in a structure by acting as external reinforcement. For example,  
 1363 carbon-fibre reinforced polymers (CFRP) can encase beams to activate ALPs  
 1364 [23]. The main function of this encasement is to help the beams bridge over  
 1365 lost columns by further enhancing the collapse prevention mechanisms such as  
 1366 catenary and flexural action. Thus, the external CFRP layer acts in a similar  
 1367 way to continuous reinforcement but provides more ductility and rotational ca-  
 1368 pacity [152]. Similarly, Qian and Li [153] used CFRP in retrofitting slabs and

1369 concluded that it can enhance a slab's load redistribution abilities.

1370

1371 In terms of strengthening, steel jacketing is most commonly used [154]. Steel  
1372 jacketing helps in increasing the serviceability of a member in near-field explo-  
1373 sions [155]. Less initial local damage can help reduce the overall subsequent  
1374 damage in a building. In an attempt to also reduce the initial local damage  
1375 endured by a member, Codina et al. [156, 106] tried to use sacrificial cladding  
1376 elements made out of reinforced resin panels and insulation. In their research,  
1377 Codina et al. [106] performed a series of experiments to represent the impact  
1378 of blasts on retrofitted members using resin panels and steel jacketing. From  
1379 this experimentation, it was concluded that steel jacketing can lead to a 57.4%  
1380 decrease in deformation when compared to un-retrofitted members. Moreover,  
1381 reinforced resin cladding was found to offer a 66% decrease in deformation in  
1382 a blast event when compared to un-retrofitted members. The beneficial effects  
1383 of steel jacketing and sacrificial cladding are demonstrated in Figure 18 since  
1384 the retrofitted members endured much less damage than the unprotected ones.  
1385 Retrofitting can be one of the most effective and practical measures that can be  
1386 applied to existing structures to help reduce their risk of progressive collapse.  
1387 This solution, however, might not be the most cost-effective for new structures  
1388 that can implement more sustainable measures in their design. For more infor-  
1389 mation on the currently proposed strengthening and retrofitting techniques in  
1390 the literature, refer to Kiakojouri et al. [157]

### 1391 6.2.1.3 Additional Reinforcement

1392 One of the most economical methods to reduce the risk of progressive collapse  
1393 in reinforced concrete structures is the optimisation of the reinforcement it-  
1394 self, which forms the tying elements in RC structures. Reinforcement can have  
1395 major effects on the strength and ductility of concrete members. Thus, var-  
1396 ious researchers aimed to further understand those effects to ensure that the  
1397 reinforcement capabilities are best employed. Typically, in beams, there are  
1398 two types of reinforcement: longitudinal and transverse. Longitudinal rein-

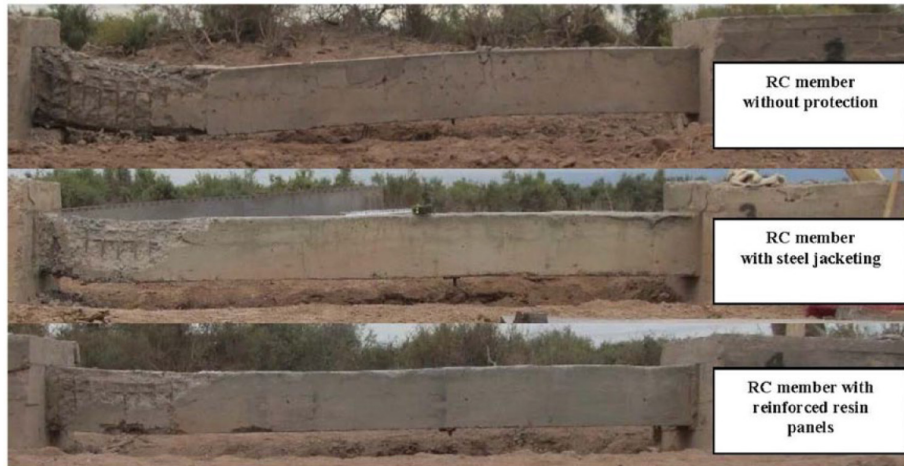


Figure 18: Member retrofitting impact [106]

1399   forcement was found to have more impact on a member's progressive collapse  
 1400   resistance characteristics, such as rotational capacity and strength. For exam-  
 1401   ple, from their work, Abdelwahed [77] concluded that additional longitudinal  
 1402   reinforcement can lead to an increase in ultimate load-bearing capacity by circa  
 1403   50%. Similarly, from their research and experimentation on catenary action,  
 1404   Abdelwahed [77] and Alshaikh et al. [23] concluded that additional longitudi-  
 1405   nal reinforcement can increase the rotational and bending moment capacity of  
 1406   an element.

1407

1408   On the other hand, Long et al. [141] noted that although increasing longitudinal  
 1409   reinforcement enhances and triggers catenary action earlier as well as increases  
 1410   deformation capacity, it can lead to a reduction in load-bearing capacity. Fur-  
 1411   thermore, Ren et al. [143] concluded that over-reinforcement can also lead to  
 1412   accelerated bending failure and earlier onset of catenary action. Additionally,  
 1413   Long et al. [141] proposed that additional reinforcement might not always lead  
 1414   to increased capacity due to the premature failure that can happen in the bars  
 1415   in progressive collapse events before reaching the full expected capacity due to  
 1416   the sudden dynamic load application usually associated with such events.

1417

1418 Various researchers have also looked into the effect of the reinforcement location  
1419 on the aforementioned structural properties of a member. It was concluded that  
1420 additional top reinforcement helps in decreasing rotation and tension forces in  
1421 members [141, 90]. Moreover, middle reinforcement helps in increasing ductility  
1422 and enhances tensile capacity by about 50% of the load carried by the top and  
1423 bottom reinforcement [108]. Finally, bottom reinforcement can also enhance the  
1424 load-bearing capacity of an element [82]. This can mainly be attributed to the  
1425 fact that bottom reinforcement at beam ends is usually one of the last to fail  
1426 in typical collapse resistance behaviour, enabling the presence of some residual  
1427 strength even after the maximum bearing capacity is reached.

1428

1429 Reinforcement is crucial for the behaviour of reinforced concrete structures,  
1430 and research has been conducted to optimise it for progressive collapse-resisting  
1431 mechanisms. However, most studies have used static or quasi-static loads due  
1432 to spatial, time, and cost constraints, which may not accurately represent the  
1433 dynamic effects of progressive collapse. Additionally, experiments have assumed  
1434 extremely stiff end conditions, which may not be feasible in real-life structures.  
1435 Therefore, further investigation is needed to consider all contributing factors  
1436 and produce informed recommendations.

#### 1437 **6.2.1.4 Seismic Design**

1438 Since seismic and progressive collapse events have a dynamic nature, several  
1439 researchers have tried to study the effect of seismic design on progressive col-  
1440 lapse resistance. Many researchers explained that seismic design can have a  
1441 positive impact on progressive collapse resistance due to the increase in section  
1442 sizes and longitudinal reinforcement and consequently strength and ductility  
1443 that this type of design usually has on a structure [78], [81], [42] and [142].  
1444 Several researchers conducted progressive collapse investigations on seismically  
1445 designed structures. For example, in their work, Sadek et al. [158] considered  
1446 column removal scenarios from assemblies of non-seismically designed frames,  
1447 Intermediate Moment Frames (IMF) and Special Moment Frames (SMF). These

1448 IMF and SMF were designed in accordance with ANSI/AISC 341 and ACI 318  
1449 to meet certain ductility and strength requirements as well as connection design  
1450 criteria [158]. Overall, SMF assemblies were found to achieve 2.25 times higher  
1451 ultimate loads than the IMF assemblies, which indicated the positive impact  
1452 that seismic detailing can have on progressive collapse resistance from a load-  
1453 bearing capacity perspective. Similarly, Yap and Li [159] conducted a study to  
1454 investigate the contribution of exterior beam-column joints in column removal  
1455 scenarios. From this testing, seismic detailing was found to significantly reduce  
1456 crack width and propagation in members. Moreover, since most seismic guide-  
1457 lines promote the design of regular, symmetric structures, seismically designed  
1458 structures tend to inherently have higher levels of redundancy and load redis-  
1459 tribution capabilities.

1460

1461 It is important to note that, as shown in Figure 19, SMF and IMF assem-  
1462 blies were tested under monotonic displacement conditions to simulate column  
1463 loss scenarios. The rotational capacities of the considered joints were found  
1464 to be 7 to 8 times higher than those obtained based on seismic cyclic testing  
1465 to verify compliance with ASCE 41-06's acceptance criteria [160]. This is be-  
1466 cause fatigue-related failures are mostly eliminated under monotonic testing.  
1467 Although most research in this area highlights the undeniable benefits of adopt-  
1468 ing seismic detailing in progressive collapse design, it is important to note that  
1469 most of the undergone testing was based on sub-assemblies of structures. Thus,  
1470 to further validate conclusions drawn in this regard, testing considering global  
1471 conditions should be carried out.

1472

1473 Other seismic design concepts could also be explored and adopted to prevent  
1474 or control damage propagation in progressive collapse events. For example,  
1475 strong column-weak beam connections could be adopted to help localise collapse.  
1476 In such arrangements, in the event of local failure, weaker beams are predicted  
1477 to fail first before the columns. Thus, the failure of these beams can help  
1478 arrest failure propagation to the neighbouring columns and, consequently, the

1479 remaining structure as a form of inherent segmentation. Further research needs  
 1480 to explore the effectiveness and applicability of this method. Moreover, other  
 1481 types of seismic connections could also be adopted in progressive collapse design.  
 1482 Elkady et al. [161], for instance, used Reduced Beam Section (RBS) connections  
 1483 in the design of Manchester's Viadux 2, a complex 15-story steel building that  
 1484 spans over a historic viaduct employing a transfer truss. The main function  
 1485 of the RBS connections implemented in the truss design was to ensure that,  
 1486 during higher deflections resulting from a potential column loss, non-linearities  
 1487 will be focused at the RBS locations, thus controlling the location at which  
 1488 plastic hinges formed. This can be attributed to the fact that because of their  
 1489 reduced area, the RBS are considerably weaker than neighbouring sections. Such  
 1490 application ensured that failures would mostly occur away from the connections  
 1491 themselves, at the locations of RBS, thus preventing more significant failures  
 1492 from occurring. The effectiveness of this method was tested using detailed 3D  
 1493 dynamic non-linear analyses in the FEA software, ETABS [161]. Given the  
 1494 potential of such applications, the implementation of various seismic design  
 1495 concepts in progressive collapse design should be further explored.



Figure 19: Full-scale seismic detailed sub-assembly for column-removal testing [160]

### 6.2.1.5 Dampers

Under dynamic conditions, it is essential to consider energy, especially in cases such as seismic and impact loading. In order to prevent damage due to excessive kinetic energy in a structure, an energy absorption or dissipation device can be used. In seismic design, dampers have been implemented as a common solution to help in the energy dissipation process to ensure that most structural members remain elastic to prevent costs associated with their renovation. There are two main types of dampers: active and passive. Active dampers require a constant source of energy and more maintenance than passive dampers. Thus, despite their underlying benefits, their associated costs make them a less favourable solution. Passive dampers, on the other hand, require minimal maintenance and thus provide a much more practical alternative. There are three main types of passive dampers: velocity-activated (e.g. viscous fluid and viscoelastic solid dampers), displacement-activated (e.g. metallic and friction dampers), and motion-activated (e.g. tuned-mass dampers) [162]. Figure 6.2.1.5 illustrates the behaviour of the most commonly used types of dampers.

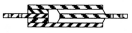
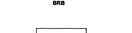
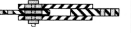
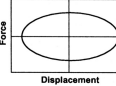
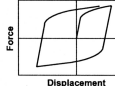
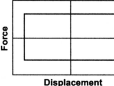
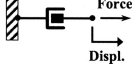
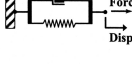
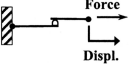
|                               | Viscous Fluid Damper                                                                | Viscoelastic Solid Damper                                                           | Metallic Damper                                                                      | Friction Damper                                                                       |
|-------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|
| Basic Construction            |  |  |  |  |
| Idealized Hysteretic Behavior |  |  |   |  |
| Idealized Physical Model      |  |  | Idealized Model Not Available                                                        |  |

Figure 20: Comparison between the most commonly adopted passive dampers used for seismic applications with potential for progressive collapse applications [163]

In terms of modern research and design, there have been various developments and applications for dampers. Some of these variations include integrated

damper and bracing systems [164, 165], Triangular-plate Added Damping and Stiffness (TADAS) dampers [166], infilled-pipe dampers (IPD) [167] and bell-shaped dampers [168]. Currently, most of the investigations undergone regarding dampers consider testing under seismic or wind loading only. However, limited research investigated the impact of dampers on progressive collapse resistance. An example is the research conducted by Kim et al. [123]. In their work, Kim et al. [123] tested the influence of their proposed integrated frictional damper and cable systems on structural resistance under column removal scenarios by performing a series of non-linear dynamic analyses. Although this method was developed mainly for seismic loading, models retrofitted with this system proved to be stable under middle and corner column removal scenarios, but the un-retrofitted models for the same structure collapsed under all column removal cases.

As can be concluded from the previous research regarding this topic in the literature, dampers can have significant positive contributions in reducing damage from seismic events. The practicality and effectiveness of dampers as a progressive collapse measure are yet to be determined. However, given their well-documented effectiveness in dissipating seismic energy, dampers may be used to assist in dissipating energy resulting from the initialising source of a progressive collapse event and the impact of debris.

#### 6.2.1.6 Non-structural Measures

Designing a structure to have sufficient inherent robustness and resilience against all potential threats, for direct habitability purposes, can be extremely costly. Therefore, rather than robustness, collapse resistance can be seen as the goal of many mitigation methods, CoPs, standards and guidelines. As mentioned in Section 1, collapse-resistant structures can use non-structural members to help mitigate the risks of an abnormal loading event. Those measures can be divided into two main types. The first type helps ensure that a potential source of impact is not within a distance that can influence the building. An example of this

kind of system is the pillar barriers, which prevent vehicles from being within a certain distance of a structure [169]. The second type of system is based on the use of sacrificial energy-dissipating elements. In this system, sacrificial elements, such as energy-absorbing cladding, can be installed to dissipate energy from a potential threat, leaving the main structural system minimally damaged. Overall, this method aims to reduce the probability of initial local failure rather than prevent failure propagation.

#### 6.2.2. Mitigation Methods

The progressive collapse mitigation techniques/ devices that will be explored in this section are segmentation, structural fuses and energy absorption units.

##### 6.2.2.1 Segmentation

As discussed in Section 4.2.3, continuity can be the basis of collapse progression in many cases. This is due to the fact that when a section fails, and its loads get redistributed to neighbouring sections, these sections might not be of adequate strength and capacity to carry the additional loading. This can lead to the failure of the neighbouring sections, causing additional successive damage until a considerably large area of a structure is damaged. This issue has two main solutions. The first, most commonly used one and currently recommended by the CoPs, is to ensure continuity but at the same time adequately design alternative load paths to ensure that they do not fail with the additional redistributed loads. This solution can result in extremely uneconomic designs, especially in structures with larger spans. The second method, segmentation, is still being developed to this date [170].

Segmentation mainly describes applying the concept of collapse isolation in a structure horizontally or vertically [5]. Horizontal segmentation is usually applied in structures with a lower height-to-width ratio, such as bridges. Moreover, vertical segmentation is conceptually developed for structures with a high height-to-width ratio, such as high-rise structures. In both cases, a structure

1574 is strategically divided into sections, horizontally or vertically, based on prede-  
1575 fined acceptable damage areas. The chosen sections are separated by elements  
1576 that isolate the different parts of the structure. These elements are designed to  
1577 either be weaker or stronger than the rest of the structure and mainly aim to  
1578 prevent excessive load redistribution to neighbouring sections and, consequently,  
1579 damage [171].

1580

1581 Stronger isolating elements are typically considered in the form of strong floors  
1582 and could be applied in vertical segmentation as illustrated in Figure 21(a).  
1583 This is since, in high-rise structures, one of the main causes of collapse progres-  
1584 sion, after the initial damage, is unaccounted for impact loading from falling  
1585 debris, similar to WTC1 and 2 cases. The main function of strong floors is to  
1586 try and dissipate as much kinetic energy as possible from the upper floors to  
1587 mitigate the effects of the impact on subsequent floors. Strong floors should  
1588 have considerable ductility and strength to ensure that they can undergo ade-  
1589 quate deformation for energy dissipation purposes. According to Starossek [5],  
1590 this can be achieved by using thick reinforced concrete slabs coupled with en-  
1591 ergy absorption methods, such as the ones proposed by [47, 164], as shown in  
1592 Figures 21(b) and (c).

1593

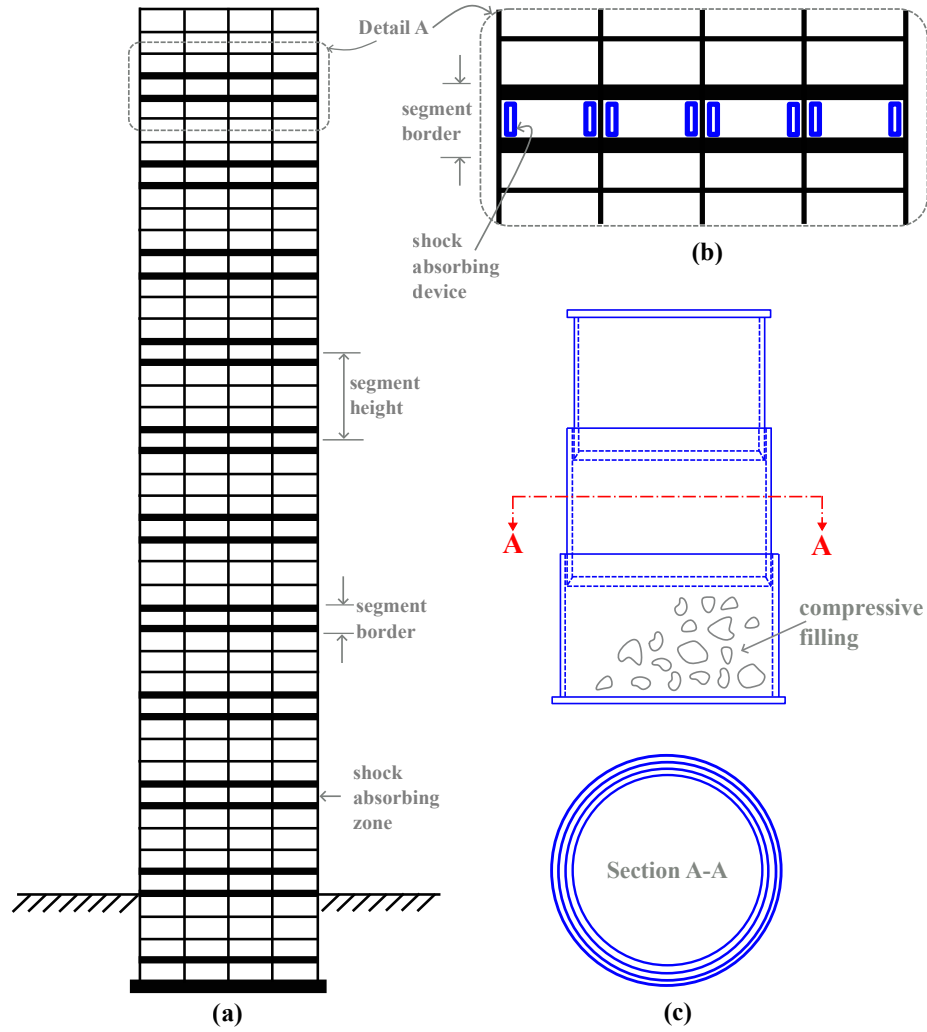
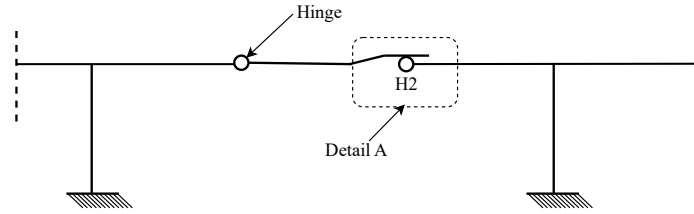


Figure 21: Vertical segmentation in a high-rise structure: (a) vertically segmented structure, (b) shock absorbing zone, and (c) shock-absorbing device, adapted based on [171]

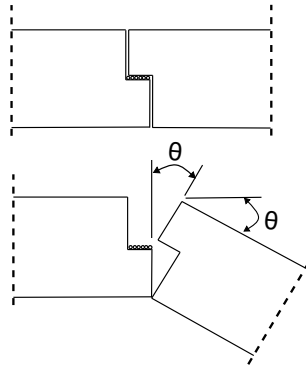
1594 In terms of horizontal segmentation, weaker elements are usually considered  
 1595 since they can act as structural fuses. This conceptual design was successfully  
 1596 applied in seismic design [172, 173, 174, 175, 176, 177]. The application of struc-  
 1597 tural fuses will be further explained in Section 6.2.2.2. In terms of progressive  
 1598 collapse, weak elements can act as points of discontinuity since any additional  
 1599 loading might damage these elements and lead to their failure. This helps pre-  
 1600 vent load redistribution to neighbouring sections beyond a certain limit. Other

1601 methods of implementing segmentation can be through utilising expansion joints  
 1602 or hinges at the borders of segments depending on the nature of a structure [85].  
 1603  
 1604 The concept of segmentation using hinges was successfully applied in the Con-  
 1605 federation Bridge [178]. The Confederation Bridge is a 12.9 km highway bridge  
 1606 in Canada consisting of 43 250m main spans. Designing the bridge using the  
 1607 traditional ALP method would have led to an inefficient design with a dra-  
 1608 matic cost increase. Thus, the bridge engineers decided to apply the concept  
 1609 of segmentation in its design. The most viable option was to have segmented  
 1610 sections in the bridge implemented through drop-in girders and hinges incor-  
 1611 porated within every other span (Figure 22) [30]. This ensures that in case of  
 1612 failure, drop-in girders will disengage and fall into the underlying watercourse,  
 1613 leaving independent, stable sections of the bridge behind.

1614



(a) Hinge and drop-in girder utilisation



(b) Detail A: Disengagement of drop-in girder

Figure 22: Confederation Bridge segmentation strategy, (a) adapted based on [178] and (b) adapted based on [30]

1615 It is important to note that segmentation has only been studied conceptually  
 1616 and theoretically with very limited practical applications, making the Confeder-  
 1617 ation Bridge the most prominent real-life example. Other examples where com-  
 1618 partmentalisation, or in other words, segmentation, has possibly helped prevent  
 1619 collapse propagation include the Pentagon Building in Virginia and Charles de  
 1620 Gaulle Airport Terminal in Paris [30]. The Pentagon Building consists of three  
 1621 rings of buildings, each divided into five sections using expansion joints. When  
 1622 the Pentagon was hit by a plane in 2001, one section of the outer rings was  
 1623 severely damaged. However, this damage did not propagate past the point of  
 1624 discontinuity, which is the expansion joint, to other neighbouring sections. If  
 1625 continuity existed between the joints, collapse progression would have occurred  
 1626 since the impacted section of the structure was severely damaged. Regarding  
 1627 Charles de Gaulle Airport, the collapse was initiated by the failure of a portion  
 1628 of the roof due to poor workmanship. This collapse was stopped at the joints,  
 1629 which separated the collapsing section from the adjacent structure. Similar to  
 1630 the Pentagon building, in case this structure was continuous, it seems unlikely  
 1631 for the undamaged section to have sustained the additional induced forces from  
 1632 the collapse. This can be attributed to the construction deficiencies that were  
 1633 present within the adjacent sections as well. Although in both examples, seg-  
 1634 mentation was not used directly to address progressive collapse, these incidents  
 1635 portrayed the potential benefits of this method as a progressive collapse miti-  
 1636 gation technique [30].

1637

1638 Despite the potential benefits of segmentation, concrete standard procedures  
 1639 for it have not yet been developed. Thus, this method should be studied in-depth  
 1640 as it could be very valuable to the field, especially if it is optimised economically  
 1641 and practically. To satisfy the CoPs while implementing this method efficiently,  
 1642 a structure can be designed to incorporate redundancy and load redistribution  
 1643 within the borders of its identified segments. This will ensure that a segment can  
 1644 withstand minor element losses without failure. However, if a certain loss limit  
 1645 is exceeded, the damage will not propagate to other segments of the structure.

### 1646 **6.2.2.2 Structural Fuses**

1647 Structural Fuses are elements in a structure designed to endure most damage  
1648 while keeping the rest of the structure undamaged. This is usually done by  
1649 ensuring that the fuse elements have sufficient ductility and stiffness to be able  
1650 to deform plastically while keeping the rest of the structure within the elastic  
1651 deformation limits [172]. This mainly aims to limit the damage to only the  
1652 sacrificial fuse elements. Moreover, structural fuses should be designed to be  
1653 easily replaced or repaired [174]. This helps ensure that damaged members can  
1654 be replaced in a rapid and economical manner, ensuring limited cost and in-  
1655 terruption to the operation and functionality of a structure [177]. To maintain  
1656 the stability of a structure after damage sustained by fuses following an ex-  
1657 treme event, they can be designed to have clear limits for the acceptable loss in  
1658 strength levels that they can endure as they undergo deformation. For example,  
1659 Knoll and Vogel [179] proposed that ductility utilisation and undergoing plastic  
1660 deformation should not cause more than a 20% degradation in the resistance of  
1661 the fuse elements to ensure the stability of the rest of the structure. Alterna-  
1662 tively, the remaining sections of the structure can be designed to be structurally  
1663 independent if the fuses are damaged.

1664

1665 To date, most research and applications of structural fuses have been fo-  
1666 cused on seismic design in both buildings and bridges. For example, Han et al.  
1667 [176] investigated the utilisation of shear keys in bridges as sacrificial elements  
1668 to help limit transverse displacements in the superstructure and control damage  
1669 to the substructure. In terms of buildings, some of the proposals included the  
1670 incorporation of fuses within elements, such as masonry infill walls [146] and  
1671 concrete-filled steel members [174], or structural systems, such as H-frame sys-  
1672 tems [177].

1673

1674 The implementation of structural fuses in progressive collapse design has not  
1675 yet been adequately studied. However, it can potentially be a viable option

in the mitigation of progressive collapse [179]. Some of the aspects that need to be investigated in such a method include the required initial and residual stiffness, ductility, and strength levels. Additionally, the impact of fuse damage and deterioration of strength on the rest of the structure should be investigated. Potentially, fuses can be applied in progressive collapse design to utilise the advantages of both continuity and segmentation. For example, for small initial failures, fuses could provide some degree of continuity to help in load redistribution and the mobilisation of alternative load paths. However, for larger initial failures, where collapse progression is inevitable, fuses can enable the implementation of segmentation in a structure to limit collapse propagation to other sections of the structure.

### 6.2.2.3 Energy Absorption Units

Szyniszewski and Krauthammer's [180] study on energy-based progressive collapse analysis reveals that energy in such events is divided into kinetic and potential forms. Kinetic energy is involved in debris impact, while potential energy is stored in static storeys before being impacted by falling material. Kinetic energy from moving particles is typically dissipated through buckling or deformations. Bazant and Verdure's [32] study suggests that if a collapsing storey's kinetic energy exceeds the energy dissipated by crushing a subsequently impacted storey, progressive collapse cannot be halted.

Furthermore, from the column removal progressive collapse analysis conducted in Szyniszewski and Krauthammer's [180] research using the implicit dynamic analysis, it was deduced that beams critically contribute to the energy redistribution in a building during a progressive collapse. Additionally, the buckling of various members in the structure can significantly assist in further energy dissipation. This led to highlighting the importance of investigating buckling from an energy rather than force-based perspective and the effect on member strength that has over time. Moreover, from investigating the WTC incident, Zhou and Yu [47] found that the damage and plastic deformations endured by exterior columns led to the dissipation of only around 6.7% of the

1706 kinetic energy involved with the impacting plane and the rest of the energy was  
1707 dissipated by the crushing and deformation of internal sections of the structure.  
1708 Thus, this indicates that the collapse of the rest of the structure happened due  
1709 to the kinetic energy associated with the debris free-falling through the storeys  
1710 of the building rather than from the initial impact itself.

1711

1712 From the previous energy-based research in progressive collapse, one main thing  
1713 can be concluded, which is that energy dissipation and absorption can be one  
1714 of the key mitigation techniques. This can be achieved through two main ways:  
1715 utilising buckling and deformation capacities of members and through installing  
1716 additional energy absorption devices. In the case of the WTC, the plastic reserve  
1717 of the towers was enough to stop the plane from further propagating. Still, it  
1718 was not enough to halt the impact of falling debris from damaging lower storeys  
1719 and thus causing further collapse propagation. Thus, Zhou and Yu [47] proposed  
1720 the installation of highly ductile, energy-absorbing devices. The concept of the  
1721 proposed devices is to undergo crushing to dissipate the maximum amount of  
1722 energy from the collapse of preceding storeys to halt collapse progression rather  
1723 than prevent its initiation. To do so, the devices are to be designed similarly to  
1724 a ‘stocky column’ with enough cross-sectional area to ensure compressing and  
1725 crushing rather than buckling. Figure 23 shows typical energy absorption lattice  
1726 structures similar to the original proposed aluminium design by Zhou and Yu  
1727 [47]. Zhou and Yu [47] argued that their proposal is much more cost-effective  
1728 than a proposal aimed at completely preventing collapse, as this will require  
1729 achieving impractical levels of strength and ductility in the overall structure.

1730

1731 The application of energy absorption devices in high-rise structures could have  
1732 major benefits. However, the main issue with such devices is capital cost. This  
1733 is mainly because although the costs and losses associated with progressive  
1734 collapse events are extremely high, they are very rare events. Therefore, it could  
1735 be infeasible to allocate large budgets to mitigation devices that will most likely  
1736 never be used in the lifetime of a structure. However, because of their potential

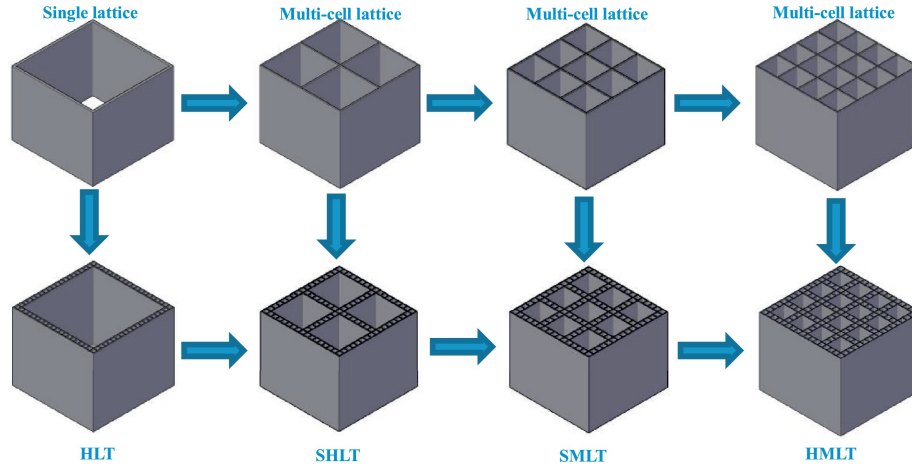


Figure 23: Typical energy absorption lattice structures (HLT: hierarchical lattice tube, SHLT: super hierarchical lattice tube, SMLT: super multi-cell lattice tube and HMLT: hierarchical multi-cell lattice tube) [181]

1737 advantages, these suggested devices can be improved in terms of size, design,  
 1738 and material to provide a practical, dependable, and affordable alternative.

### 1739 6.3. Summary

1740 From this section, as summarised in Table 11, it can be concluded that  
 1741 there are numerous proposals for collapse prevention and mitigation techniques.  
 1742 The primary issue with most of these approaches is that they are either not  
 1743 practical or adaptable enough to be used regularly in the industry or need addi-  
 1744 tional research and validation. For a proposed method to be widely accepted, it  
 1745 must fulfil the following criteria: functionality, cost-effectiveness, sustainability,  
 1746 applicability to various structures, thorough testing, and codifiability. To meet  
 1747 these criteria, various concepts may be implemented simultaneously to ensure  
 1748 effectiveness while eliminating high additional costs.

1749

1750 Moreover, as was discussed previously in Section 4, current codes of practice  
 1751 have various gaps associated with them. Some of these gaps, specifically related  
 1752 to the proposed mitigation and prevention methods, have been addressed by  
 1753 researchers in various ways, as summarised within this section. In order to  
 1754 address some of the codes' gaps while ensuring efficient and economical design,

Figure 24 proposes a possible framework that can be followed in the progressive progressive collapse design of most buildings. This framework aims to ensure code compliance by incorporating the main guidance provided by the discussed codes while addressing several identified gaps, through incorporating various research proposals.

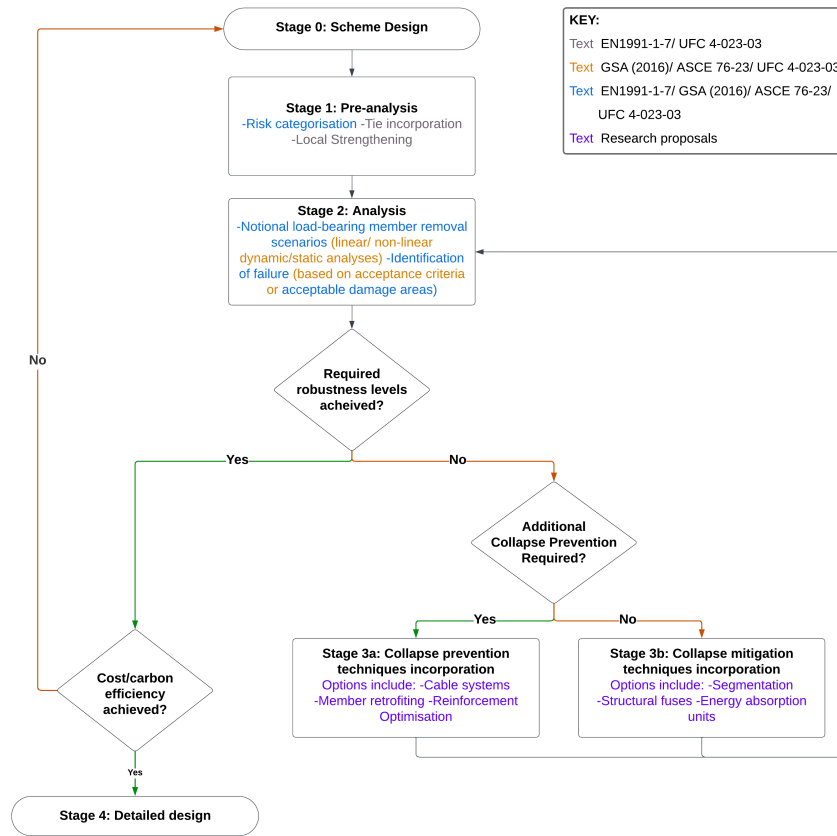


Figure 24: Proposed framework for progressive collapse design based on current knowledge

Table 11: Proposed methods for progressive collapse resistance following local failure

| Type       | Proposed Method                                                                                     | Description                                                                               | Advantages                             | Disadvantages                                                               |
|------------|-----------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------|----------------------------------------|-----------------------------------------------------------------------------|
| Mitigation | -Segmentation<br>-Structural fuses<br>-Energy absorption devices<br>-Steel cable system             | -Some failure is allowed<br>-Overall structural integrity is prioritised                  | -Economic design                       | -Some sections of the structure are allowed to fail                         |
| Prevention | -Member retrofiting<br>-Additional reinforcement<br>-Seismic design<br>-Bracing systems<br>-Dampers | -All failure should be prevented<br>-Structure is designed to bridge over failed elements | -Additional failure is not anticipated | -Uneconomic design<br>-Infeasible for longer spans and irregular structures |

## 1760 7. Other Considerations

1761 Various factors could be attributed to the progressive collapse resistance of a  
1762 structure. Progressive collapse occurrences may be better understood and rep-  
1763 resented by taking these variables into thorough analysis and comprehension.  
1764 Some factors are general and apply to various structures, while others are more  
1765 applicable to specific structural forms. This section assesses the contribution of  
1766 some general variables, such as column removal locations, structural arrange-  
1767 ment, construction errors, and deterioration. Additionally, factors related to  
1768 specific types of construction, such as precast concrete, timber and modular  
1769 structures, are also considered.

### 1770 7.1. Significance of Column Loss Location

1771 The location and number of columns lost following a threat scenario have  
1772 a significant impact on the behaviour of a structure in terms of progressive  
1773 collapse. Several researchers have tried to investigate this issue by removing  
1774 individual columns or, less commonly, several columns to better understand  
1775 how this might affect the collapse resistance properties of a structure. Mostly,  
1776 researchers investigate the loss of ground floor columns as they are the most  
1777 likely to be affected by different types of disasters [84]. Furthermore, several  
1778 researchers concluded that corner column loss had the most adverse effects on  
1779 the considered structures [182, 183, 84, 184]. This can be attributed to the fact  
1780 that, as previously discussed in depth, several collapse resistance mechanisms,  
1781 such as compressive arch action and catenary action, highly depend on lateral  
1782 restraint and anchorage to start developing. Thus, a reduction in anchorage crit-  
1783 ically affects the ability of such mechanisms to activate, which in turn reduces  
1784 the overall resistance to the progressive collapse of a structure. This effect is  
1785 further amplified when two adjacent columns are lost at the corner of a building  
1786 [84]. On the other hand, other researchers concluded that other scenarios, such  
1787 as internal or edge column loss, are the most critical cases [185, 186, 187, 188].  
1788 This can be attributed to the additional loading and tributary areas usually

Table 12: Summary of studies investigating the criticality of column loss locations in progressive collapse events

| Reference                     | Considered Structure/s                            | Analysis Method                                                      | Most Critical Column Loss                         |
|-------------------------------|---------------------------------------------------|----------------------------------------------------------------------|---------------------------------------------------|
| Attia et al. [185]            | 10 storey reinforced concrete flat-slab structure | 3D nonlinear dynamic analysis using ELS (AEM)                        | Interior column                                   |
| Gowtham et al. [182]          | 5 storey reinforced concrete frame                | 2D linear static and non-linear dynamic analysis using SAP2000 (FEA) | Corner column                                     |
| Rahnavard et al. [186]        | 20 storey composite steel frame                   | 3D non-linear dynamic analysis using ABAQUS (FEA)                    | Edge column                                       |
| Galal et al. [183]            | 9 storey semi-rigid composite steel frame         | 3D non-linear dynamic analysis using ABAQUS (FEA)                    | Corner column                                     |
| Parisi and Scalvenzi [84]     | 5 storey reinforced concrete frame                | 2D non-linear dynamic analysis using SiesmoStruct (FEA)              | Consecutive columns at the corner of the building |
| Ghassemieh et al. [184]       | 7 and 12 storey moment steel frames               | 2D non-linear dynamic analysis using OpenSEES (FEA)                  | Corner column                                     |
| Anusha and Chakravarthy [187] | 10 storey steel building                          | 3D linear static analysis using SAP2000 (FEA)                        | Interior column                                   |
| Kumar et al. [188]            | 7, 9 and 11 storey reinforced concrete buildings  | 3D linear static and non-linear dynamic analysis using ETABS (FEA)   | Penultimate column                                |

associated with such column locations.

Table 12 summarises various studies conducted to study the impact of column loss locations on progressive collapse resistance. Additionally, further studies are discussed in Makoond et al. [18]. From the considered and presented data, it can be concluded that the criticality of column loss location is highly case-dependent. Thus, factors such as the assessed structural system, geometric and stiffness irregularities, as well as the type of analysis undergone can impact the conclusions of studies addressing this issue. Currently, most research and design CoPs focus on single-column removals. The problem is that it may not reflect the real-life scenarios in many instances. For example, in the case of a malicious blast attack, usually more than a column is damaged and accounting for only a single column loss and designing for that case can be very under-conservative. Therefore, more tests and investigations must be done to gain an in-depth understanding of how the loss of several columns simultaneously impacts a structure [77, 83, 84]. As discussed in Sections 5.2.4 and 4.6, this issue is currently being addressed in ASCE 76-23 since the consideration of multi-element loss scenarios is proposed for higher risk category structures [8].

## 1807 *7.2. Influence of Structural Arrangement*

1808        Structural arrangement highly impacts a structure's reaction to member loss.  
1809        Some factors that can affect a structure's reaction to losing a member include  
1810        the number of storeys, layout, and stiffness distribution. First, structures with a  
1811        higher number of floors tend to have better load redistribution effects. Although  
1812        dead load increases with increased storeys, taller structures have more members  
1813        above a lost column/member, which can help the load redistribution [9]. This  
1814        can be attributed to the fact that most load redistribution in a structure occurs  
1815        in the section directly above the lost member. This conclusion was also made  
1816        by Li et al. [41], where they modelled column removals in 3-storey and 8-storey  
1817        structures with the same structural grid and the 3-storey structure collapsed  
1818        after a column loss, while the 8-storey structure did not.

1819  
1820        Moreover, stiffness distribution in structures has been found to highly affect  
1821        a structure's reaction to progressive collapse. In the USA, a common type of  
1822        structural arrangement adopted for seismic design is one where the perimeter  
1823        of the structure is made of an extremely stiff moment frame while the interior  
1824        frame is moderately stiff. The main issue with this type of structure in terms  
1825        of progressive collapse is that losing an internal column will lead to devastating  
1826        effects due to the unstiffened interior, especially in structures of longer spans.  
1827        However, external column losses will have a much milder impact due to the  
1828        potential ability of a stiff perimeter to redistribute the additional load. WTC7 is  
1829        an example of this type of structure. In the WTC7 collapse event, it is assumed  
1830        that the debris falling from the Twin Towers initiated a fire and some damage  
1831        in the interior section, which then caused the loss of load-bearing capacity of  
1832        other members due to thermal expansion [50]. Soon after that, the structure  
1833        completely collapsed from the inside out since the internal unfortified structure  
1834        could not handle the additional loading imposed on it from other elements,  
1835        especially with the large spans in that structure. The stiff external did not  
1836        provide many benefits in this case since, by the time the load was redistributed  
1837        to the external skeleton, most of the internal structure was assumed to have

1838 collapsed, causing instability to that external section despite its independent  
1839 strength and stiffness.

### 1840 *7.3. Factors for Realistic Representation*

1841 Many aspects associated with progressive collapse are often overlooked for  
1842 simplification purposes because of the lack of adequate financial resources and  
1843 time. Oversimplification, however, can lead to the misrepresentation of the  
1844 true conditions of a building. The aspects that are often overlooked include  
1845 construction tolerances and errors, and structural deterioration. This section  
1846 will focus on explaining the effect of oversimplification on progressive collapse  
1847 studies.

#### 1848 *7.3.1. Construction Errors and Tolerances*

1849 With certain materials, such as steel, a constructed structure will be almost  
1850 identical to the initial design set by structural design engineers with minor con-  
1851 struction tolerances. Other materials, such as concrete, require much higher  
1852 tolerances and include much more variability in the material and construc-  
1853 tion. This is, of course, in addition to construction errors that can occur in  
1854 all projects. The problem with construction errors and unidentified tolerances  
1855 is that they are largely unaccounted for in post-construction analyses and can  
1856 have a major impact on the overall strength of a structure and resistance to  
1857 progressive collapse [42]. In order to ensure that the strength of a structure  
1858 is not overestimated, reasonable construction error tolerances should be taken  
1859 into account in design processes. Furthermore, construction processes must be  
1860 quality-controlled to ensure a structure performs as expected. An example of  
1861 the detrimental effects of construction errors is the collapse of the Sampoong De-  
1862 partment Store in Seoul. The tragic sudden progressive collapse of the 5-storey  
1863 structure was mainly attributed to construction errors and poor construction  
1864 quality. After an in-depth investigation of the event, it was concluded that the  
1865 collapse of Sampoong Superstore was completely preventable, given that the  
1866 construction was quality controlled or that the building was fortified after com-  
1867 pletion of construction upon discovery of faults [31]. Furthermore, in a study

conducted by Careda et al. [34], in which the cause of failure of a number of case studies was analysed, it was found that design errors contributed to 48% of the considered collapses followed by construction errors at 29%. These significant values reinforce the importance of quality control in the design and construction processes of structures.

### 7.3.2. *Deterioration*

With time, due to environmental factors, materials deteriorate, and so do structures. Both seismic and non-seismic structures subject to deterioration were found to have less progressive collapse resistance [142]. This can be associated with material deterioration having decreased ductility and strength, which can lead to disabled compensation mechanisms. An example of this issue can be the collapse of Champlain Towers South in Surfside, Florida. Final conclusions with certainty have not yet been established on the cause of the collapse of this four-decade structure as the incident is still being investigated. However, from initial reports, it was deduced that corrosion due to water leakage substantially weakened the reinforcement in lower levels and thus triggered the initiation of failure. This failure then led to the progressive collapse of a major section of the structure [33]. In the case of Champlain Towers South, if the presumed cause is confirmed, the failure could have been prevented by ensuring adequate waterproofing and drainage systems were in place through regular maintenance checks and interventions. In other cases, such as structures in contact with the ground or seawater, the appropriate concrete types must be used to ensure minimum deterioration and prolonged design lives.

In addition to deterioration resulting from environmental factors, structures' strengths can deteriorate due to events such as earthquakes throughout their lifetime. Some earthquakes or similar events might not be of a significant magnitude to cause a structure to collapse instantaneously, but they might lead to fatigue and deterioration in its members in the form of micro cracking or deformation, for example. Such structures might be able to withstand normal gravity

loading. However, another minor seismic event can lead to its collapse due to the presence of weakened members from previous events. This type of failure can be challenging to prevent if structures are not monitored regularly after seismic events. Therefore, regular rigorous maintenance, although costly, can have major economic, environmental, and safety benefits for structures throughout their lifetime. Moreover, despite the criticality and importance of considering the effects of deterioration and damage accumulation due to multiple hazards on a structural system, progressive collapse design is still performed considering the ideal conditions assumed in the original structural design, disregarding the current and future conditions of a structure. Thus, more studies need to be conducted to assess the effect of current and future structural conditions on the progressive collapse resistance of ageing structures.

#### 7.4. *Considerations for Different Types of Structures*

A building's structural arrangement and its material properties highly govern its behaviour during progressive collapse events. Until this point in the paper, most of the behaviours and mitigation techniques discussed were applicable mainly to framed reinforced concrete and steel structures. Although these behaviours might be relevant to other types of structures, some specific aspects should be taken into account when assessing each type of structure. In this section, specific aspects of different structural systems, including precast concrete, timber, and modular structures, will be highlighted and explored.

##### 7.4.1. *Precast Concrete Structures*

Precast concrete solutions have become very common in recent decades due to the ease, safety, high quality, speed, and control of construction that they offer. Nevertheless, there are a relatively limited number of studies on the progressive collapse resistance of precast elements or whole precast structures. One of the main concerns associated with this construction type is inadequate tying between the elements due to noncontinuous reinforcement, similar to the Ronan Point case [41]. This can prevent the development ALPs and thus lead to direct failure in the section of the structure where a member is lost, consequently

causing further damage propagation. In particular, welded reinforcement at the connections has been found to be particularly problematic. In their research, Qian et al. [144] noticed that welded precast elements could not reach the stage of developing tensile catenary action. This was mainly attributed to the lack of continuity or adequate connection between bars. A proposed solution to this issue is to explore the development and testing of connections of adequate strength and ductility to ensure that the required tying and continuity levels are achieved to enable ALPs to develop. On the other hand, tensioned precast elements were found to achieve substantial improvement in load redistribution, especially over longer spans [90]. To the authors' knowledge, the behaviour of fully precast concrete structures in terms of progressive collapse has not been adequately investigated. Thus, precast structures should be modelled and tested globally (such as in Buitrago et al. [117]) to understand the behaviour of such structures after the loss of load-bearing components. Additionally, connection design in precast structures should be further investigated and developed. For a full review of studies related to precast concrete structure's progressive collapse resistance, the reader is referred to Alshaikh et al. [189].

#### 7.4.2. *Structural Timber*

Timber structures are considered to be a significant part of future buildings because of the environmental advantages of timber construction over concrete or steel structures. The use of wood from sustainably managed forests contributes greatly to reducing  $CO_2$  emissions generated in the construction sector [190]. This main advantage is followed by the outstanding characteristics of energy efficiency, thermal and acoustic comfort, lightness and even fire resistance, as well as the economic and temporal advantages of industrialised construction.

There are different types of timber building structures, which can be classified as roof structures, light-timber, modular timber, CLT-Platform type, and post-and-beam [19, 11]. Apart from 1 or 2-storey buildings (e.g. single-family houses, sports halls, indoor swimming pools), the most commonly used building systems

are the CLT-Platform type or post-and-beam type [191]. It is on these types of structures that existing research to date in the field of structural robustness has focused.

Timber structures can be considered discontinuous due to the way the elements are interconnected. Most failures in such structures occur due to the rupture of the connections, usually before the rupture of the wood itself. Currently, the Eurocode guidance against disproportionate collapse for timber structures follows the general recommendations provided by the code. For example, some of the measures proposed against this issue include ensuring continuity at the connections and providing adequate anchorage. Thus, it is important, as in other types of structures, to provide the structure with redundancy, continuity and ductility at the connections. This can be achieved through common measures such as implementing prescriptive design rules for tying elements and ensuring the activation of ALPs in the structure. Although research in this field has been very limited, and there is still a long way to go, good guidance can be found in [11].

To fill the gaps related to the design of timber structures against progressive collapse, in the past years, a limited number of research studies have been directed towards understanding their resistance and behaviour, as summarised in Table 13. A noteworthy example of this includes the research conducted by Cheng et al. [192], in which strain-rate effects were investigated to successfully predict stiffness, capacity, and nonlinear behaviours of dowel connections under progressive collapse. Moreover, in his study about large-span timber roof structures, Dietsch [193] concluded that most failures of timber structures happen due to a globally weakening event, such as construction errors or erosion, rather than a local event, such as a blast, which also has a much lower frequency of occurrence. Thus, instead of following methods such as key element design, Dietsch [193] proposed the application of compartmentalisation or segmentation in timber structures to ensure increased robustness. In addition, Voulpiotis et al. [194, 195]

considered the robustness of tall timber buildings through its quantification and the definition of a holistic framework for their design, while Cao et al. [196] studied the activation of the catenary action in strip-reinforced timber beams. Other studies [197, 198, 199, 200, 201, 19, 202, 203, 204, 205, 192, 206, 207], aimed to characterise the behaviour of timber structures subjected to the removal of elements. These works studied different types of connections using computational or analytical modelling strategies as well as static and dynamic experimental tests employing different setups, such as sub-assemblies with and without the contribution of slabs.

Despite this previous work, more research in this area is still required to formulate comprehensive and effective progressive collapse guidelines for timber structures. Experimental studies on building systems with more than one floor are still required. At the same time, more types of connections already available in the market should be analysed, and new ones should be designed to improve the robustness of timber structures. One of the key aspects of timber structures is to be able to activate the catenary/membrane action, and this is only possible with ductility, which must be provided by the connections since the timber of the elements is brittle. To date, several studies have highlighted the limitation in this respect [196, 197]. Moreover, the robustness of Modular-Timber or Light-Timber construction has yet to be studied. The former is a research gap that should be covered, although it is highly dependent on the module and the inter-module connections, while the latter seems to have fewer problems from the point of view of robustness against progressive collapse since it is composed of lots of vertical and horizontal elements (ribs and panels) that can accommodate the local failure of some elements. Finally, it should be noted that timber structures are sensitive to scale effects, an aspect that still needs to be assessed and requires urgent attention [200, 199].

Table 13: Summary of progressive collapse studies for timber structures

| Reference                    | Main Aim                                                                                                                                                                                                                         |
|------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Cao et al. [196]             | Derivation of analytical expressions for the elastic, plastic, and catenary capacity of laterally loaded wood and timber beams with a tension-side strip reinforcement in order to achieve the activation of the catenary action |
| Cheng et al. [206]           | Studying the dynamic behaviour after sudden column removal of post-and-beam mass timber frames manufactured from Laminated Veneer Lumber structural products                                                                     |
| Cheng et al. [192]           | Studying the influence of earthquake and progressive collapse strain rate on the structural response of timber dowel connections                                                                                                 |
| Dietsch [193]                | Evaluating the robustness of large-span timber roof structures                                                                                                                                                                   |
| Grantham and Enjily [207]    | A small part of the research aims to study the behaviour of CLT-platform systems subjected to load-bearing wall failure                                                                                                          |
| Hua and Chun [203]           | Understanding the progressive collapse resistance mechanisms of Puo-zuo (an ancient Chinese construction technique) timber buildings                                                                                             |
| Hua et al. [202]             | Studying the progressive collapse behaviour of ancient Chinese timber structures with different joint strengthening techniques                                                                                                   |
| Huber et al. [19]            | A review of robustness in timber buildings                                                                                                                                                                                       |
| Huber et al. [201]           | Studying the ALPs after an internal wall loss, using a 3D FEM non-linear component-based pushdown analysis for a platform-type CLT floor system                                                                                  |
| Lyu et al. [197]             | Testing 2D scaled down timber frame substructures under a middle column removal scenario with three types of commercially available beam-to-column connections and a proposed non-commercial novel connection                    |
| Lyu et al. [199]             | Investigating the structural response of post-and-beam mass timber buildings under edge column removal scenarios using scaled-down experimental models                                                                           |
| Lyu et al. [198]             | Investigating the structural response of post-and-beam mass timber buildings under corner column removal scenarios using scaled-down experimental models                                                                         |
| Lyu et al. [200]             | Investigating the structural response of post-and-beam mass timber buildings under edge and corner column removal scenarios using finite element models                                                                          |
| Mpidi Bitá et al. [205]      | Investigating the structural behaviour of Cross-Laminated Timber (CLT) buildings subjected to the sudden removal of internal and external ground floor loadbearing walls                                                         |
| Mpidi Bitá and Tannert [204] | Adapting the tie-force procedure of the Eurocodes and American guidelines to the case of CLT platform-type systems                                                                                                               |
| Voulpitis et al. [194]       | Discussing the existing state-of-the-art and proposing a holistic framework for considering robustness in the design of tall timber buildings                                                                                    |
| Voulpitis et al. [195]       | Exemplifies in a case study the quantification of robustness in tall timber buildings                                                                                                                                            |

### 2017 7.4.3. Modular Construction

2018 Modular construction is a technique in which a structure is divided into  
2019 smaller units. Each of these units is prefabricated off-site and then transported  
2020 and assembled on-site. These smaller units are called modules and are typically  
2021 designed to be highly similar to ensure the efficiency and cost-effectiveness of the  
2022 design and fabrication processes [208]. This type of construction is referred to  
2023 as being ‘Lego-like’ due to having an end product composed of smaller building  
2024 units assembled with ease. Due to the high regularity between modular units,  
2025 modularly constructed structures inherently possess high levels of redundancy.  
2026 The main issue of concern in this type of structure is connections between mod-  
2027 ules because of its discontinuous nature. Incidentally, in a study conducted by  
2028 Alembagheri et al. [72], modularly constructed steel structures were found to  
2029 perform exceptionally well under module loss scenarios with minor impact on the  
2030 tested structure when a single corner module was removed. This is illustrated in  
2031 Figure 25, where the tested structure managed to successfully bridge over the re-  
2032 moved module. This was mainly attributed to redundancy, as explained earlier,  
2033 and reliable intermodular connections at the corners of each module. Moreover,  
2034 the loss of 2 modules was found to cause collapse only when the modules were  
2035 removed from the longer side of the structure. Finally, the removal of 3 modules  
2036 was found to cause instability in all cases. Modular construction is a novel tech-  
2037 nique that only recently started attracting the interest of progressive collapse  
2038 researchers [209, 210, 211, 212, 213, 214, 215]. Consequently, to date, it remains  
2039 understudied in the progressive collapse field. However, from the research con-  
2040 ducted to date, it can be concluded that intermodular connections have a very  
2041 important role in the progressive collapse resistance of such structures. More-  
2042 over, in terms of progressive collapse, modularly constructed structures can be  
2043 seen as segmented structures with high continuity within the segments or mod-  
2044 ules and controlled continuity between them. For an in-depth review of the  
2045 progressive collapse studies undergone considering modular construction, refer  
2046 to Thai et al. [216].

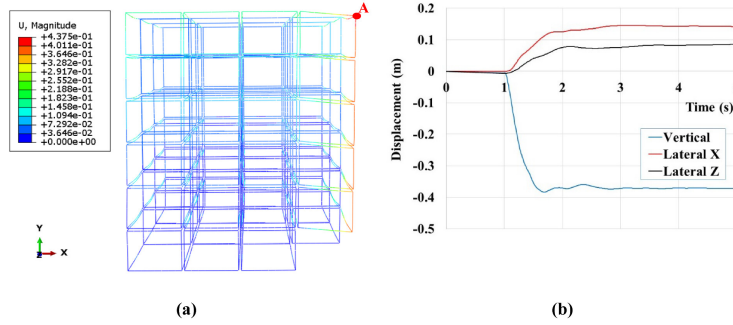


Figure 25: Single module removal for a modular structure: (a) The final equilibrium position of the structure after corner module removal and (b) Time history of global displacements of the roof corner above the missing module, designated by Alembagheri [72]

## 8. Conclusion, Recommendations and Future Needs

This paper presents a comprehensive review of the progressive collapse of framed structures. As progressive collapse is one of the most disastrous types of collapse that needs direct attention in the engineering field, various researchers have attempted to study the topic in recent years. These research works mainly aimed to gain a more in-depth understanding of the phenomenon and consequently develop effective prevention methods against it. Considering this, several CoPs have been developed to address progressive collapse. However, both current research and Codes of Practice lack substantial understanding regarding various aspects of the topic, which are required to enable the development of mitigation approaches and, eventually, CoPs that could provide conclusive and practical guidance to engineers regarding progressive collapse design. Based on this review, some areas that need further investigation include:

1. *Types of progressive collapse*: Studying the types of progressive collapse can help inform the susceptibility of different types of structures to certain types of collapse. This facilitates the process of choosing suitable, effective, and economic mitigation techniques for structures directed toward preventing the types of collapse to which they would be most vulnerable. Several studies have been conducted to investigate the potential types of progressive collapse, but very limited ones focused on the correlation be-

2067       tween structure type and collapse type. Thus, to ensure the efficiency of  
2068       the utilisation of collapse prevention methods, it is recommended that the  
2069       relationship between structure and collapse types be further investigated.

2070   2. *Current codes of practice and design guidelines:* Current international  
2071       codes have a variety of issues associated with them, ranging from being  
2072       incomprehensive to being highly demanding in terms of human and com-  
2073       putational resources. For codes to be effective, they should be able to  
2074       provide reasonable guidance for a designer to produce a robust and pro-  
2075       gressive collapse-resistant structure efficiently. There are several methods  
2076       to achieve this. For example, given the dynamic nature of progressive col-  
2077       lapse research, CoPs need to be regularly revised to integrate novel pro-  
2078       posals and knowledge. Additionally, to ensure the efficiency of structures,  
2079       especially in terms of performance, cost, and carbon expenditure, general  
2080       progressive collapse guidance might not be sufficient. Therefore, specific  
2081       guidance can be provided to structures based on different criteria, such as  
2082       their types, sizes, and susceptibility to certain collapse mechanisms.

2083   3. *Experimental Methods:* Most progressive collapse studies have been per-  
2084       formed on sub-assemblies of structures, which can be very beneficial to  
2085       help in understanding certain relevant local phenomena. However, de-  
2086       pending on local testing to predict global behaviour can be misleading, es-  
2087       pecially in progressive collapse studies, due to the number of variables con-  
2088       tributing to this type of collapse. On the other hand, performing full-scale  
2089       experimentation can be extremely demanding in terms of time, cost, re-  
2090       sources and expertise. Thus, alternative methods to investigate the global  
2091       behaviour of progressive collapse need to be investigated. An example of  
2092       this can be the development of scaling laws to enable the performance of  
2093       representative experiments using scaled-down models of structures. This  
2094       can help critically reduce costs and eliminate spatial restrictions usually  
2095       associated with progressive collapse studies while providing an expedited  
2096       testing nature.

2097   4. *Numerical Modelling:* The majority of numerical progressive collapse stud-

ies conducted to date are performed using FEA. Although FEA has numerous benefits, it cannot accurately represent progressive collapse once the elements start to separate / fail or in stages of larger strains. Several researchers attempted to integrate different methods within FEA to provide a more realistic representation of progressive collapse, which led to the development of solutions with mostly impractical computational demands. Consequently, some researchers have worked to develop alternatives for FEA. One of these methods is AEM. AEM has been shown to have an extremely high potential for progressive collapse studies. However, this method still requires further validation and testing to ensure reliability. In addition, different structural arrangements must be considered in the investigation processes.

5. *Analytical Methods*: Various researchers have developed analytical methods to help quantify various parameters related to progressive collapse. The proposed analytical methods in this field can be divided into three main categories: robustness quantification, collapse resistance capacity and dynamic amplification factor determination. Several proposed methods require further development and validation to ensure their effectiveness and applicability. For example, the proposed methods for the determination of the collapse resistance capacity of an overall structural frame are extremely limited when compared to methods directed towards a member or sub-assembly capacity. Due to the complexity of progressive collapse considerations, most methods might not provide accurate parameters, but such methods can be used as useful approximation tools.

6. *Machine Learning and Physics Engine*: These are valuable tools in progressive collapse studies, aiding engineers and researchers in understanding structures. The main challenge is to collate reliable and accurate data that helps to build machine learning models. It has been shown that the required data can be generated using validated engineering numerical models. At this present time, challenges regarding the physics engine are related to the accurate representation of the physical behaviour of struc-

tures. Due to recent advances in computing, developing an accurate model in a physics engine is not far in the future. Therefore, these fields of study are expected to boom in the near future. For these reasons, future research directions using the physics engine and machine learning are outlined in Sections 6.1.2 and 6.4, respectively.

7. *Mitigation and Prevention Methods:* Over the past decades, several progressive collapse prevention and mitigation methods have been developed. Overall, mitigation methods can be seen as a more efficient solution, but numerous projects will still require ensuring the prevention of collapse. Moreover, although many current prevention methods have proved effective, their generalised application to all types of structures may be uneconomical and impractical. Thus, a solution for this issue can be attempting to optimise the use of each method by directing it to certain structural types or alternatively by combining some mitigation and prevention techniques in certain applications. For instance, relying on catenary action and developing ALPs may be suitable for structures of shorter spans since neighbouring elements may reasonably sustain the redistributed load from a lost member. On the other hand, achieving this might lead to unreasonable increases in section sizes in taller structures with larger spans. Thus, for such structures, implementing the concept of segmentation may yield several benefits. Theoretically, segmentation has a very high potential when applied to taller or longer structures but is yet to be fully investigated and validated. Investigating the applicability of such concepts can have extremely beneficial contributions towards further understanding how to best optimise mitigation and prevention methods in progressive collapse design. Moreover, the global impact of all proposed methods should be carefully considered. This will help eliminate issues that are not apparent on a sub-assembly scale. An example of this is the effect of catenary action on surrounding elements, such as the deflection of neighbouring columns. This phenomenon, for example, needs to be further investigated due to its potential implications on collapse propagation.

- 2160 8. *Realistic Representation and Research Assumptions*: Most progressive col-  
2161 lapse research has focused on studying frame models consisting mainly of  
2162 beam and column elements. While this is essential to provide a basic un-  
2163 derstanding of the collapse resistance mechanisms in framed structures,  
2164 the contribution of other structural and non-structural elements, such as  
2165 masonry infill walls and slabs, whether advantageous or not, has been  
2166 largely disregarded. The impact of these elements, which are present in  
2167 most typical structures, needs to be further investigated locally and glob-  
2168 ally to ensure that their beneficial contributions are optimised and that  
2169 any attributed risks are eliminated. Furthermore, for studies involving  
2170 new or existing structures, it is important to ensure that factors poten-  
2171 tially impacting structural behaviour, such as deterioration and construc-  
2172 tion errors or tolerances, are adequately incorporated. In other words, the  
2173 realistic representation of structures in the studies conducted helps yield  
2174 more reliable data and conclusions.
- 2175 9. *Other Considerations*: Other contributing factors to progressive collapse  
2176 events have not been fully studied yet. For example, factors such as col-  
2177 umn loss locations, number of storeys, layout and stiffness distribution  
2178 in a structure need to be investigated to clarify their effect on collapse  
2179 resistance. Additionally, understanding the behaviour and specific contri-  
2180 butions of different types of structures needs to be further investigated.  
2181 Most of the progressive collapse studies conducted to date address rein-  
2182 forced concrete or steel structures. However, other types of structures,  
2183 such as precast concrete, timber, modular, lattice and bridge structures,  
2184 remain understudied in the field. Thus, further studies are required to ad-  
2185 dress the gaps in knowledge related to such structures. Understanding the  
2186 general behaviour and specific issues associated with different structural  
2187 typologies will help structural engineers optimise the design and analysis  
2188 processes, which will aid in the construction of more robust structures  
2189 efficiently.

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